



# Beam Asymmetry Measurements from g8b for $\gamma p \rightarrow p \pi^+ \pi^-$ : An Update

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For the CLAS Collaboration: 20Nov09



# Outline

- Motivation
- Kinematic Fitter
- Momentum Corrections
- Tagger Sag (Photon Energy Corrections)
- Preliminary Results
- Q-Values (Background Subtraction)

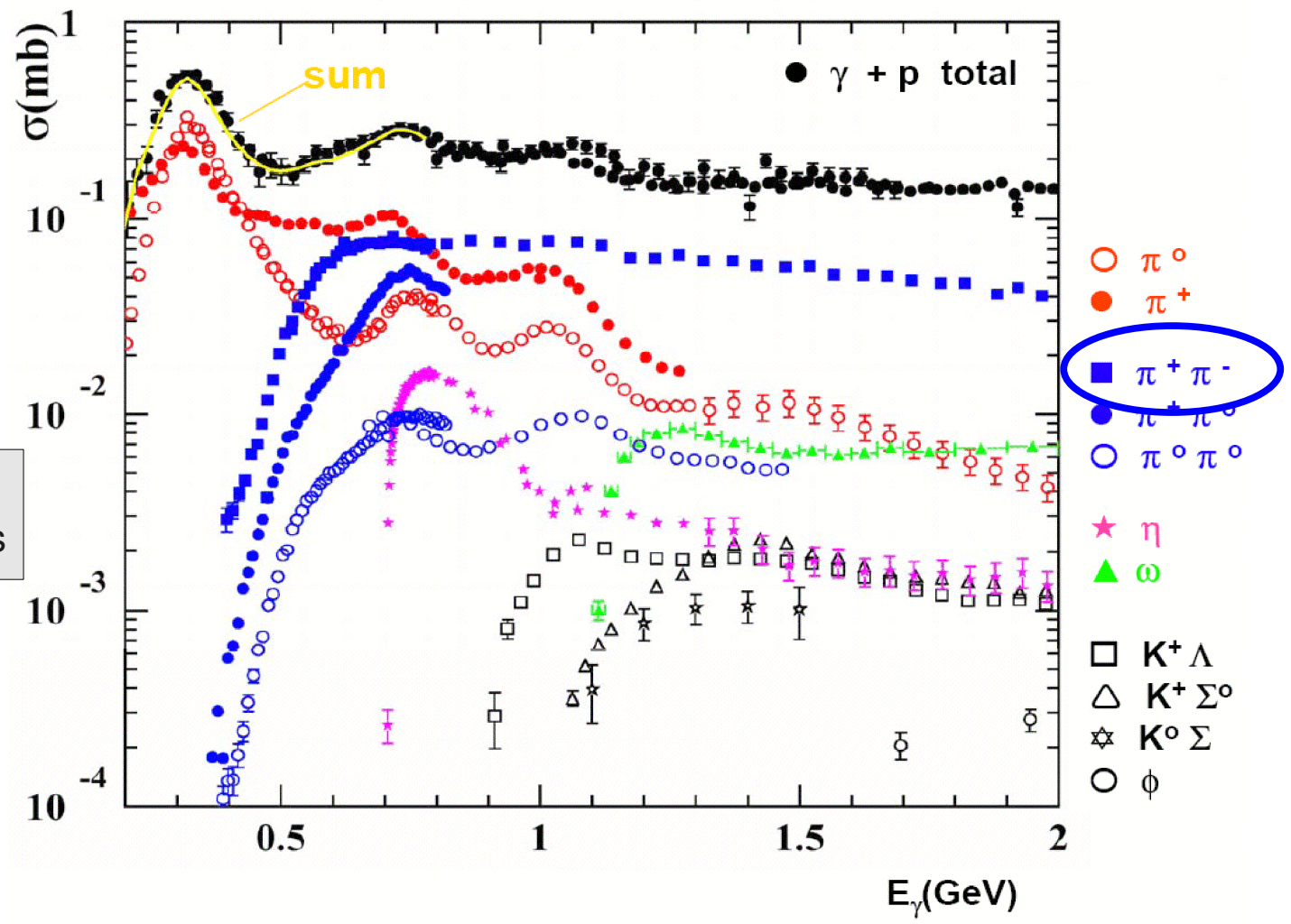








# $\gamma+p$ Cross Section



Experimental Cross Sections

- $\pi^+\pi^-$  cross section is large but devoid of structure.  $\rightarrow$  resonances are broad and overlapping.
- Cannot go “peak hunting”.
- Constraints provided by polarization are needed to disentangle and isolate resonance<sup>5</sup> contributions.

# Final State Equation

- To isolate resonance contributions we aim to measure polarization observables.
- The final state equation for two mesons in the final state has a total of 15 observables.

$$I = I_0 \{ (1 + \Lambda_i \cdot \mathbf{P}) + \delta_{\odot} (\mathbf{I}^{\odot} + \Lambda_i \cdot \mathbf{P}^{\odot}) + \delta_l [ \sin 2\beta (\mathbf{I}^s + \Lambda_i \cdot \mathbf{P}^s) + \cos 2\beta (\mathbf{I}^c + \Lambda_i \cdot \mathbf{P}^c) ] \}$$

$I_0$  = unpolarized reaction rate

$\Lambda_i$  = degree of polarization of target

$\delta_{\odot, l}$  = degree of polarization of photon beam

$\mathbf{P}$  = observables arising from target polarization

$\mathbf{I}^{\odot, s, c}$  = observables arising from use of polarized photons

$\beta$  = orientation of polarization w.r.t. a final state particle

- Through the use of experimental conditions/setup, we can reduce the number of observables making a measurement possible.

# Final State Equation : g8b

- Used linearly polarized photons incident on an unpolarized  $\text{LH}_2$  target.

$$I = I_0 \{ (1 + \Lambda_i \cdot \mathbf{P}) + \delta_{\odot} (\mathbf{I}^{\odot} + \Lambda_i \cdot \mathbf{P}^{\odot}) + \delta_l [ \sin 2\beta (\mathbf{I}^s + \Lambda_i \cdot \mathbf{P}^s) + \cos 2\beta (\mathbf{I}^c + \Lambda_i \cdot \mathbf{P}^c) ] \}$$

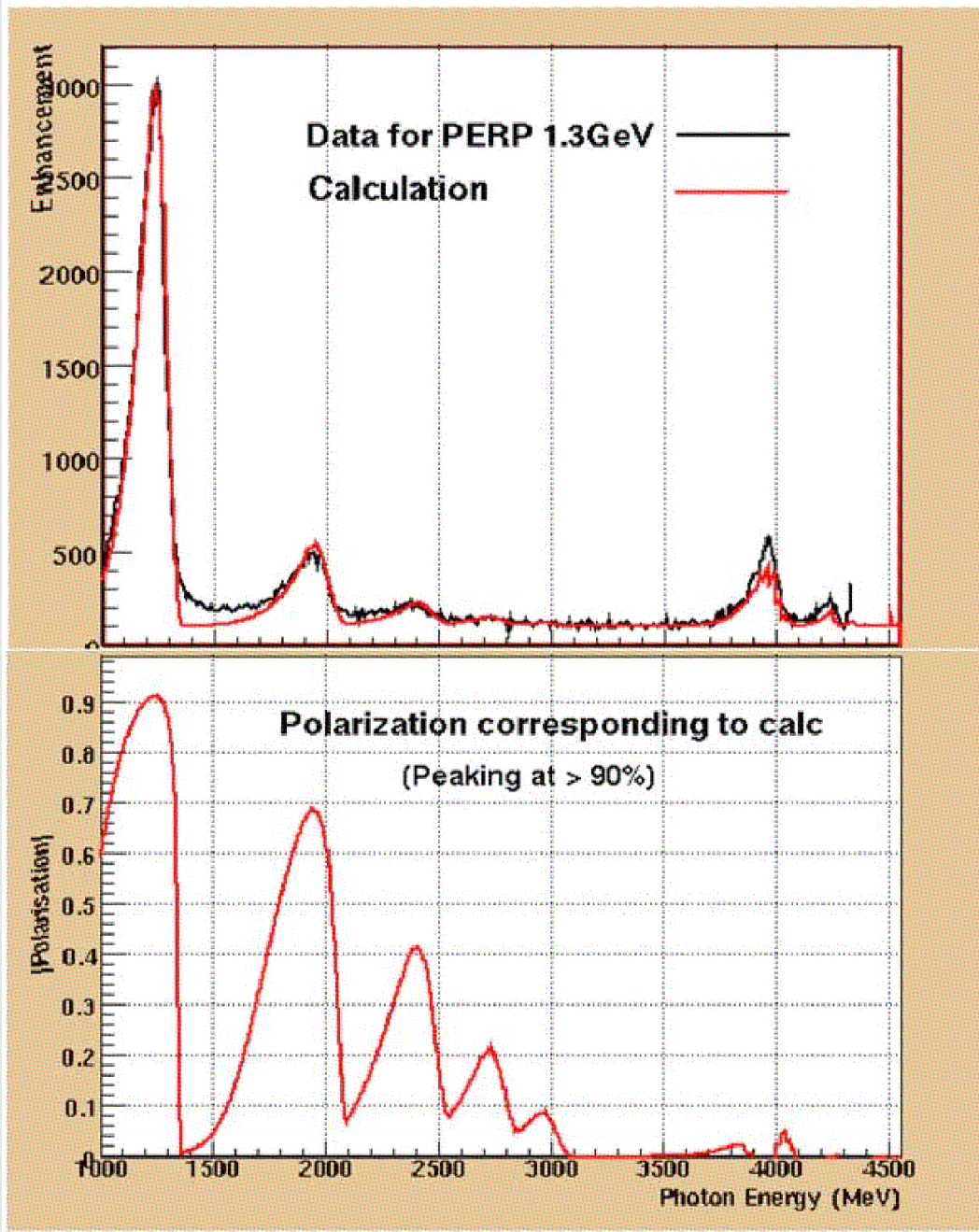


$$I = I_0 \{ 1 + \delta_l [ \mathbf{I}^s \sin 2\beta + \mathbf{I}^c \cos 2\beta ] \}$$

- $I^c$  (also known as  $\Sigma$  in the single-meson equation)
- $I^s$
- Measuring both for  $\gamma p \rightarrow p \pi^+ \pi^-$

# g8b : A reminder

- The g8b experiment ran from July 20 to Sep 1<sup>st</sup> 2005
- Used linearly polarized and tagged photons incident on unpolarized LH<sub>2</sub>.
- Obtained a degree of linear polarization of over 90%
- Polarized photon were produced at 5 different coherent edge energies : 1.3, 1.5, 1.7, 1.9, 2.1 GeV.







