

*Scaling phenomenology of meson photoproduction in
new CLAS G11A results from CMU*

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OUTLINE

- 1 INTRODUCTION AND OVERVIEW
- 2 SCALING: REGGE
- 3 SCALING: FIXED-ANGLE
- 4 PWA: INTERPOLATING TRAJECTORIES
- 5 SUMMARY

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INTRODUCTION

- CLAS **G11A** experiment – unpolarized photoproduction on ℓH_2 target, two-prong trigger, mostly runs with electron beam energy 4.019 GeV.
- Missing baryon resonance problem – look at **non- $N\pi$ channels**.
- CMU is analysing several of these channels – $p\omega$ (M. Williams), $p\eta$, $p\eta'$ (M. Williams, Zeb Krahn), including strangeness production – $K^+\Lambda$ (M. McCracken), $K^+\Sigma^0$ (B. Dey).
- Differential cross sections and polarizations – \sqrt{s} from threshold till ~ 2.85 GeV in 10 MeV wide bins. Wide angular coverage – $-0.95 \leq \cos \theta_{CM}^{meson} \leq 0.95$
- $p\omega$ PWA already done and nearing publication. PWA on other channels is in progress. Final goal – do a coupled channel analysis!
- Status of **my $K^+\Sigma^0$ analysis** – $d\sigma/dt$ and P_Σ measurements are in collaboration Analysis Review review stage.
- I've shown these measurement results in previous talks, so, I'll focus on some of the new *physics* results that are beginning to emerge.

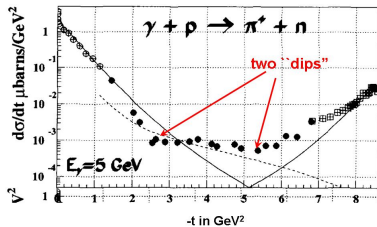
UNIVERSALITY IN HIGH \sqrt{s} BEHAVIOR

$$\gamma p \rightarrow K^+ \Sigma^0$$

- Recap: at the June Users' Group meeting, I showed that for $\gamma p \rightarrow K^+ \Sigma^0$, $d\sigma/dt$ -vs- t shows a “dip” structure above $\sqrt{s} \approx 2.2$ GeV.
- Furthermore, at even higher energies, the “dip” separates into two separate “dips”.

UNIVERSALITY IN HIGH \sqrt{s} BEHAVIOR

- Similar behavior can be seen in the other pseudoscalar mesons too (in varying degrees/kinematics).



SLAC data

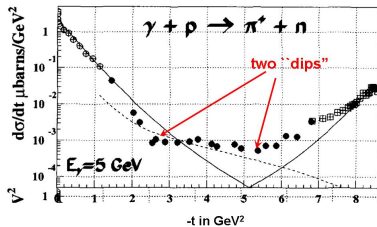
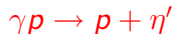
Anderson *et al*, PRD 14 (1976) 649

(plot: Guidal *et al*, Nucl. Phys. A 627 (1997) 645-678)

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UNIVERSALITY IN HIGH \sqrt{s} BEHAVIOR

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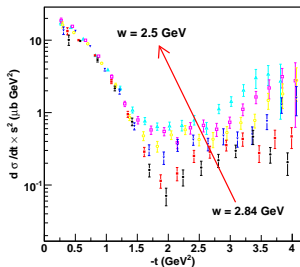
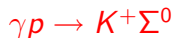
- Away from the resonance region, there seems to be a **universality** in the features for exclusive $\gamma p \rightarrow PS + B$ (PS = π, K, η, η' ; B = baryon)

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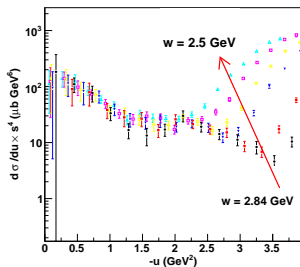
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SCALING PART I: REGGE REGION

- Let's start by looking at large \sqrt{s} , $|t| \rightarrow 0$ (forward-angle) and $|u| \rightarrow 0$ (backward-angle). This's the "Regge region".
- **Regge** scaling: $d\sigma/dx \sim s^{2\alpha(x)-2}$, where $x = u, t$ and $\alpha(x) = \alpha_0 + \alpha_1 x$ is the Regge trajectory for the particular exchange.
- Note: most previous high energy world data at are at $|t| \rightarrow 0$. *The new CLAS results are unique in having a wide angular coverage.*
- We want to cover all three regions: forward-, mid- and backward-angles. This's important because we want to tie them all together finally.

