

The Study of Excited Baryon Resonances

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Excited QCD 2010

Tatra National Park (Slovakia), 02/03/2010



Outline

- 1 Introduction
 - Toward Complete Experiments
- 2 Experimental Setup: The CLAS Detector at Jefferson Lab
- 3 Photoproduction of a Single (Pseudoscalar) Meson
 - η Photoproduction (off the Proton)
 - π Photoproduction
- 4 Double-Meson Photoproduction
 - $\pi^+ \pi^-$ Photoproduction
- 5 Summary and Outlook



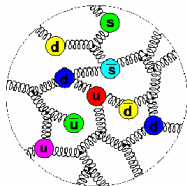
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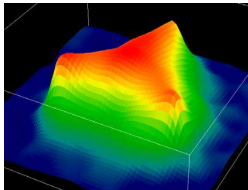
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$\ll 0.1 \text{ fm}$ 

pQCD

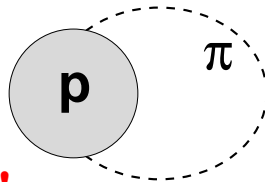
q, g, q \bar{q} 

0.1 – 1.0 fm



Models

Quarks and Gluons
 as Quasiparticles

 $> 1.0 \text{ fm}$ 

ChPT

Nucleon and
 Mesons

- 1 What are the relevant degrees of freedom?
- 2 What are the corresponding effective interactions responsible for hadronic phenomena?

The Excited Baryon Program at Jefferson Lab

The excited baryon program has two main components:

- Establish the systematics of the spectrum
 - Provides information on the nature of effective degrees of freedom in strong QCD
- Probe resonance transitions at different distance scales (electron beams are ideal to measure transition form factors)
 - Provides information on the confining forces of the 3-quark system

One of the Main Goals of the N^* Program ...

Search for *missing* or yet unobserved resonances

Quark models predict many more baryons than have been observed

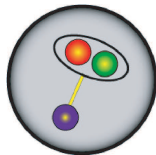
	****	***	**	*
N Spectrum	11	3	6	2
Δ Spectrum	7	3	6	6

\Rightarrow according to PDG
 (Phys. Rev. **D66** (2002) 010001)

\Rightarrow little known
 (many open questions left)

Possible solutions:

1. Quark-diquark structure



one of the
 internal degrees
 of freedom
 is frozen

2. Have not been observed, yet

Nearly all existing data result from
 πN scattering experiments

\rightarrow If the missing resonances did not couple to
 $N\pi$, they would not have been discovered!!

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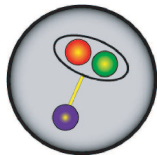
(Phys. Lett. B **667**, 1 (2008))

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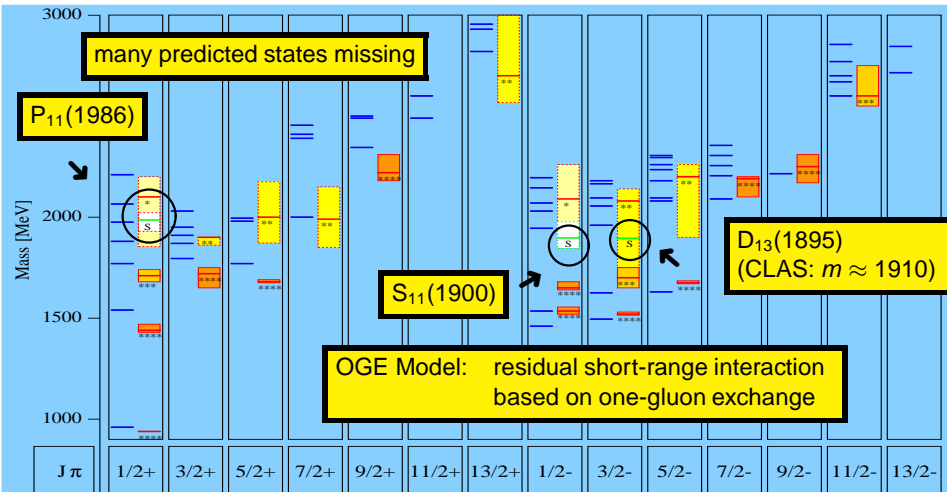
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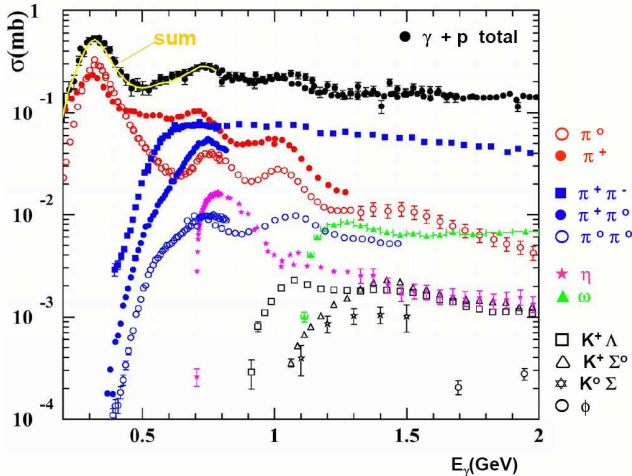
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Nucleon Resonances: Status of 2001