# g8b : A reminder

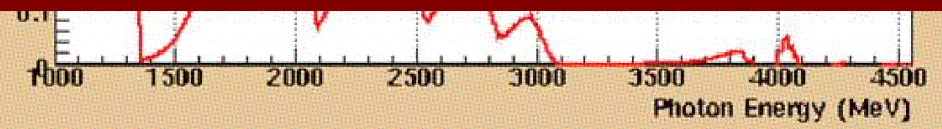
THE  
CATHOLIC UNIVERSITY  
*of* AMERICA



UNIVERSITY  
*of*  
GLASGOW

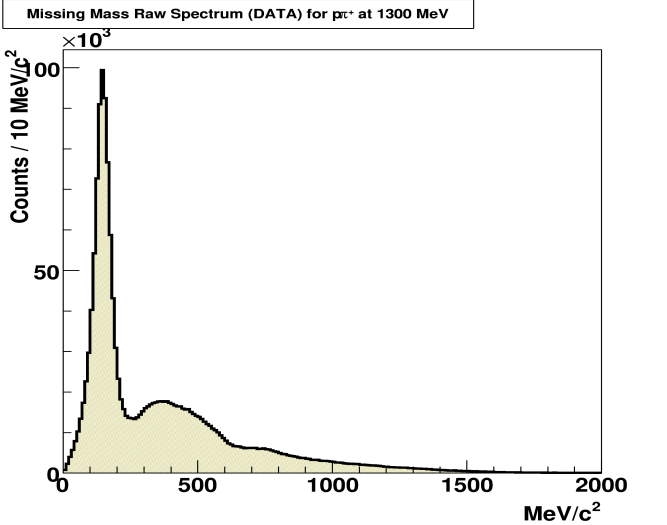
**ASU**  
ARIZONA STATE  
UNIVERSITY

 **Jefferson Lab**

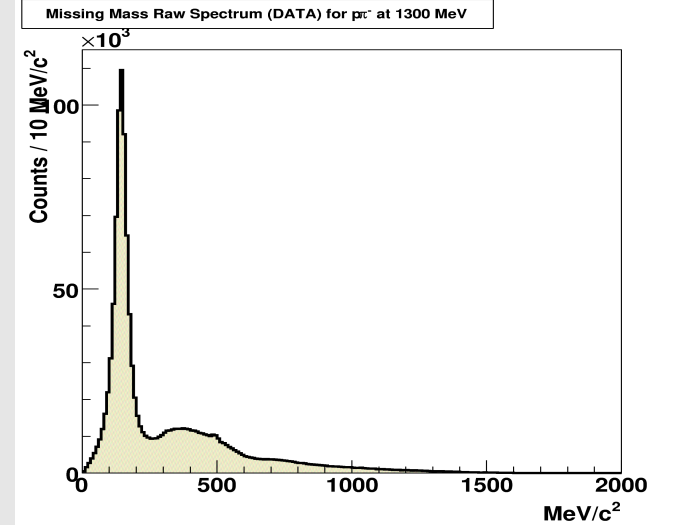


# The g8b Data Set

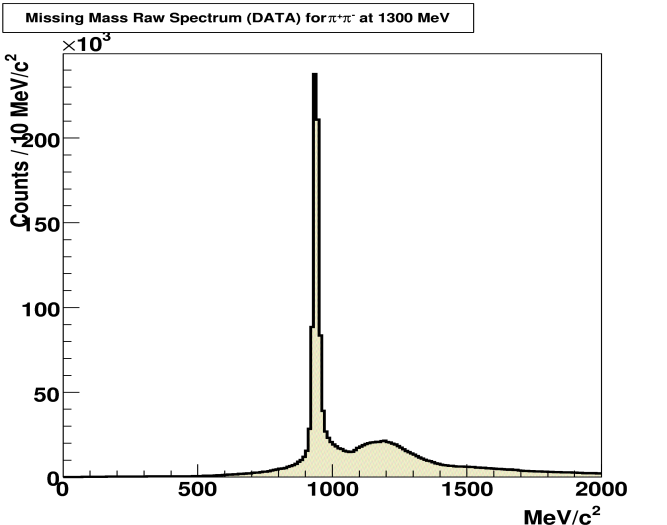
- $\gamma p \rightarrow p \pi^+ \pi^-$  from the g8b data set
- Kinematically fitting four topologies:



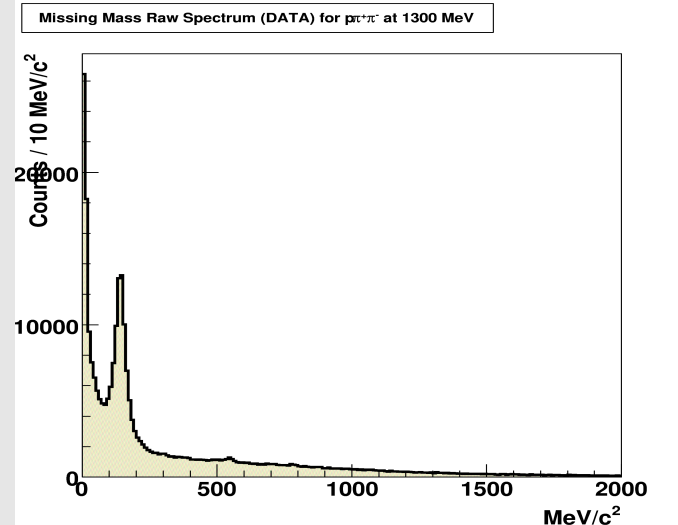
$p \pi^+ (\pi^-)$



$p \pi^- (\pi^+)$



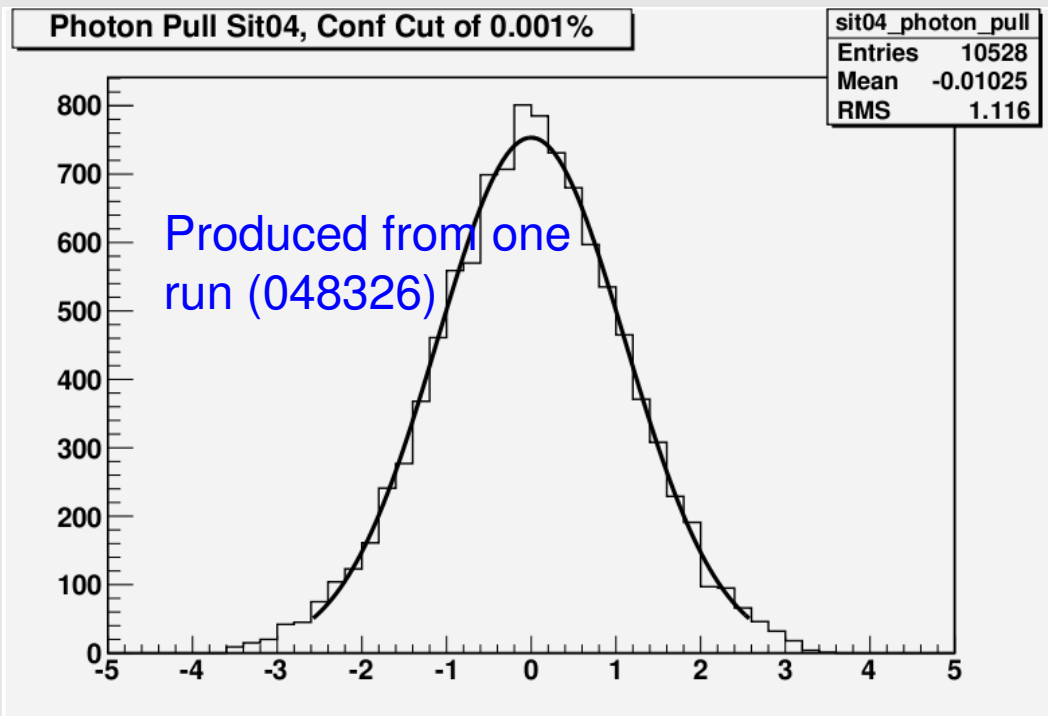
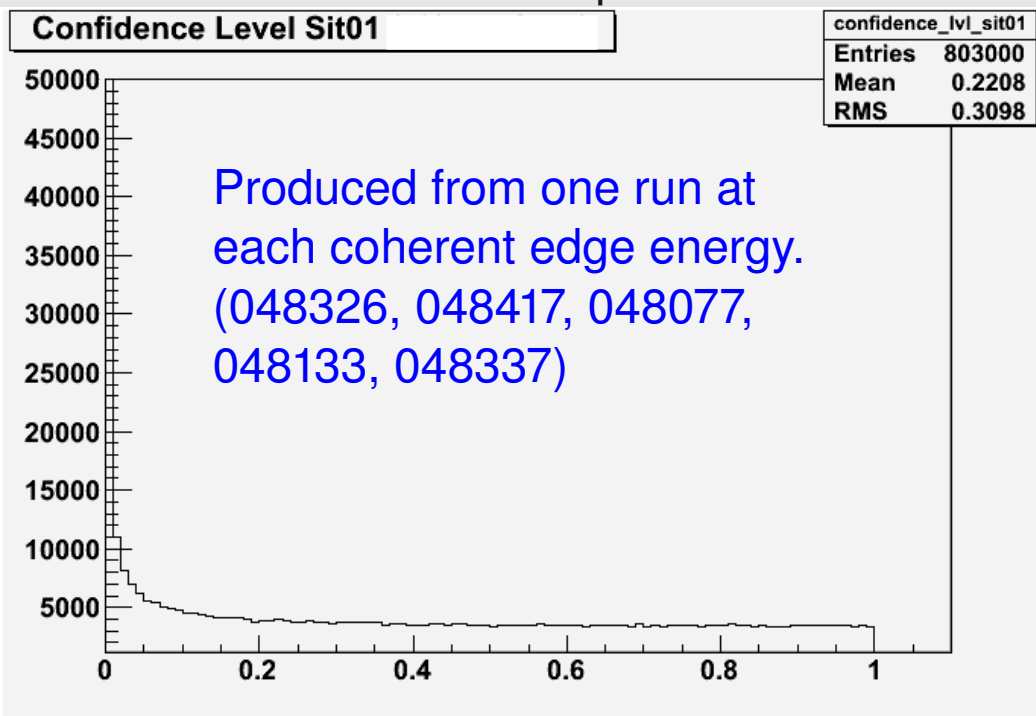
$\pi^+ \pi^- (p)$



$p \pi^+ \pi^- ( )$

# Kinematic Fitting of g8b Data

- Uses energy/momentum conservation and missing mass to vary final state measurements within the error of the measurements.
- Tracking measurements (from the TBER bank) are used to build the covariance matrix\*.
- Quality of a fit → pull distributions and confidence level.
- “Pure” parameters of the covariance matrix have pull distributions.
- Systematics affect pull means, covariance matrix errors affect pull widths and slope of confidence level plots.