REGGE SCALING: BOTH u AND t CHANNELS

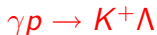
$|t| \rightarrow 0 \sim s^2$ scaling



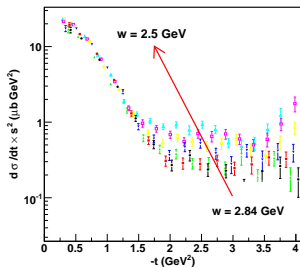
$|u| \rightarrow 0 \sim s^4$ scaling

- Scaling powers different because exchange trajectories are different.
- Note: with multiple trajectories (at the amplitude level), expect only an “effective” scaling power for the differential cross-sections.

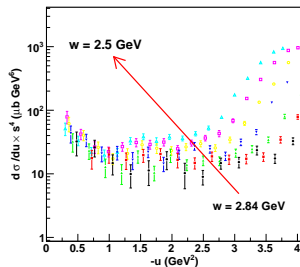
REGGE SCALING: MORE EXAMPLES



(from Mike McCracken's CMU thesis)



$|t| \rightarrow 0 \sim s^2$ scaling



$|u| \rightarrow 0 \sim s^4$ scaling

- Note: we don't *quite* go to the $|t| \rightarrow 0$ or $|u| \rightarrow 0$ limits (the extreme forward/backward angles).
- The *onset* of the Regge behavior is also channel dependent.

REGGE SCALING: THE “POWERS”

- Guidal *et al* and later, Bradford and co-workers noted that for the hyperons, if the exchanges trajectories are K^+ and $K^*(892)$, then $\alpha(t)_{K^+} + \alpha(t)_{K^*(892)} \sim 0$ near $t \sim 0$.
- If $\alpha_{eff} \sim 0$ then the scaling power $-2(\alpha - 1) \sim 2$. This could explain the power law behavior.
- For the u -channel case, the exchanges are Λ/Σ . What are the Regge trajectories?

$$\alpha(u)_{\Lambda} \sim -0.6 + 0.9u$$

$$\alpha(u)_{\Sigma} \sim -0.8 + 0.9u$$

- u -channel: $t \rightarrow u$, physical region: $u < 0$
- At $|u| \rightarrow 0$:

$$(2\alpha - 2)_{\Lambda} \approx -3.2$$

$$(2\alpha - 2)_{\Sigma} \approx -3.6$$

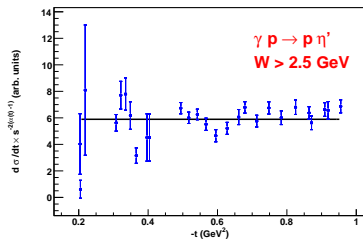
- It is thus *conceivable* that the scaling power $-(2\alpha - 2)$ be > 2 .

REGGE SCALING: ONE LAST EXAMPLE



(Zeb Krahn's CMU thesis)

- t -channel Regge exchanges are the ω/ρ trajectories: $\alpha(t)_{\omega/\rho} \approx 0.5 + 0.9t$.
- Plot $\frac{d\sigma}{dt} \times s^{-2(\alpha(t)-1)}$ keeping the full t dependence. Include only points with $\sqrt{s} > 2.5$ GeV and $|t| \leq 1$ GeV²



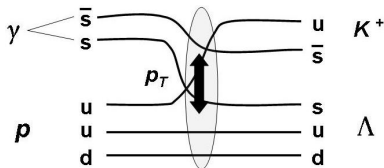
- After scaling, the differential cross-sections approximately line up.