— S. Capstick and N. Isgur, Phys. Rev. **D34** (1986) 2809

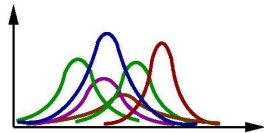


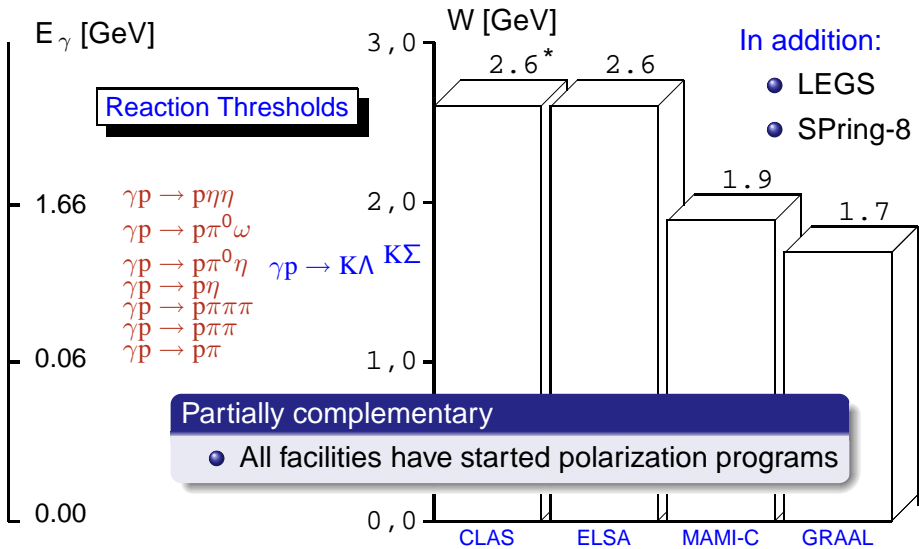
Total Photoproduction Cross Sections



No peak hunting

- Decays into neutral and charged particles
- Broad resonances





Ingredients

- Measurements off neutron and proton to resolve isospin contributions
 - ① $\mathcal{A}(\gamma N \rightarrow \pi, \eta, K)^{I=3/2} \iff \Delta^*$
 - ② $\mathcal{A}(\gamma N \rightarrow \pi, \eta, K)^{I=1/2} \iff N^*$
- Re-scattering effects: Large number of measurements (and also final states) needed to define the full scattering amplitude
- Double-polarization measurements

Chiang & Tabakin, Phys. Rev. C**55**, 2054 (1997)

In order to determine the full scattering amplitude without ambiguities, one has to carry out eight carefully selected measurements: four double-spin observables along with the four single-spin observables.

Photon beam		Target			Recoil			Target - Recoil										
					x'	y'	z'	x'	x'	x'	y'	y'	y'	z'	z'	z'		
		x	y	z				x	y	z	x	y	z	x	y	z		
unpolarized	σ_0		T			P				$T_{x'}$		$L_{x'}$		Σ		$T_{z'}$		$L_{z'}$
linearly P_γ	Σ	H	P	G	$O_{x'}$	T	$O_{z'}$	$L_{z'}$	$C_{z'}$	$T_{z'}$	E		F	$L_{x'}$	$C_{x'}$	$T_{x'}$		
circular P_γ		F		E	$C_{x'}$		$C_{z'}$		$O_{z'}$		G		H			$O_{x'}$		

status	CLAS run period	beam	target	
complete	g1	$\gamma, \vec{\gamma}_c$	LH ₂	Miskimen/Schumacher
complete	g8	$\vec{\gamma}_L$	LH ₂	Cole
complete	g9a - P_z^T	$\vec{\gamma}_L, \vec{\gamma}_c$	FROST - C ₄ $\vec{H}_9, O\vec{H}$	Klein, Pasyuk
2010	g9b - P_x^T	$\vec{\gamma}_L, \vec{\gamma}_c$	FROST - C ₄ $\vec{H}_9, O\vec{H}$	Klein, Pasyuk

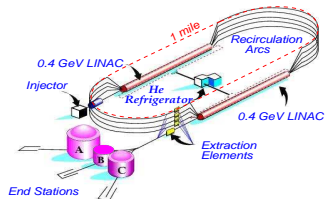
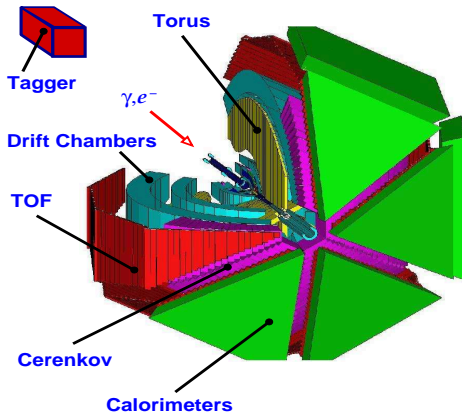
Full set of 16

Picture taken from A. Sandorfi

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CLAS Spectrometer



CHARACTERISTICS:

Electron Coverage: $\theta : 15-50^\circ$

Hadron Coverage:

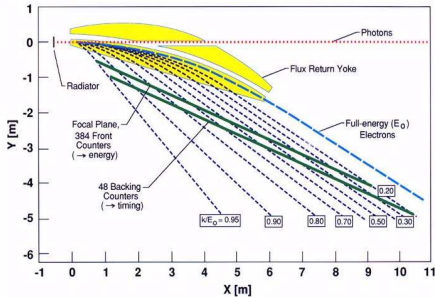
$\theta : 15-140^\circ, \phi : 80\% 2\pi$

Resolution : $\Delta p/p \sim 1-2\%$
 $\Delta\theta, \Delta\phi \sim 2 \text{ mrad}$

$\mathcal{L} = 1 \times 10^{34} \text{ cm}^{-2} \text{ sec}^{-1}$

$\mathcal{F}_\gamma = 1 \times 10^7 / \text{s}$

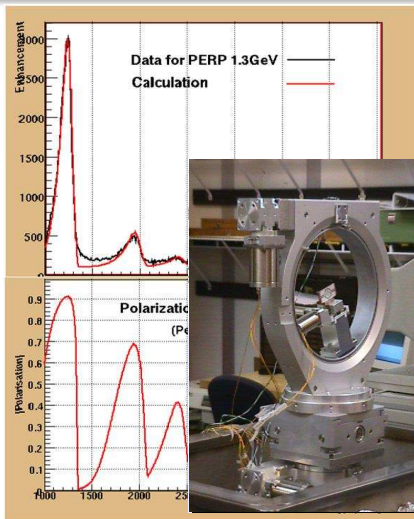
The Hall-B Photon Tagging Facility



Photons via Bremsstrahlung:

- $E_\gamma = 20 - 95\%$ of E_0
- E_γ up to ~ 6 GeV
- $dE/E \sim 10^{-3}$ of E_0

The Coherent Bremsstrahlung Facility at CLAS

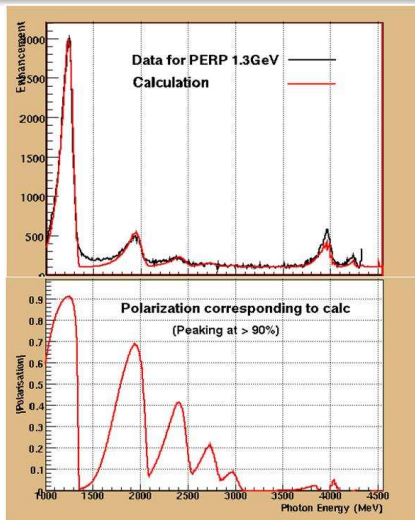


g8b Run Group (data from 2005)

Bremsstrahlung in 50μ diamond:

- 40 cm liquid hydrogen target located 20 cm upstream
- Two linear polarization states (vertical & horizontal)
- Incident electron energy from CEBAF of 4.55 GeV
 $\rightarrow 1.0 \text{ GeV} < E_\gamma < 2.1 \text{ GeV}$
- Single-charged particle trigger

The Coherent Bremsstrahlung Facility at CLAS



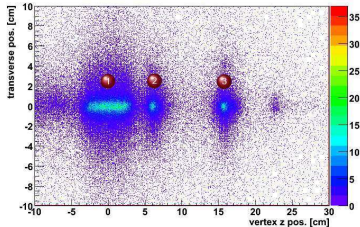
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The Frozen-Spin (FROST) Target

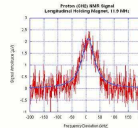
vertex cut



$$\Delta B/B \approx 3 \cdot 10^{-3} \text{ at } 0.5 \text{ T}$$

$$B \approx 0.5 \text{ T}$$

$$T \approx 0.05 \text{ K}$$



Production Data

- Target (Butanol)

Longitudinally-polarized target
 Average polarization $\sim 80\%$
 Additional targets: ^{12}C , CH_2

- Photon Beam

Circular and linear Polarization
 Excellent degrees of polarization

Target Performance

28 mK w/o beam
 30 mK with beam

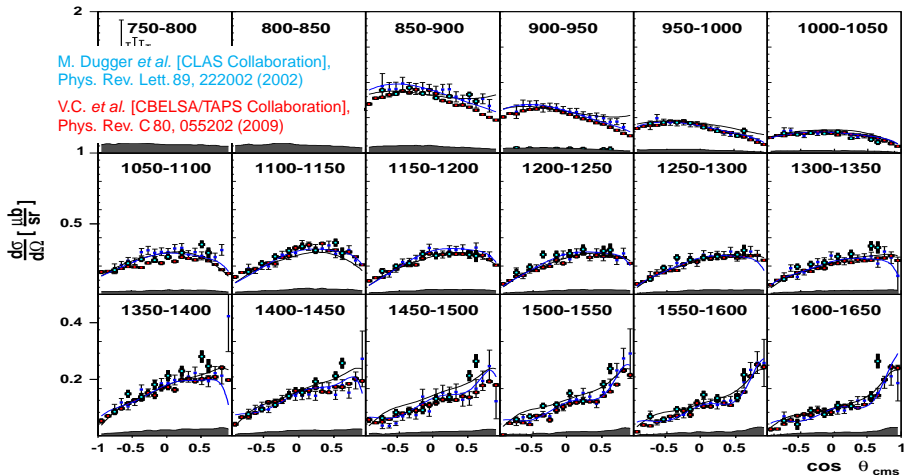


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Photoproduction of η Mesons off the Proton

— CB-ELSA/TAPS — CB-ELSA — CLAS — SAID — BoGa Fit

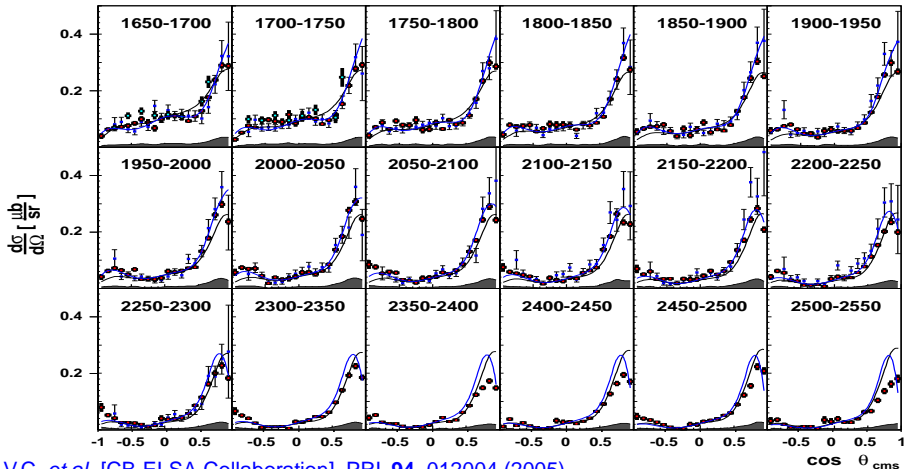


M. Dugger *et al.* [CLAS Collaboration],
 Phys. Rev. Lett. 89, 222002 (2002)

V.C. *et al.* [CBELSA/TAPS Collaboration],
 Phys. Rev. C 80, 055202 (2009)

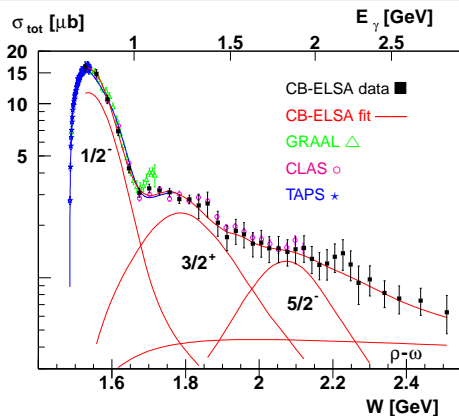
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V.C. *et al.* [CB-ELSA Collaboration], PRL **94**, 012004 (2005)

Analysis of $\gamma p \rightarrow p\eta$: Total Cross Section



Isospin Filter

→ Only N^* resonances can contribute!