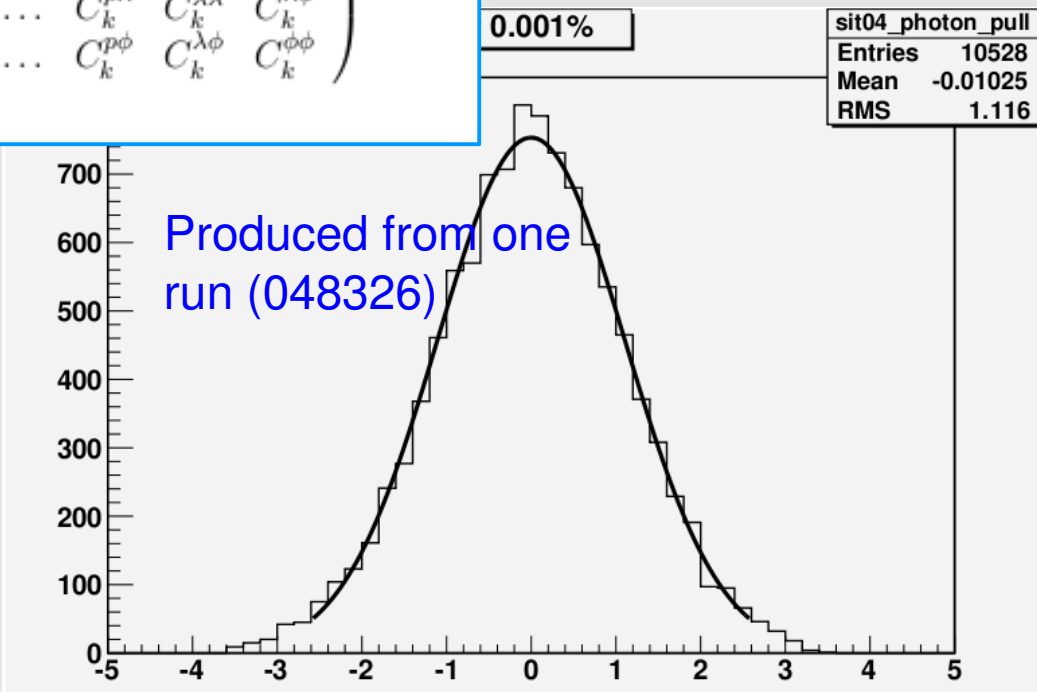
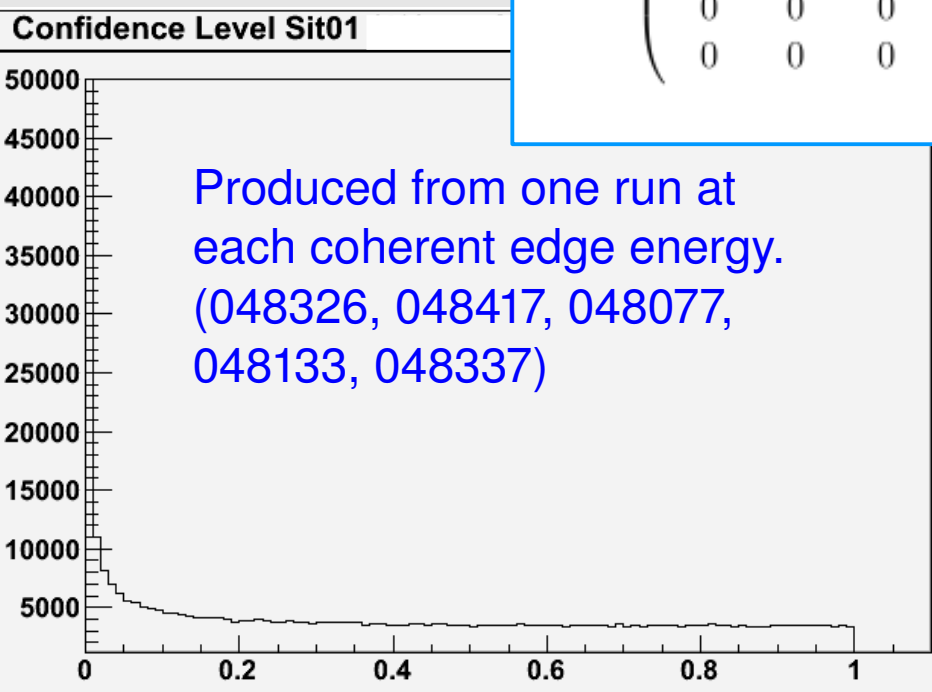


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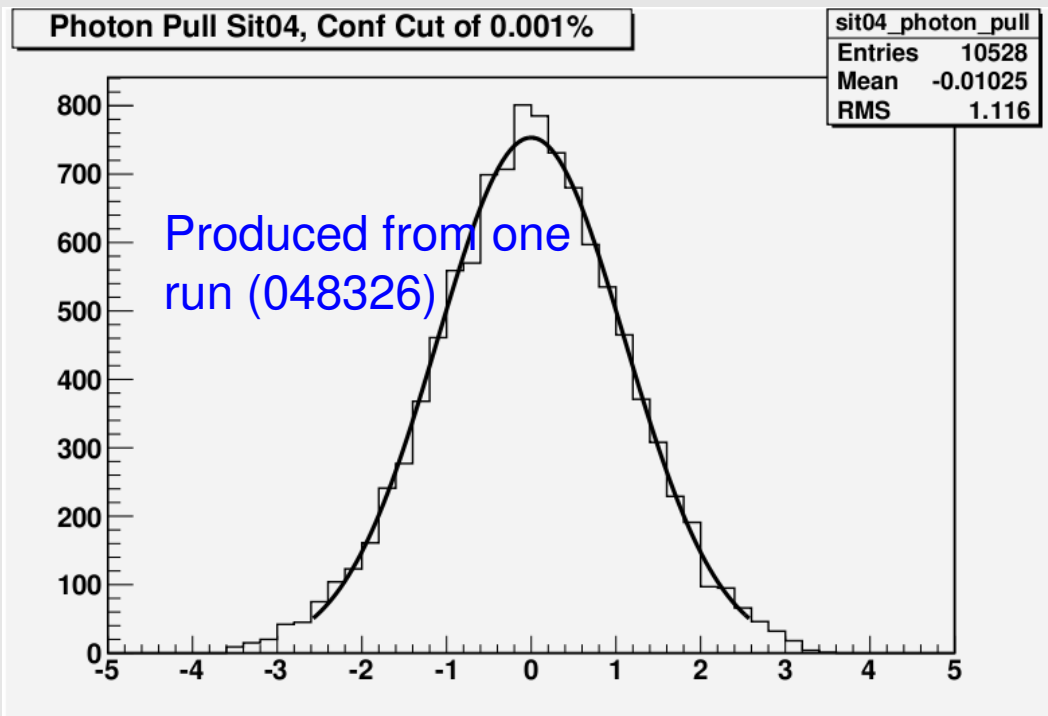
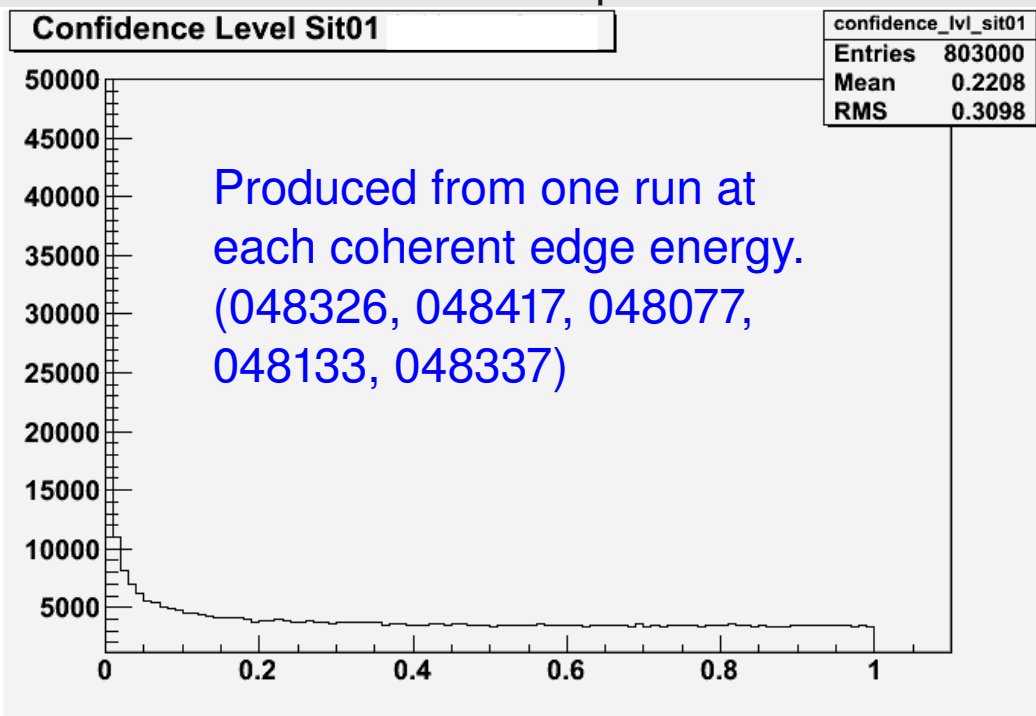
$$C = \begin{pmatrix} \sigma_{E_\gamma}^2 & 0 & 0 & 0 & \dots & 0 & 0 & 0 \\ 0 & C_1^{pp} & C_1^{p\lambda} & C_1^{p\phi} & \dots & 0 & 0 & 0 \\ 0 & C_1^{p\lambda} & C_1^{\lambda\lambda} & C_1^{\lambda\phi} & \dots & 0 & 0 & 0 \\ 0 & C_1^{p\phi} & C_1^{\lambda\phi} & C_1^{\phi\phi} & \dots & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & 0 & \dots & C_k^{pp} & C_k^{p\lambda} & C_k^{p\phi} \\ 0 & 0 & 0 & 0 & \dots & C_k^{p\lambda} & C_k^{\lambda\lambda} & C_k^{\lambda\phi} \\ 0 & 0 & 0 & 0 & \dots & C_k^{p\phi} & C_k^{\lambda\phi} & C_k^{\phi\phi} \end{pmatrix}$$

is.  
pull widths and slope



# Kinematic Fitting of g8b Data

- Uses energy/momentum conservation and missing mass to vary final state measurements within the error of the measurements.
- Tracking measurements (from the TBER bank) are used to build the covariance matrix.
- Quality of a fit  $\rightarrow$  pull distributions and confidence level.
- “Pure” parameters of the covariance matrix have pull distributions.
- Systematics affect pull means, covariance matrix errors affect pull widths and slope of confidence level plots.