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SCALING PART II: FIXED-ANGLE REGION

- Look at large s and large $-t$ or $-u$, with constant t/s or u/s .
- In the high energy limit, $t/s \sim (1 - \cos \theta)$, so $\cos \theta \approx$ **fixed**. Take $\theta \sim 90^\circ$.
- Simplified picture: transfer momentum $p_T \sim \sqrt{|t|}$ sets the time scale: $\tau \sim 1/p_T$.



- **Large p_T** means constituents have very little time to interact. Hard scattering at the parton level (**fixed-angle** region)
- **Small p_T** means constituents have time to form intermediate bound states. Regge poles are exchanged (**Regge** region)
- Intermediate region? – interpolating trajectories.

FIXED-ANGLE SCALING LAWS

- Brodsky and Farrar (PRL 31 (1973), 1153): for exclusive scattering at $s \rightarrow \infty$, t/s fixed,

$$(d\sigma/dt)_{AB \rightarrow CD} \sim s^{2-n} f(t/s)$$

- n is the total number of elementary fields participating in the hard scattering process.
- Note: a photon counts a single parton. However if it participates as VMD-like $\gamma \rightarrow q\bar{q}$, then it counts as 2 partons.
- So the prediction is: $d\sigma/dt_{\gamma p \rightarrow \pi p} \sim s^{-7}$. The same law should apply to the other pseudoscalar mesons ηp , $\eta' p$, $K^+ \Lambda$, $K^+ \Sigma^0$, and even the vector meson ωp .
- Again, under the VMD picture this should change to s^{-8} . *So in general, something between -7 and -8 is predicted.*

PREVIOUS EXPERIMENTS

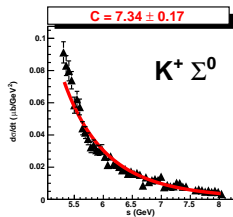
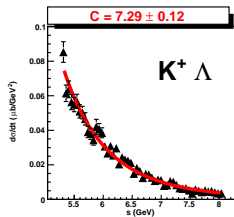
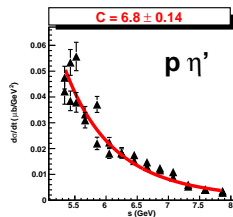
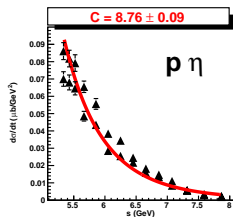
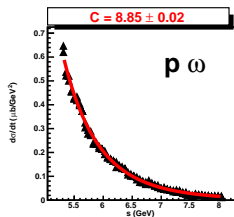
- **BNL** experiment **Comparison of 20 exclusive reactions at large t** , White *et al*, PRD 49 (1994), 58

| No. | Interaction | Cross section | | $n-2$ ($\frac{d\sigma}{dt} \sim 1/s^{n-2}$) |
|-----|--------------------------------------|---------------|---------------|--|
| | | E838 | E755 | |
| 1 | $\pi^+ p \rightarrow p\pi^+$ | 132 ± 10 | 4.6 ± 0.3 | 6.7 ± 0.2 |
| 2 | $\pi^- p \rightarrow p\pi^-$ | 73 ± 5 | 1.7 ± 0.2 | 7.5 ± 0.3 |
| 3 | $K^+ p \rightarrow pK^+$ | 219 ± 30 | 3.4 ± 1.4 | $8.3^{+0.6}_{-1.0}$ |
| 4 | $K^- p \rightarrow pK^-$ | 18 ± 6 | 0.9 ± 0.9 | ≥ 3.9 |
| 5 | $\pi^+ p \rightarrow p\rho^+$ | 214 ± 30 | 3.4 ± 0.7 | 8.3 ± 0.5 |
| 6 | $\pi^- p \rightarrow p\rho^-$ | 99 ± 13 | 1.3 ± 0.6 | 8.7 ± 1.0 |
| 13 | $\pi^+ p \rightarrow \pi^+ \Delta^+$ | 45 ± 10 | 2.0 ± 0.6 | 6.2 ± 0.8 |
| 15 | $\pi^- p \rightarrow \pi^- \Delta^-$ | 24 ± 5 | ≤ 0.12 | ≥ 10.1 |
| 17 | $pp \rightarrow pp$ | 3300 ± 40 | 48 ± 5 | 9.1 ± 0.2 |
| 18 | $p\bar{p} \rightarrow p\bar{p}$ | 75 ± 8 | ≤ 2.1 | ≥ 7.5 |

More or less good agreement with theory.