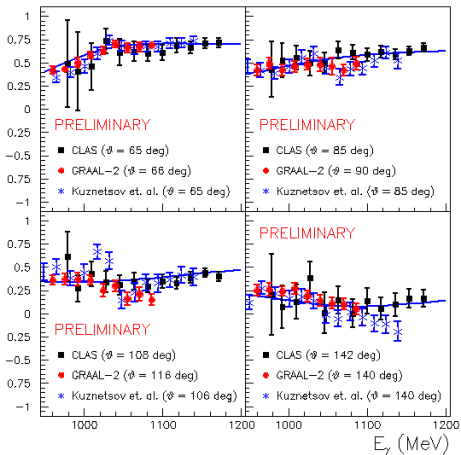
Bonn-Gatchina (PWA) group:
 Hint for N^* resonance (2070) D_{15}
 (Phys. Rev. Lett. **D94**, 012004 (2005))

Three resonances are dominantly contributing:

$N(1535)S_{11}$, $N(1720)P_{13}$, $N(2070)D_{15}$

Beam Asymmetry Σ in the Reaction $\vec{\gamma}p \rightarrow p\eta$

Higher sensitivity due to interference effects: $\Sigma \sim A_{1/2}(S_{11}) * A_{1/2}(P_{13}) + \dots$

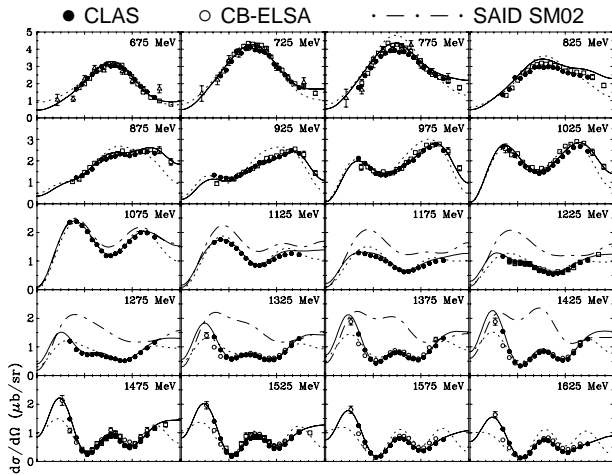


Further spin observables available

- E and G from FROST run with longitudinal target polarization (2007/2008)
- T, F, and H will be available from FROST run with transverse target polarization (Spring 2010)

P. Collins, CLAS g8b run group, to be published

Photoproduction of π^0 Mesons off the Proton



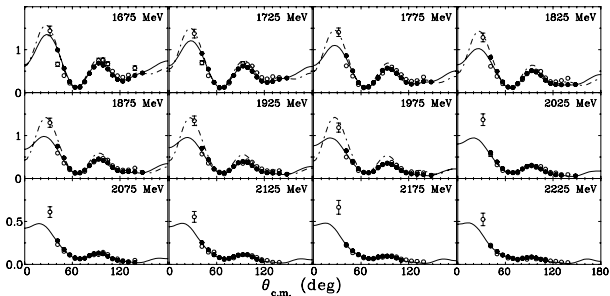
Resonance	πN SAID	$A_{1/2}$	$A_{3/2}$
$N(1535)S_{11}$	$W_R=1547$ MeV $\Gamma=188$ MeV $\Gamma_R/\Gamma=0.36$	91.0 ± 2.2 90 ± 30	
$N(1650)S_{11}$	$W_R=1635$ MeV $\Gamma=115$ MeV $\Gamma_R/\Gamma=1.00$	22.2 ± 7.2 53 ± 16	
$N(1440)P_{11}$	$W_R=1485$ MeV $\Gamma=284$ MeV $\Gamma_R/\Gamma=0.79$	-50.6 ± 1.9 -65 ± 4	
$N(1720)P_{13}$	$W_R=1764$ MeV $\Gamma=210$ MeV $\Gamma_R/\Gamma=0.09$	96.6 ± 3.4 18 ± 30	-39.0 ± 3.2 -19 ± 20
$N(1520)D_{13}$	$W_R=1515$ MeV $\Gamma=104$ MeV $\Gamma_R/\Gamma=0.63$	-28.0 ± 1.9 -24 ± 9	143.1 ± 2.0 166 ± 5
$N(1675)D_{15}$	$W_R=1674$ MeV $\Gamma=147$ MeV $\Gamma_R/\Gamma=0.39$	18.0 ± 2.3 19 ± 8	21.2 ± 1.4 15 ± 9
$N(1680)F_{15}$	$W_R=1680$ MeV $\Gamma=128$ MeV $\Gamma_R/\Gamma=0.70$	-17.3 ± 1.4 -15 ± 6	133.6 ± 1.6 133 ± 12
$\Delta(1620)S_{31}$	$W_R=1615$ MeV $\Gamma=147$ MeV $\Gamma_R/\Gamma=0.32$	49.6 ± 2.2 27 ± 11	
$\Delta(1232)P_{33}$	$W_R=1233$ MeV $\Gamma=119$ MeV $\Gamma_R/\Gamma=1.00$	-139.1 ± 3.6 -135 ± 6	-257.6 ± 4.6 -250 ± 8
$\Delta(1700)D_{33}$	$W_R=1695$ MeV $\Gamma=376$ MeV $\Gamma_R/\Gamma=0.16$	125.4 ± 3.0 104 ± 15	105.0 ± 3.2 85 ± 22
$\Delta(1905)F_{35}$	$W_R=1858$ MeV $\Gamma=321$ MeV $\Gamma_R/\Gamma=0.12$	21.3 ± 3.6 26 ± 11	-45.6 ± 4.7 -45 ± 20

M. Dugger *et al.* [CLAS Collaboration], PRC **76**, 025211 (2007)

Photoproduction of π^0 Mesons off the Proton

- Strong excitation of $N(1720)P_{13}$ consistent with analysis of $\pi^+\pi^-$ electro-couplings
- No new nucleon resonances needed!