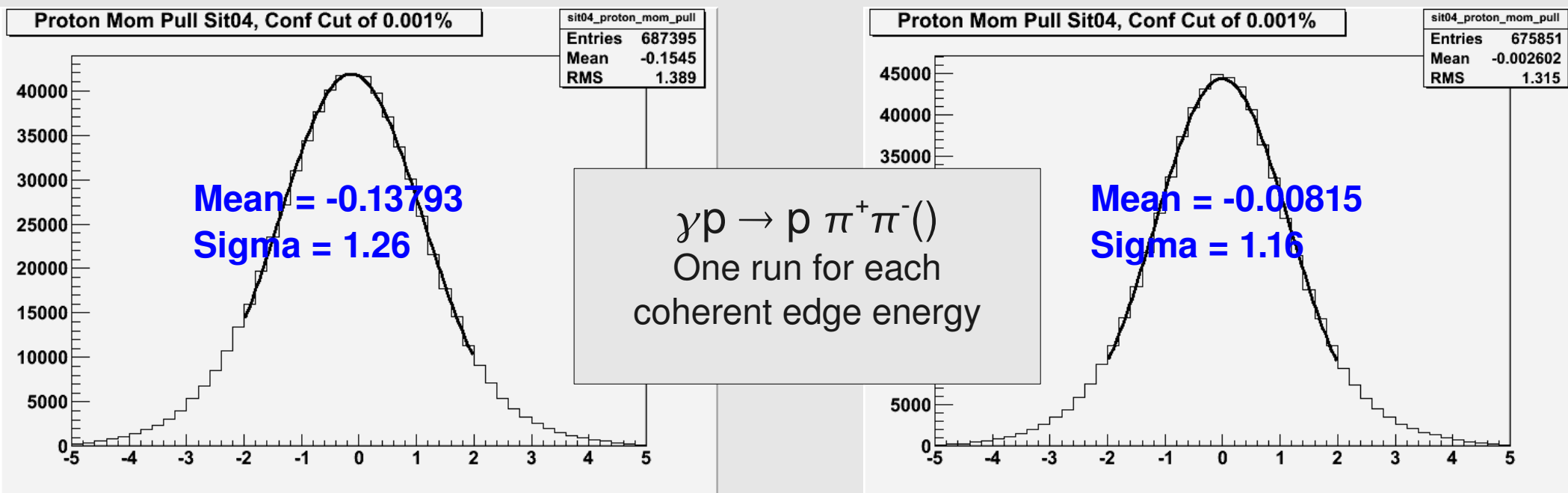
# Correcting the g8b data set

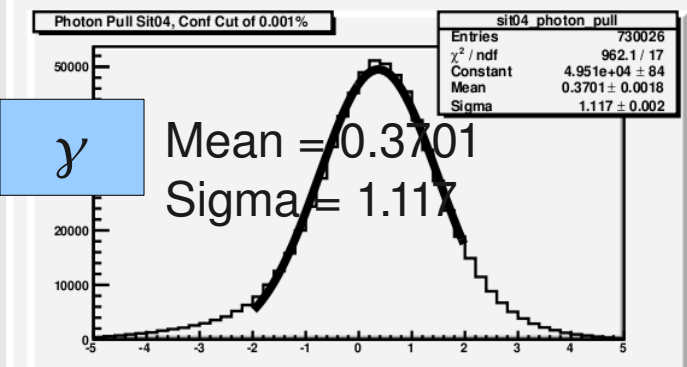
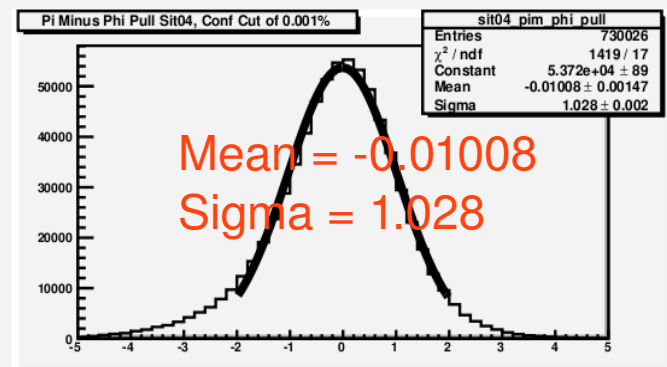
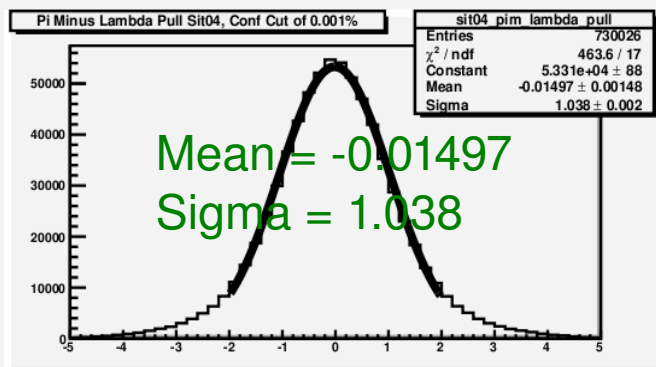
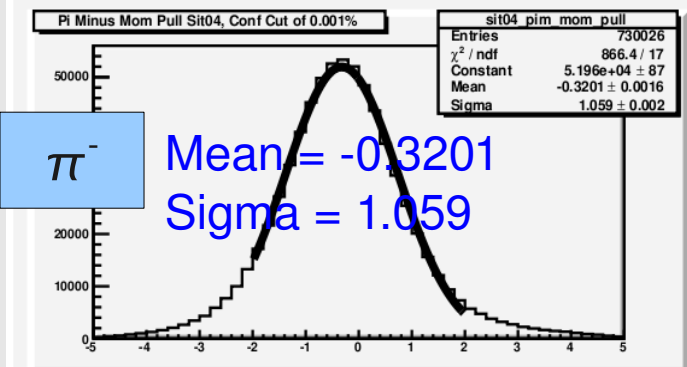
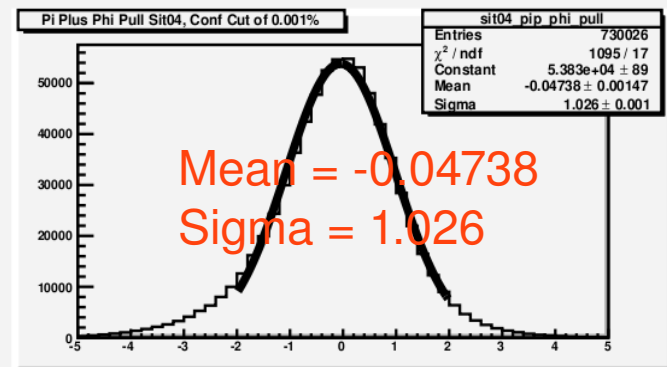
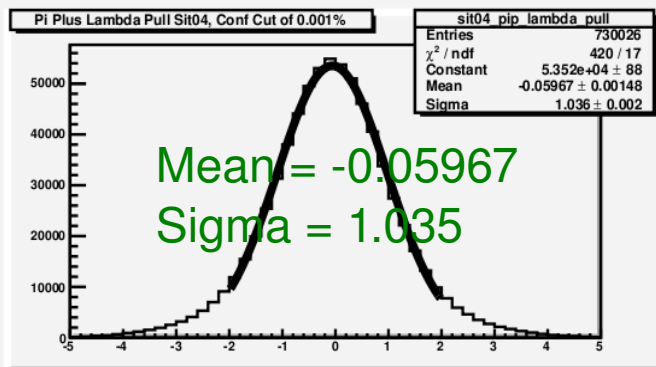
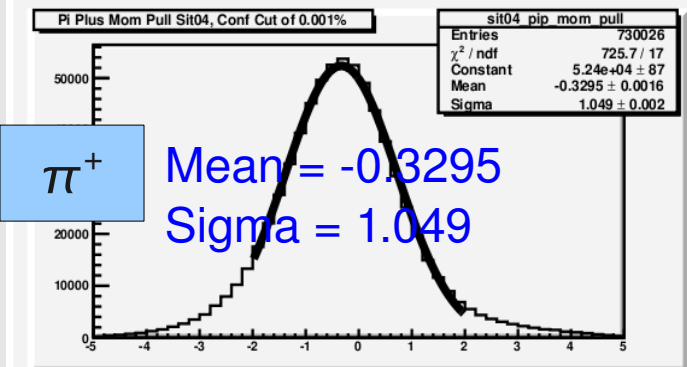
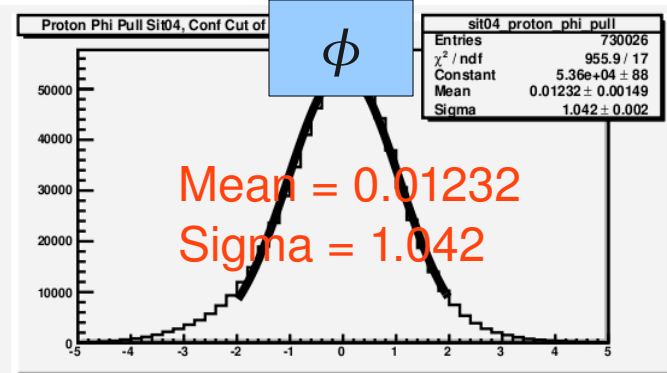
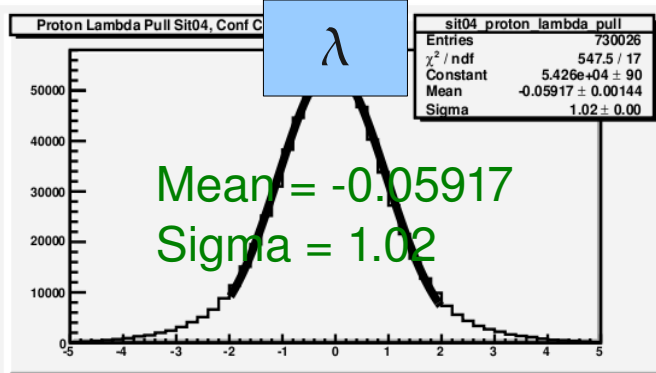
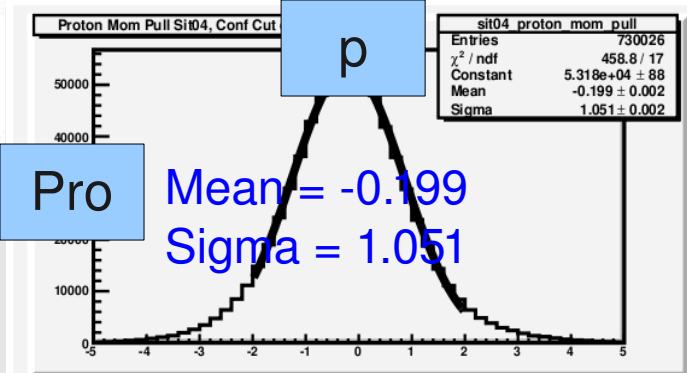
- Momentum corrections were determined using the pulls generated from fitting to a  $p \pi^+ \pi^-()$  final state.
- The errors applied to the covariance matrix were determined by starting with the g11a errors. Errors were altered to obtain pull widths of one.
- A study into the sag of the tagger E-counters produced an energy dependent photon correction.
- Momentum corrections were refined after the application of the photon corrections.
- Covariance matrix errors were also refined/finalized.