- **CLAS** experiment: ω photoproduction at large p_T , Battaglieri, PRL 90 (2003), 022002. Found power law behavior s^{-C} with $C \approx 7.2 \pm 0.8$

NEW CLAS G11A RESULTS

Fixed angle scaling: $\theta = 90^\circ$ Fit fn: $f(s) = A s^{-C}$

CLAS g11a data

- Note the high precision for $p\omega$!
- Interesting that the Λ and Σ^0 results look similar and very close to the predicted s^{-7} .

NEW CLAS G11A RESULTS: FEATURES

- It is interesting that fixed-angle scaling is visible in the new CLAS data for all the mesons, and lies around the predicted scaling behavior.
- The $p\eta$ and $p\eta'$ cases are limited by statistics, but still “point towards” a scaling behavior.
- For hard scattering, it seems that $K^+\Lambda$ and $K^+\Sigma^0$ behaves very similarly and well within the scaling-law prediction. Does the singlet/triplet structure of the (ud) diquark not matter here?
- Excellent statistics for $p\omega$ and the fit looks very good. The experimental power law approaches s^{-9} however, which's different from the prediction. So why is the vector meson different?

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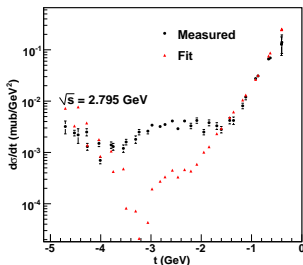
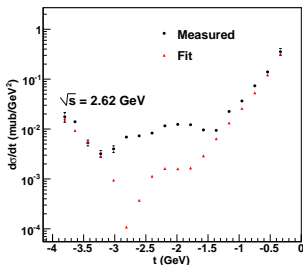
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PWA FITS

- “Scaling region” is high s ($\sqrt{s} > 2.5$ GeV). But, our main goal is to look for missing resonances (lower \sqrt{s}).
- However, to fix the “background processes” (non-resonant u - and t -channel exchanges), we look at the high \sqrt{s} region where there’s presumably very little resonance contribution.
- **Regge based approach** has been quite successful to explain the high energy data.
- Chief attraction: **simplicity** and **few parameters** (no form-factors are involved).
- Theoretical difficulties: replaces the Feynman propagators by a Regge propagator computed at the “first materialization” m_1 .
- Assumption: m_1^2 not “too far” from the *physical region* ($u, t < 0$). Okay for $m_{K^+}^2 \approx 0.25$, but a stretch for $m_{\rho}^2, m_{\lambda}^2 \approx 1$ (u -channel exchanges).

$p\eta'$ FITS

- Trial fit run over $2.6 \text{ GeV} \leq \sqrt{s} \leq 2.84 \text{ GeV}$.
- “Reggized” ρ (t -channel) + ρ (u -channel) trajectories – “rotating” or “constant” phase. Used “rotating” versions here (arbitrary choice).
- A scale factor for each trajectory – 2 fit parameters (note simplicity!). 10 iterations per fit.



- Forward and backward angles are being fit quite well.
- Obviously, mid-angle regions are not being described very well.