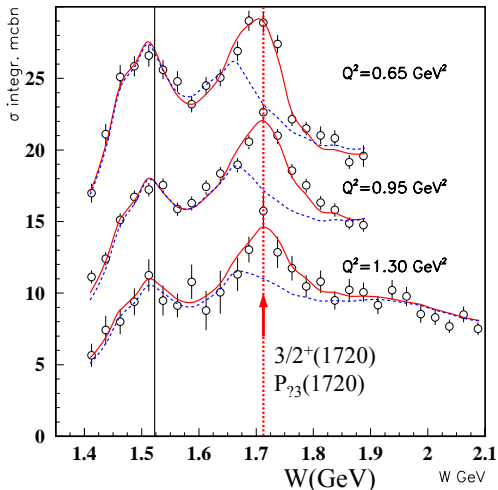
● CLAS ○ CB-ELSA · · · · · SAID SM02



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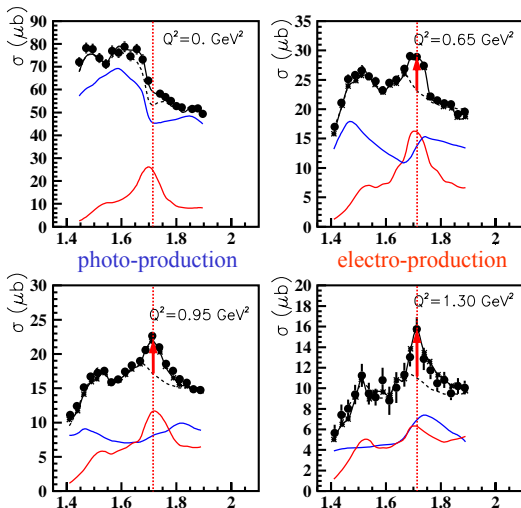
Resonances in $\gamma^{(*)}p \rightarrow p\pi^+\pi^-$



- 2π channel sensitive to N^* 's heavier than 1.4 GeV
- Provides complementary information to the 1π channel
- Many higher lying N^* 's decay preferably to $N\pi\pi$ final states via intermediate states

Solid curves are from fits using the recent JM06 model with and without a new $?(1720)P_{73}$ state

Resonances in $\gamma^{(*)}p \rightarrow p\pi^+\pi^-$



- Background
- Resonances

Combined analysis of preliminary real (M. Bellis) and also published virtual photon data (M. Ripani):

Fit needs both the candidate $?(1720)P_{73}$ and the $N(1720)P_{13}$ state.

Authors claim that combined fit of various single differential cross sections allowed to establish all significant mechanisms.

Reasonable Description of $N\pi/N\pi\pi$ Electroproduction

The CLAS-Collaboration phenomenological models (UIM/DR/JM) reproduce reasonably well comprehensive CLAS/world data on all observables in $N\pi/N\pi\pi$ electroproduction:

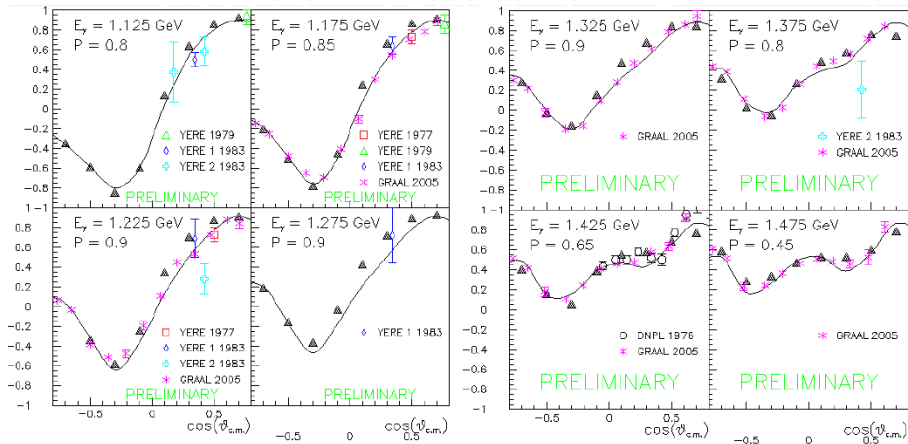
- Isobars used in $N\pi\pi$ electroproduction

- 1 All well-established $N^* \rightarrow \pi^- \Delta^{++}$ decays + $3/2^+(1720)$
- 2 All well-established $N^* \rightarrow \rho\pi$ decays + $3/2^+(1720)$
- 3 Observed for the first time in CLAS data:
 $\pi^+ D_{13}^0(1520)$, $\pi^+ F_{15}^0(1685)$, and $\pi^- P_{33}^{++}(1640)$

- Models can be used to evaluate N^* electrocouplings

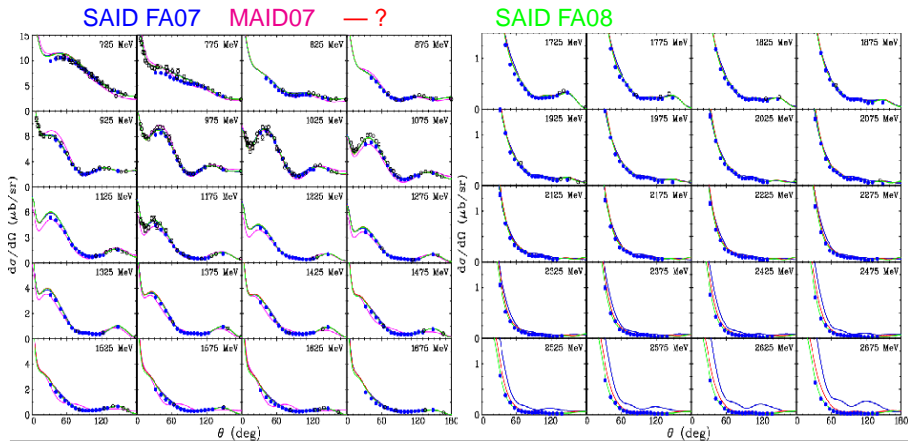
- Information on contributing mechanisms will be used by EBAC for N^* studies in advanced coupled channel analysis (Julia-Diaz, Lee, Phys. Rev. C76, 065201 (2007))