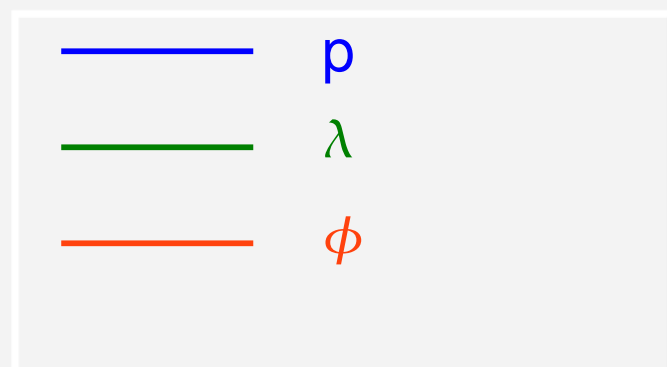
# Momentum Corrections

- Kinematic fitter is highly sensitive to changes in momentum → good tool for determining momentum corrections.
- Momentum pulls binned in: 7 bins in  $\theta$  (lab), 18 bins in  $\phi$  (lab), 6 bins in momentum (0.2-1.7 GeV).
- Corrections range from a few percent to ~10%.



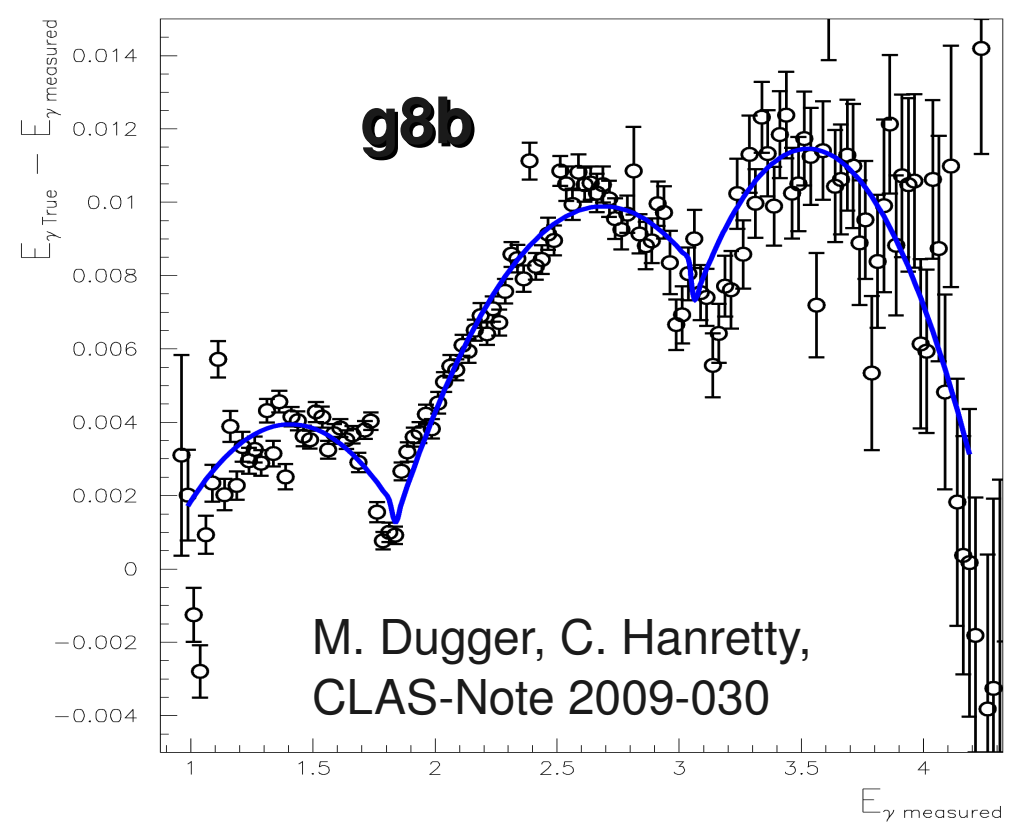
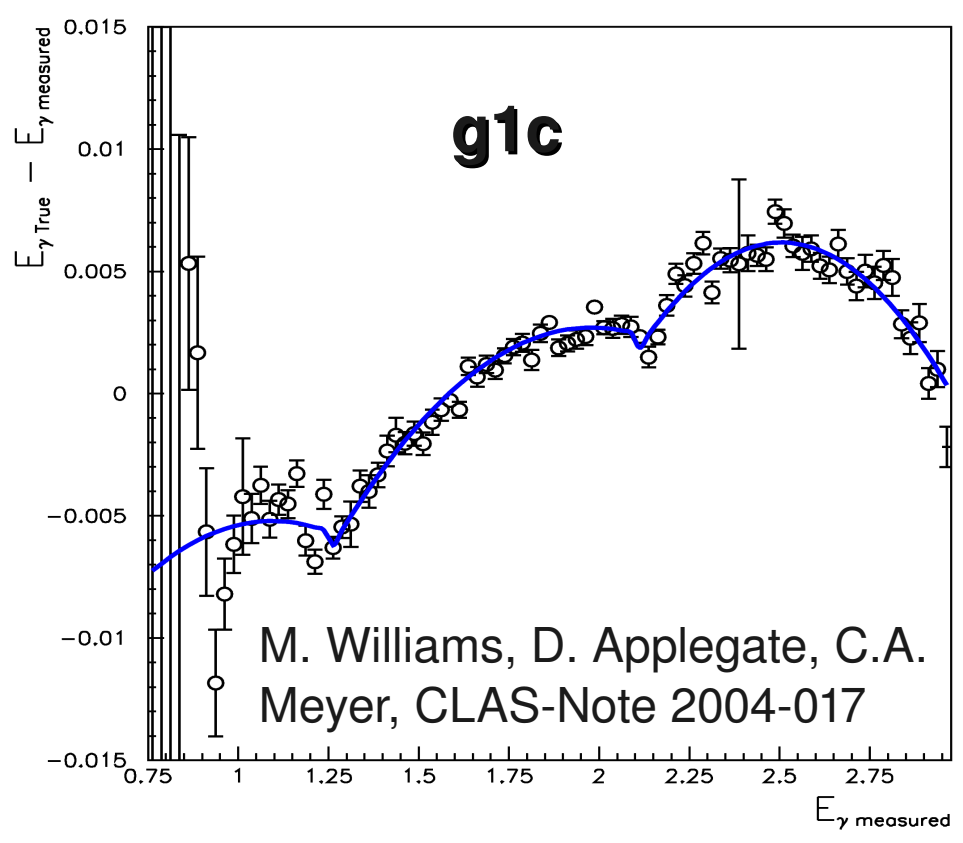


$\gamma p \rightarrow p \pi^+ \pi^- ()$   
(Run #048326)