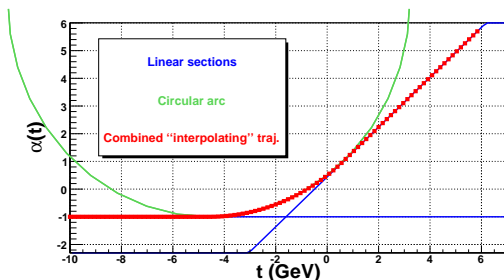
SATURATED REGGE TRAJECTORIES

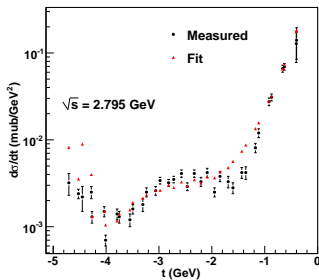
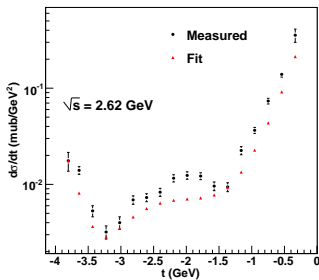
- We have seen earlier that the **Regge** region and **fixed-angle** region consists of very **different physics**. The only seeming connection is that both shows scaling, but scaling of completely different natures.
- Conventional Regge trajectories are linear while hard scattering scaling has a constant/flat exponent. In Regge language, the trajectories seem to get “saturated off” for large negative t or u .
- Following is from Brodsky *et al*, PRD 8 (1973), 4117:
 - $u, -t, s$ all large with u/s and t/s fixed
 - $\mathcal{A}_{AB \rightarrow CD} \sim s F_A(-s) F_C(u) F_D(t) \sim s^{1-A} (-u)^{-C} (-t)^{-D}$
 - where the form-factors $F_M(x) \sim (-x)^{-M}$; $M = 1, 2$ for mesons and baryons resp. in *photoproduction*, $\mathcal{A} = \mathcal{A}_\mu k_T^\mu$ where $k_T \sim \sqrt{s}$. Propagator $\sim 1/t$, so $M = 1$.
- These reproduce the fixed-angle scaling laws. Next, cast them in the Regge form:
 - $\mathcal{A} \sim \beta(t) (-u)^{\alpha(t)}$ OR $\mathcal{A} \sim \beta(u) (-t)^{\alpha(u)}$
- Then, in the **Regge** form, the “**saturated**” trajectories for $\gamma p \rightarrow \text{PScalar} + \text{Baryon}$:

$$\alpha(u)_{-u \rightarrow \infty} = -2, \quad \alpha(t)_{-t \rightarrow \infty} = -1$$

INTERPOLATING TRAJECTORIES

- Join the **linear** and **flat saturated** parts smoothly by an *interpolating trajectory*.
- Theoretical (analytic) expression was given by Sergeenko (Z. Phys. C 64 (1994), 315), but only for quarkonia. Guidal *et al* used the formula for ρ trajectory in their $\pi^+ n$ analysis.
- Try the simple but adhoc construction: join the two limits by an **circular arc**. Make the linear parts to be tangents to this circle.
- Shown below for the ω case:



REFIT $p\eta'$ USING INTERPOLATING TRAJECTORIES

- Marked improvement!
- Works best at higher \sqrt{s} – just as expected.

REGGE FITS – OVERVIEW

- Overall, the Regge description seems like a very compact way of describing the data.
- Using interpolating trajectories, the high energy data can be fit quite well (*works for the other mesons as well*).
- The radius of the “arc” becomes as new fit variable now.
- Caveat: overcounting could occur from “duality”, if we use resonances *and* the Reggeized background contributions, at the *intermediate* energies. So one needs to be careful.

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SUMMARY AND WORK IN PROGRESS

- We have found some very interesting *universal features* for *exclusive pseudoscalar meson photoproduction*. Given that spin-parity-wise they are equivalent, it is probably not too unexpected.
- We confirm *fixed-angle scaling* in these reactions, as predicted by Brodsky and co-workers.
- Saturating the Regge trajectories in a manner dictated by the fixed-angle behavior, we were able to *fit the high energy data* over almost the *entire angular spectrum*.
- The saturated Regge fits need to be further tuned and finalized. Also, they have to be compared with Feynman pole fits (with form factors).
- Our final goal is to do perform a coupled channel PWA using the *K*-matrix formalism on all these channels, to look for missing baryon resonances.