Photoproduction of π^0 Mesons: Beam Asymmetry Σ



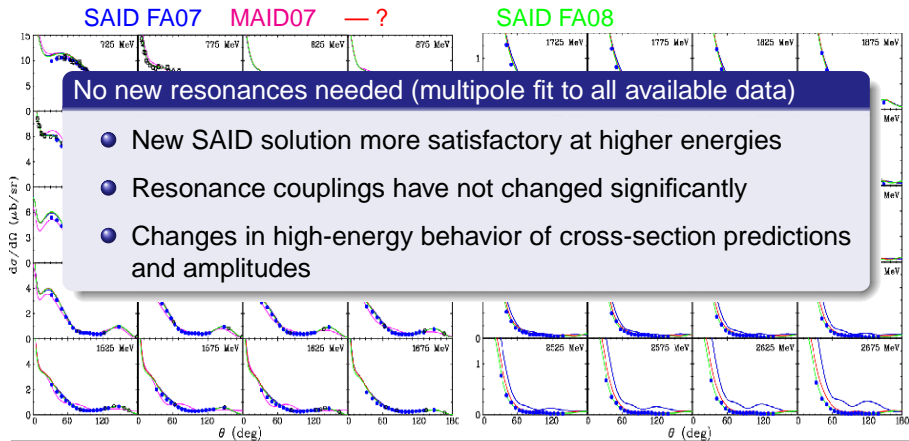
M. Dugger, CLAS g8b run group, to be published (▲)

Photoproduction of π^+ Mesons: $\gamma p \rightarrow n \pi^+$

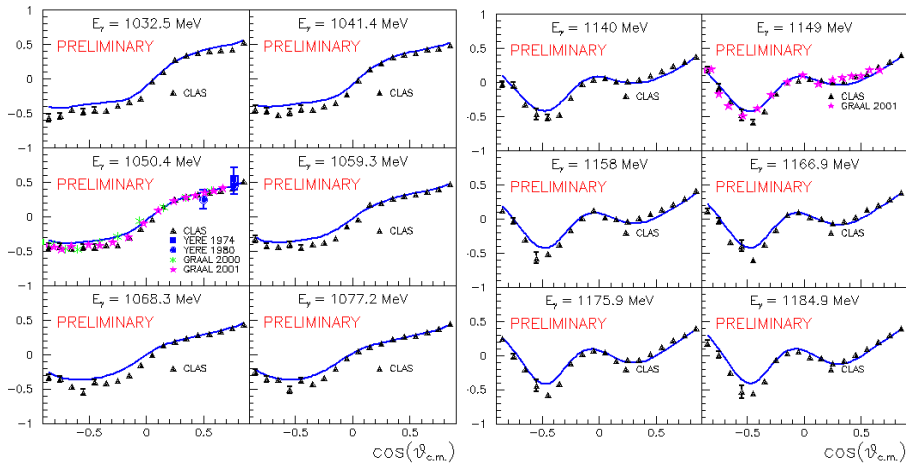


M. Dugger *et al.* (CLAS g1c), PRC **76**, 065206 (2009)

Photoproduction of π^+ Mesons: $\gamma p \rightarrow n \pi^+$



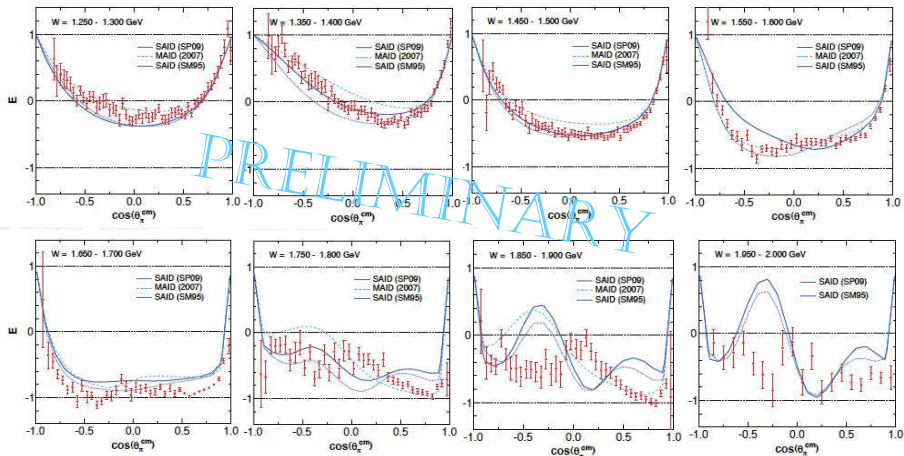
Photoproduction of π^+ Mesons: Σ in $\gamma p \rightarrow n \pi^+$



CLAS g8b run group, ASU analysis, to be published (▲)

Photoproduction of π^+ Mesons: Helicity Difference E

circ.-pol. beam on long.-pol. target: good agreement with SAID & MAID for $W < 1.7$ GeV



CLAS g9a (FROST) run group, USC analysis

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Beam-Target Polarization Observables

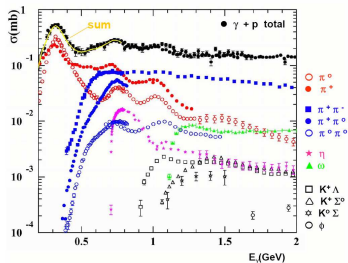
$$\frac{d\sigma}{d\Omega} = \sigma_0 \{ 1 - \delta_I \Sigma \cos 2\phi$$

$$+ \Lambda_x (-\delta_I \mathbf{H} \sin 2\phi + \delta_\odot \mathbf{F})$$

$$- \Lambda_y (-\mathbf{T} + \delta_I \mathbf{P} \cos 2\phi)$$

$$- \Lambda_z (-\delta_I \mathbf{G} \sin 2\phi + \delta_\odot \mathbf{E}) \}$$

← Single-Meson
 Final States
 (7 Observables)