# Tagger Sag

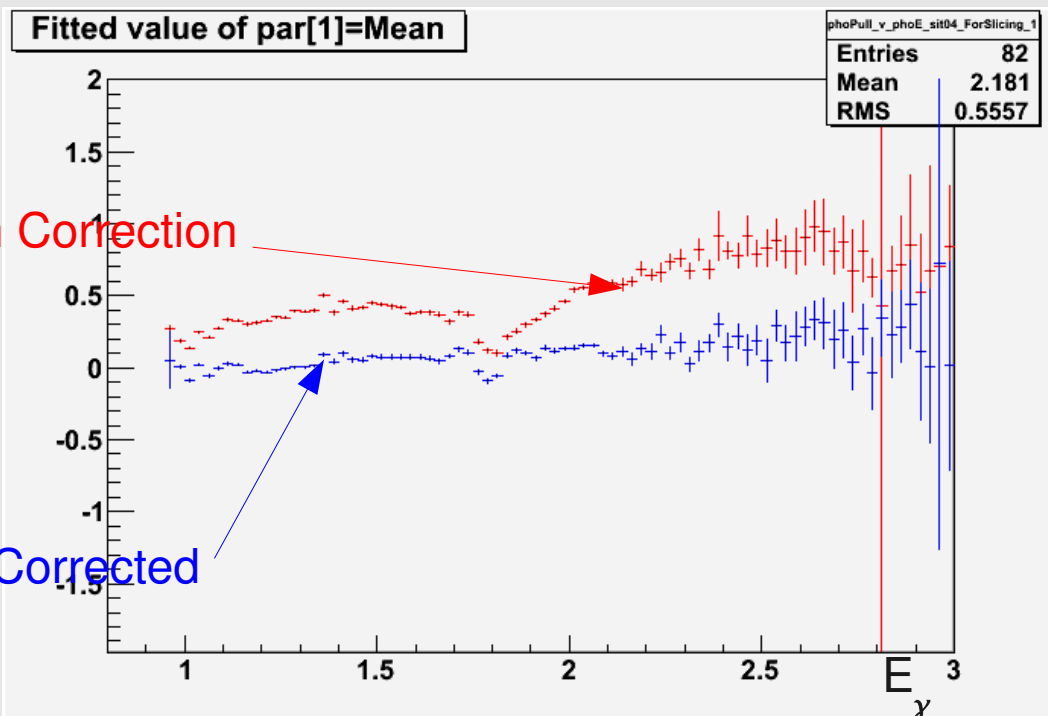
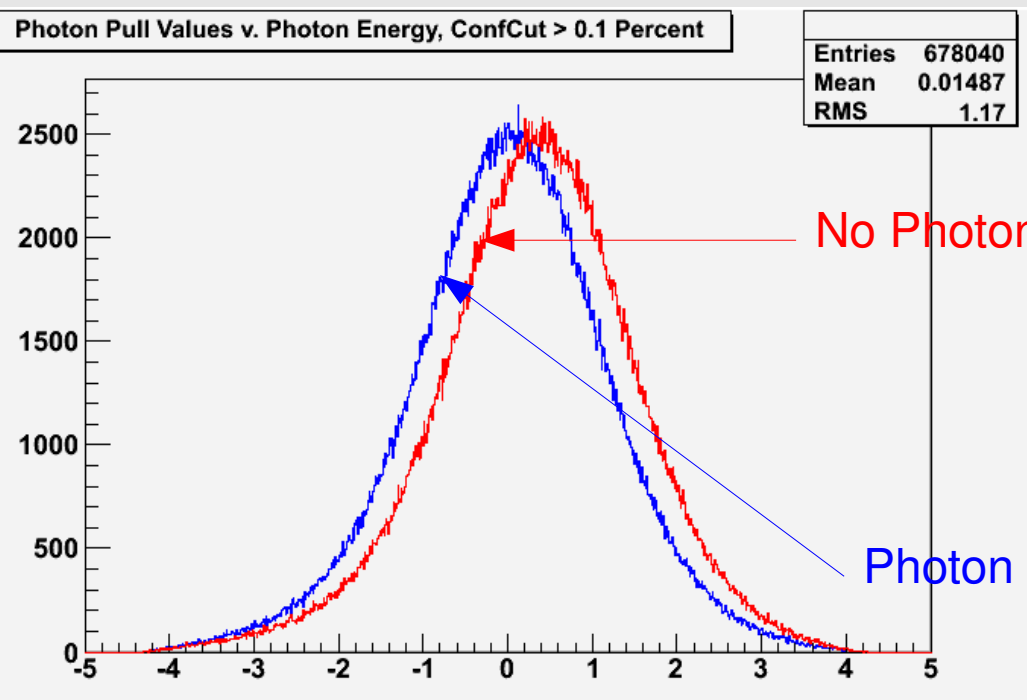
- Results from a physical “sagging” of the E-counter scintillator bars.
- Has been seen in several runs.

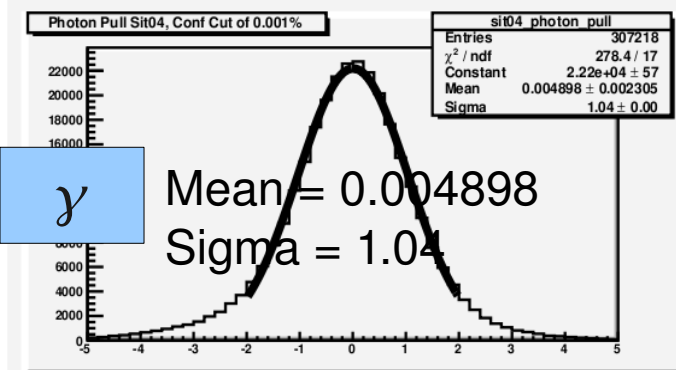
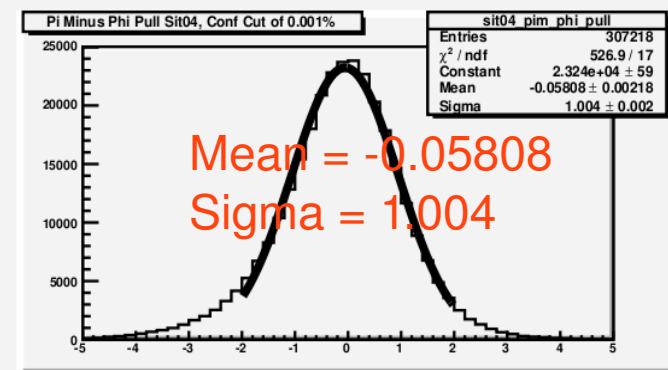
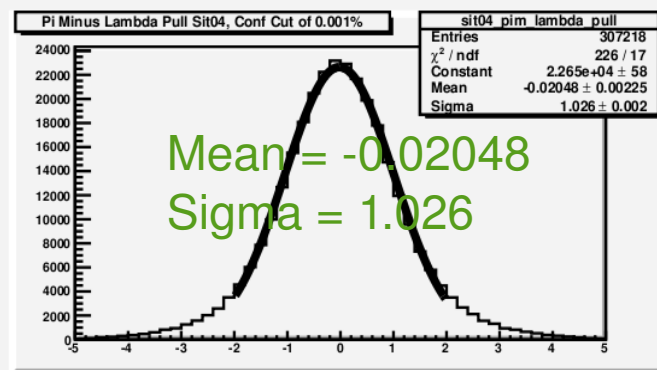
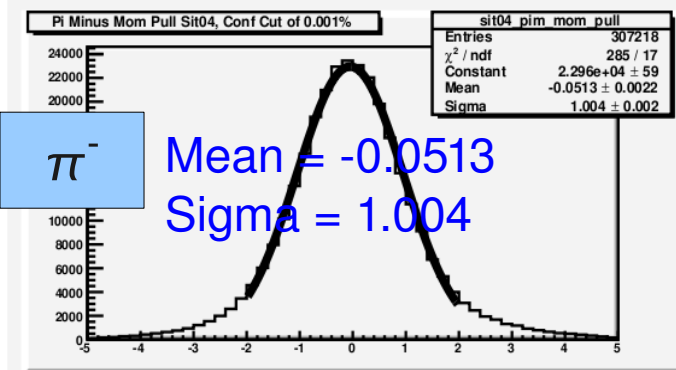
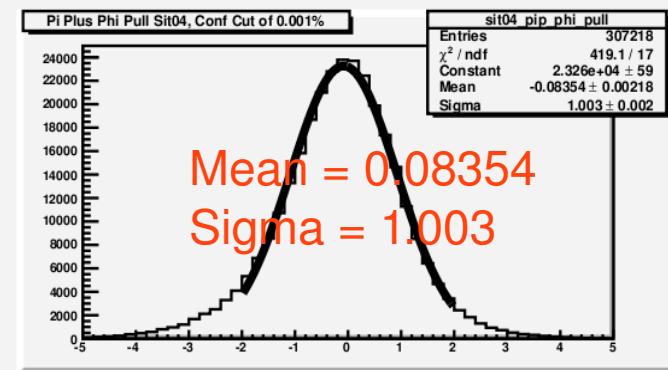
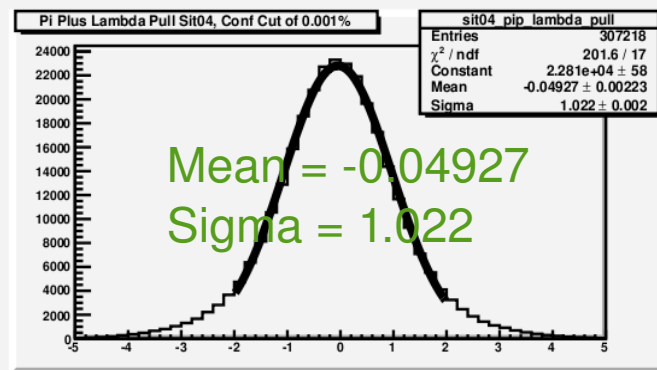
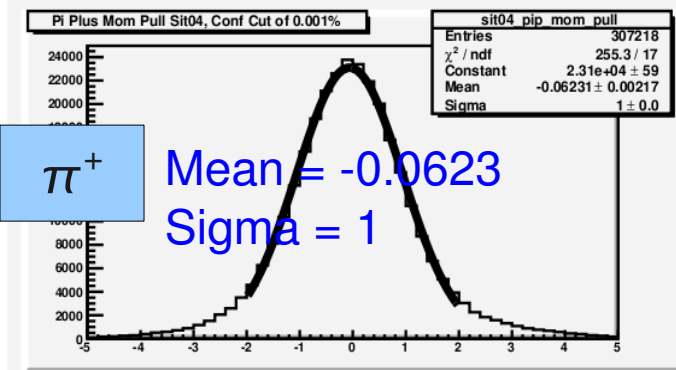
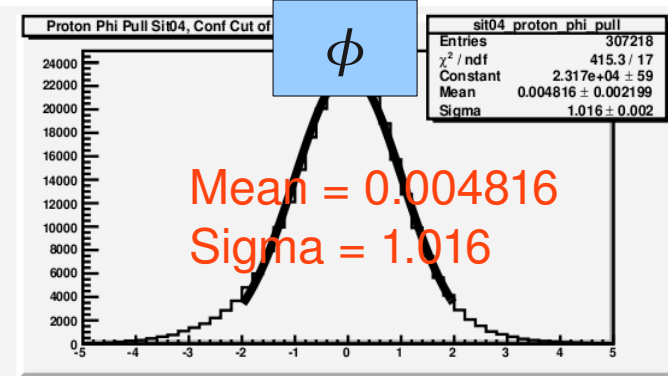
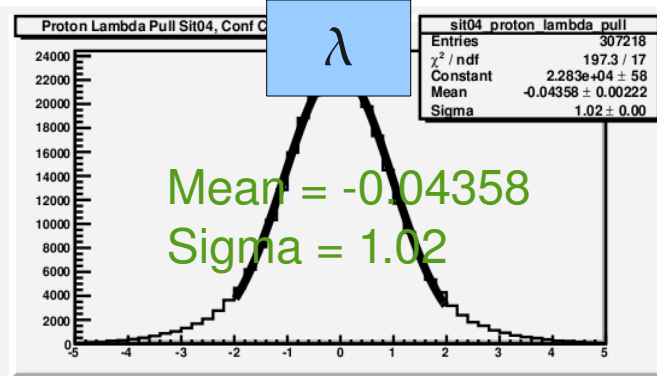
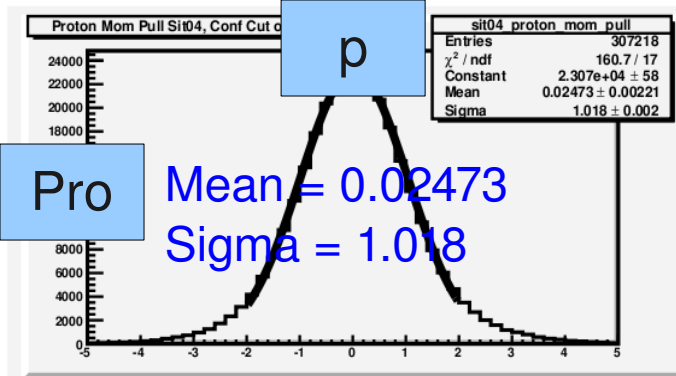




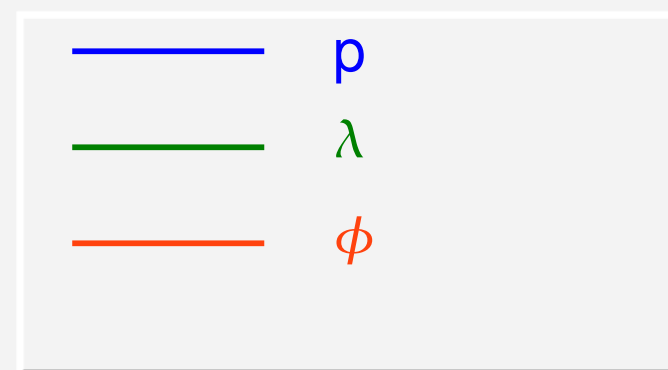
# Tagger Sag

- Results from a physical “sagging” of the E-counter scintillator bars.
- Has been seen in several runs.
- Requires and energy-dependent photon energy correction.





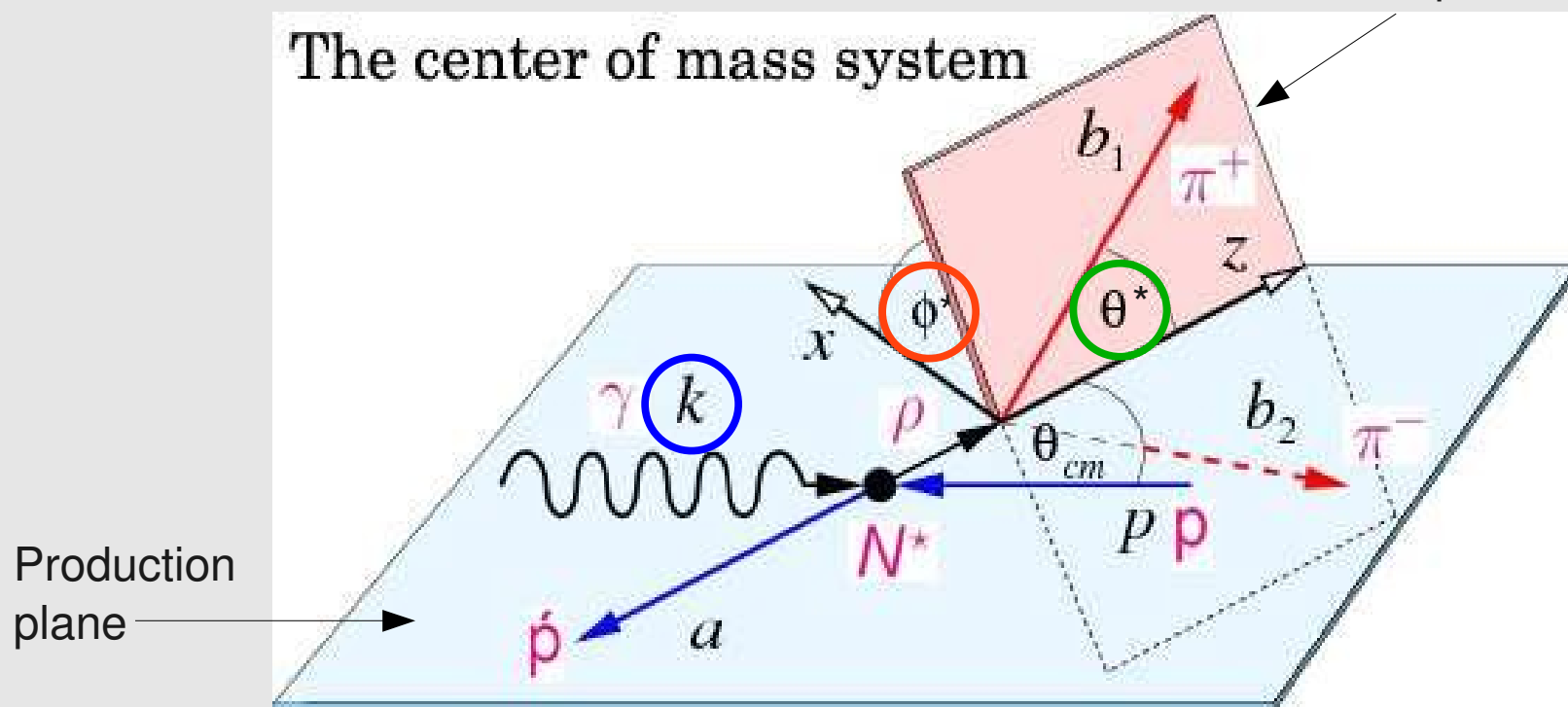
$\gamma p \rightarrow p \pi^+ \pi^- ()$   
(Run #048326)



# CM Coordinate System for $\gamma p \rightarrow p \pi^+ \pi^-$

- Analysis of the  $\gamma p \rightarrow p \pi^+ \pi^-$  channel requires the employ of 5 independent variables, for example :  $\cos\theta_{cm}$ ,  $m$ ,  $k$ ,  $\phi^*$ ,  $\theta^*$
- $\gamma p \rightarrow N^* \rightarrow N \rho \rightarrow p \pi^+ \pi^-$

Event plane formed by 2 final state particles

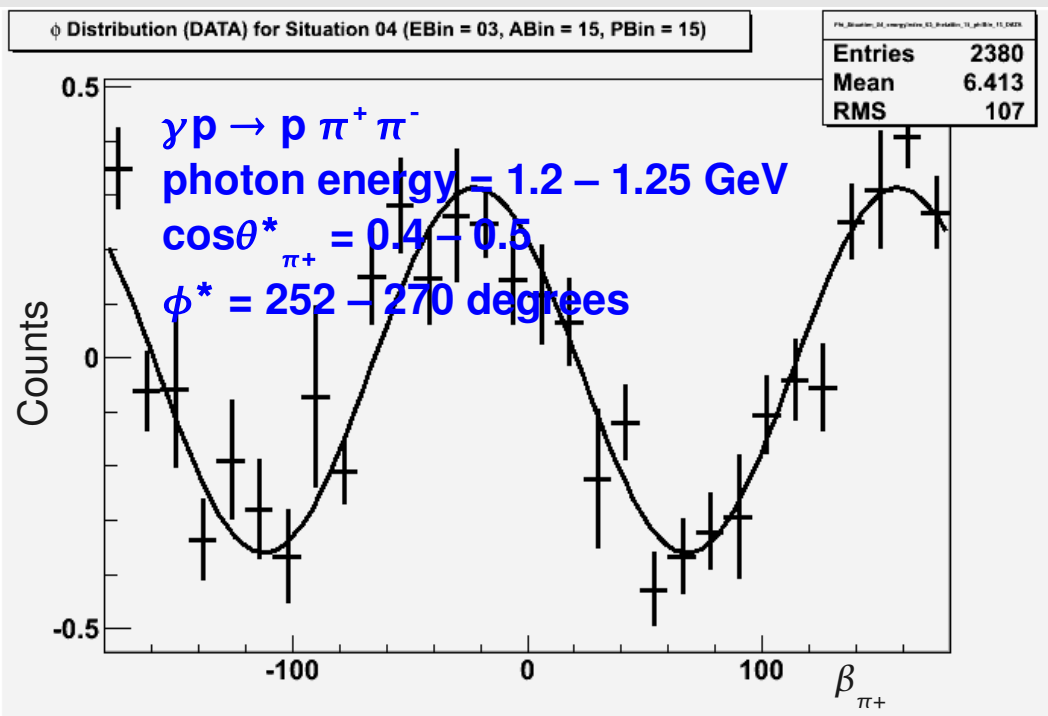
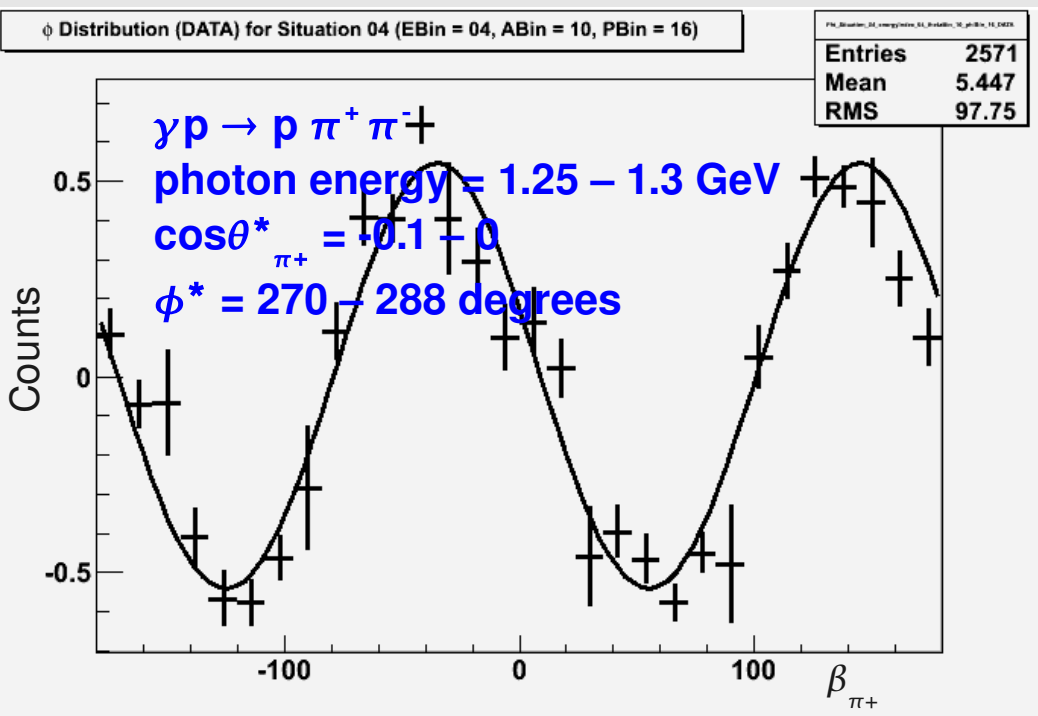




# Preliminary Results: Phi Distributions

- To remove systematics while maintaining statistics, the phi distributions for PARA are normalized to the PERP phi distributions.