Beam-Target Polarization Observables

$$\frac{d\sigma}{d\Omega} = \sigma_0 \{ 1 - \delta_I \Sigma \cos 2\phi$$

$$+ \Lambda_x (-\delta_I \mathbf{H} \sin 2\phi + \delta_{\odot} \mathbf{F})$$

$$- \Lambda_y (-\mathbf{T} + \delta_I \mathbf{P} \cos 2\phi)$$

$$- \Lambda_z (-\delta_I \mathbf{G} \sin 2\phi + \delta_{\odot} \mathbf{E}) \}$$

⇐ Single-Meson
 Final States
 (7 Observables)

Two-Meson Final States ⇒
 (15 Observables)

$$I = I_0 \{ (1 + \vec{\Lambda}_i \cdot \vec{\mathbf{P}})$$

$$+ \delta_{\odot} (\mathbf{I}^{\odot} + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}^{\odot})$$

$$+ \delta_I [\sin 2\beta (\mathbf{I}^s + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}^s)$$

$$\cos 2\beta (\mathbf{I}^c + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}^c)] \}$$

Photoproduction of $\pi^+ \pi^-$ off the Proton: Kinematics

Two mesons in the final state require 5 independent variables!

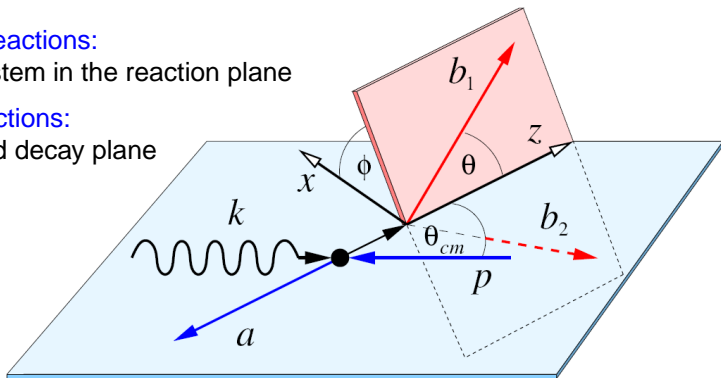
For example: E_γ , $\Theta_{\text{c.m.}}$, ϕ^* , θ^* , $M_{p+\text{meson}_1}$

Single-meson reactions:

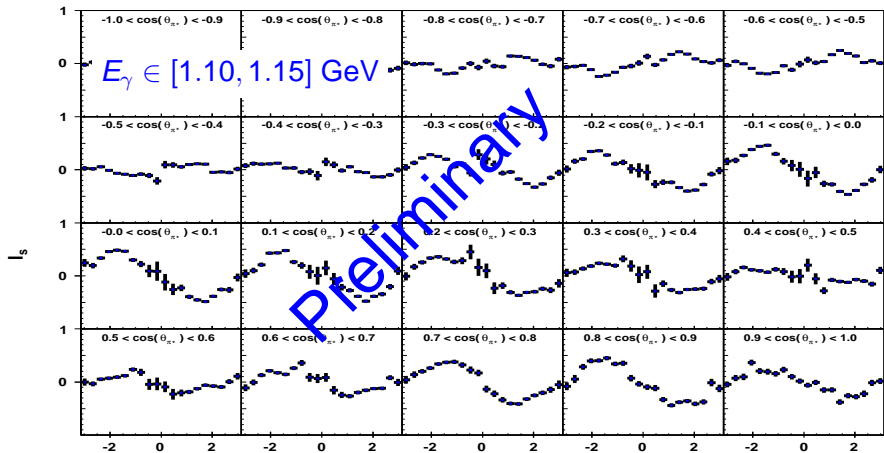
→ p -meson system in the reaction plane

Two-meson reactions:

→ Reaction and decay plane
 form angle ϕ



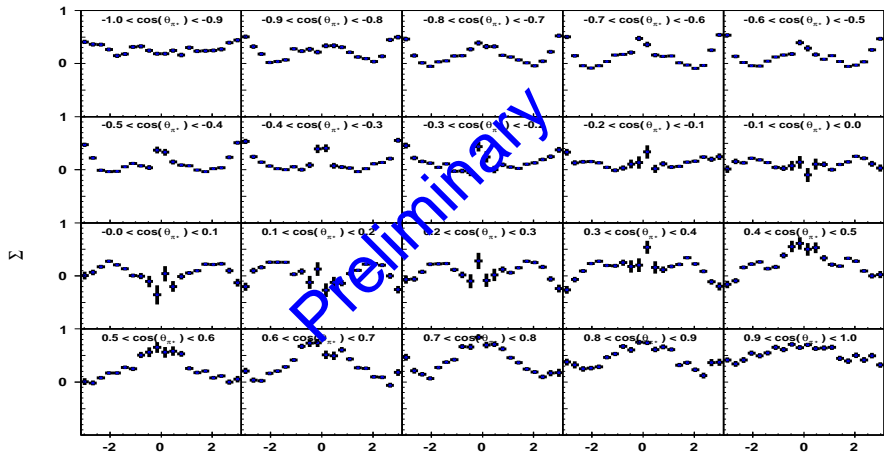
Photoproduction of $\pi^+ \pi^-$: Beam Asymmetry I_s (new)



C. Hanretty (FSU), CLAS g8b run group, to be published



Photoproduction of $\pi^+ \pi^-$: Beam Asymmetry $I_c (= \Sigma)$

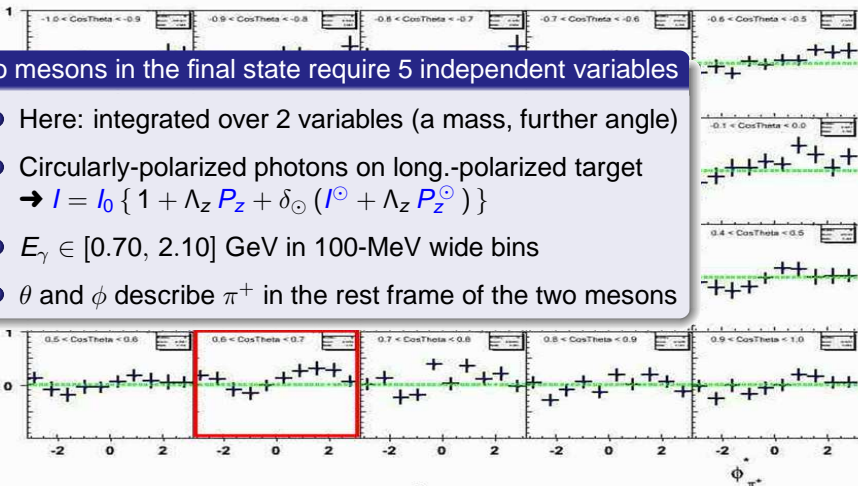


C. Hanretty (FSU), CLAS g8b run group, to be published

Photoproduction of $\pi^+ \pi^-$: Helicity Difference $P_z^\odot (= E)$

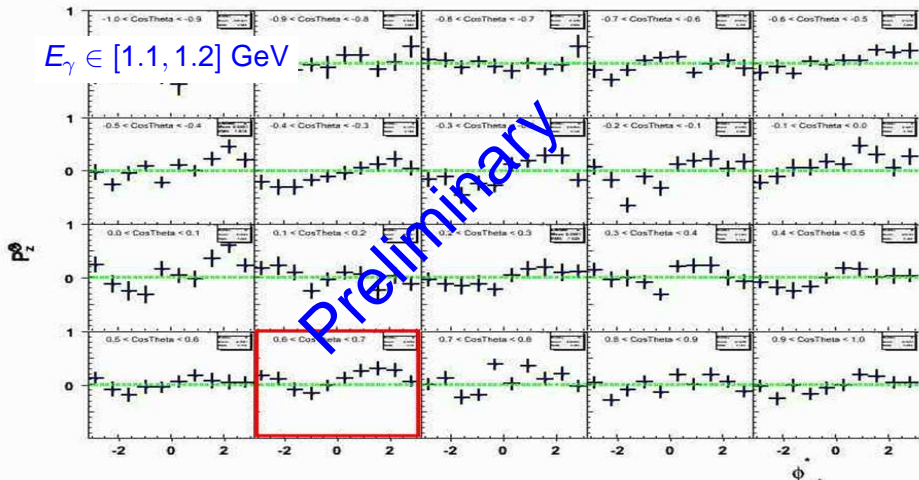
Two mesons in the final state require 5 independent variables

- Here: integrated over 2 variables (a mass, further angle)
- Circularly-polarized photons on long.-polarized target
 $\rightarrow I = I_0 \{ 1 + \Lambda_z P_z + \delta_\odot (I^\odot + \Lambda_z P_z^\odot) \}$
- $E_\gamma \in [0.70, 2.10]$ GeV in 100-MeV wide bins
- θ and ϕ describe π^+ in the rest frame of the two mesons



Photoproduction of $\pi^+ \pi^-$: Helicity Difference $P_z^\ominus (= E)$

$E_\gamma \in [1.1, 1.2]$ GeV



S. Park (FSU), CLAS g9a (FROST) run group

Outline

- 1 Introduction
 - Toward Complete Experiments
- 2 Experimental Setup: The CLAS Detector at Jefferson Lab
- 3 Photoproduction of a Single (Pseudoscalar) Meson
 - η Photoproduction (off the Proton)
 - π Photoproduction
- 4 Double-Meson Photoproduction
 - $\pi^+ \pi^-$ Photoproduction
- 5 Summary and Outlook

Summary and Outlook

Search for new excited baryon states in full swing:

- Precise cross-section measurements in several channels in nearly full phase space ($N\pi$, $N\eta$, $N\eta'$, $N\omega$, $K\Lambda$, $K\Sigma$, etc.)
- Precise photon beam asymmetries on proton and neutron targets (g8b & g13 run groups)
- Strong coupling of $N\omega$ to $N(1700)D_{13}$, $N(1680)F_{15}$, $N(2190)G_{17}$
→ Hints for Capstick/Roberts $N(2000)F_{15}$ decaying into $N\omega$
- Double polarization observables with linear/circular photons and recoil hyperon polarization → $N(1900)P_{13}$
- First data on polarized proton targets with circularly and linearly polarized beam (FROST)

(New) Baryon Resonances (e.g. Bonn-Gatchina PWA)

Reaction	Resonances			
$\gamma p \rightarrow N\pi$	$\Delta(1232)P_{33}$	$N(1520)D_{13}$	$N(1680)F_{15}$	$N(1535)S_{11}$
$\gamma p \rightarrow p\eta$	$N(1535)S_{11}$	$N(1720)P_{13}$	$N(2070)D_{15}$	$N(1650)S_{11}$
$\gamma p \rightarrow p\pi^0\pi^0$	$\Delta(1700)D_{33}$	$N(1520)D_{13}$	$N(1680)F_{15}$	
$\gamma p \rightarrow p\pi^0\eta$	$\Delta(1940)D_{33}$	$\Delta(1920)P_{33}$	$N(2200)P_{13}$	$\Delta(1700)D_{33}$
$\gamma p \rightarrow \Lambda K^+$	$S_{11} - \text{wave}$	$N(1720)P_{13}$	$N(1900)P_{13}$	$N(1840)P_{11}$
$\gamma p \rightarrow \Sigma K$	$S_{11} - \text{wave}$	$N(1900)P_{13}$	$N(1840)P_{11}$	
$\pi^- p \rightarrow n\pi^0\pi^0$	$N(1440)P_{11}$	$N(1520)D_{13}$	$S_{11} - \text{wave}$	

The available data sets comprising various high-statistics differential cross sections, beam, target, recoil asymmetries, double polarization observables, and also data resolving isospin contributions are not yet sufficient to converge into a unique solution.