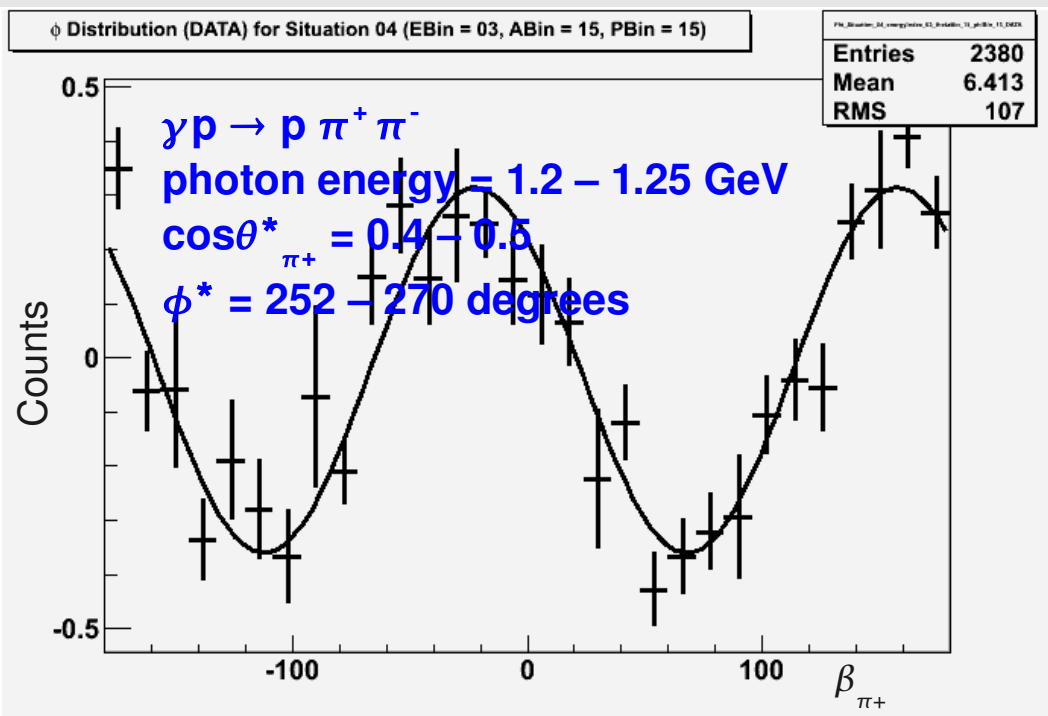
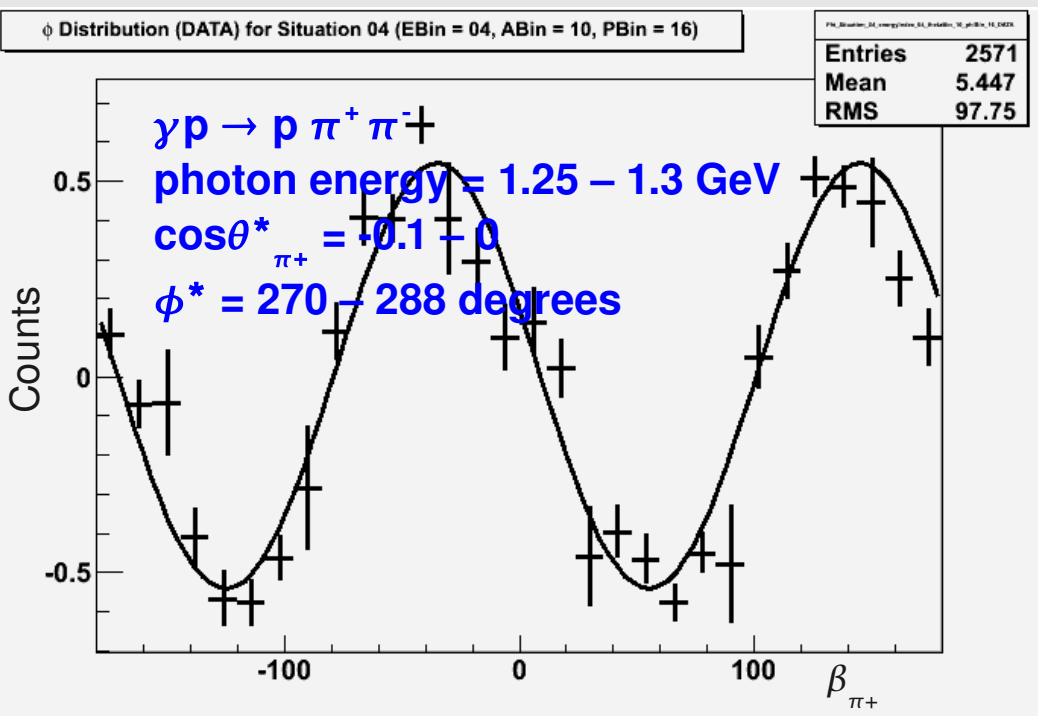
- Fit to : 
$$\frac{PARA - PERP}{PARA + PERP} = \frac{I_{PARA} - I_{PERP}}{I_{PARA} + I_{PERP}}$$



# Preliminary Results: Phi Distributions

- To remove systematics while maintaining statistics, the phi distributions for PARA are normalized to the PERP phi distributions.

- Fit to : 
$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)} \quad \beta = \phi_{lab} + \phi_{polarization}$$

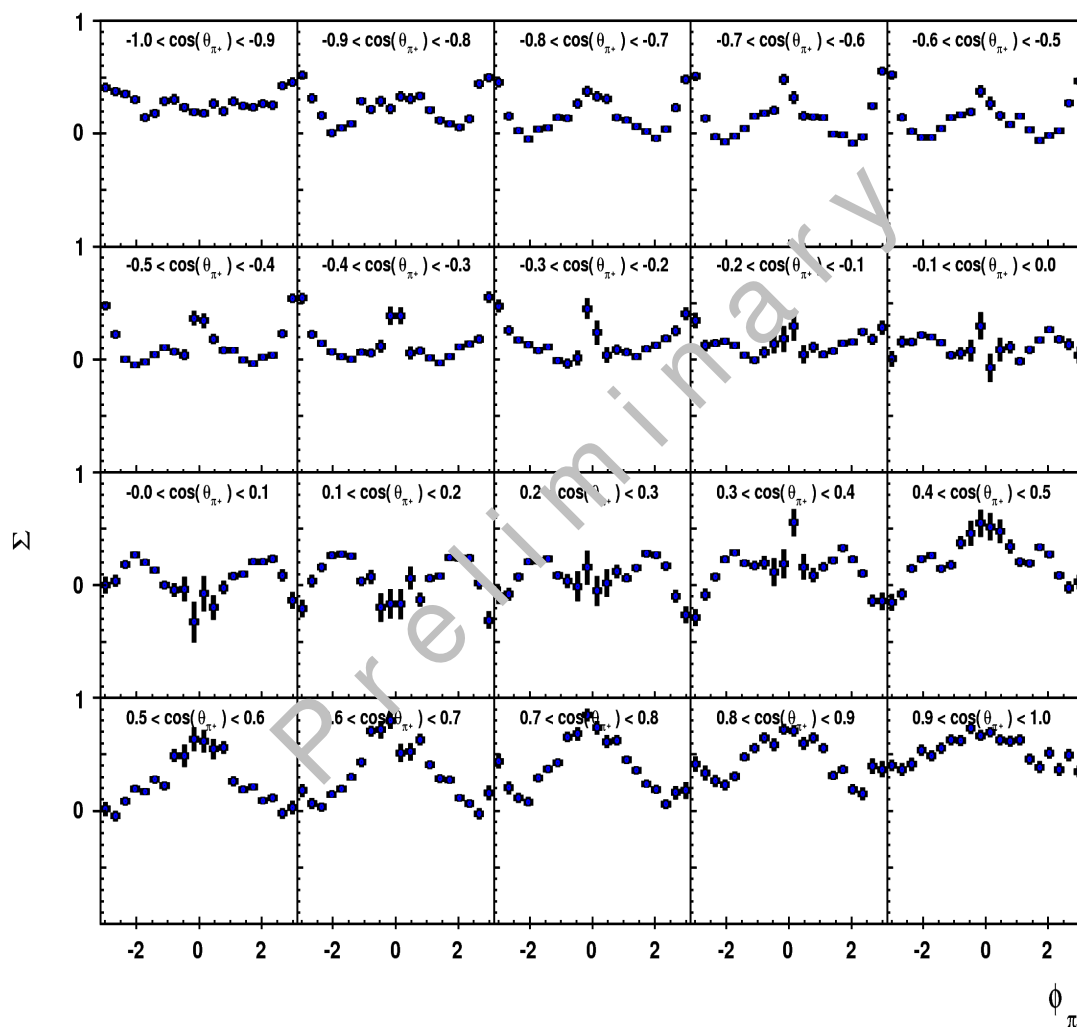


# Preliminary Results : $I^c$

$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)}$$

$\gamma p \rightarrow p \pi^+ \pi^- ()$

- Photon energy of 1100 – 1150 MeV
- Each square is an bin in  $\cos\theta^*$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- We see a non-zero value for  $I^c$  ( $\Sigma$ ).
- $I^c$  is symmetric around the origin.

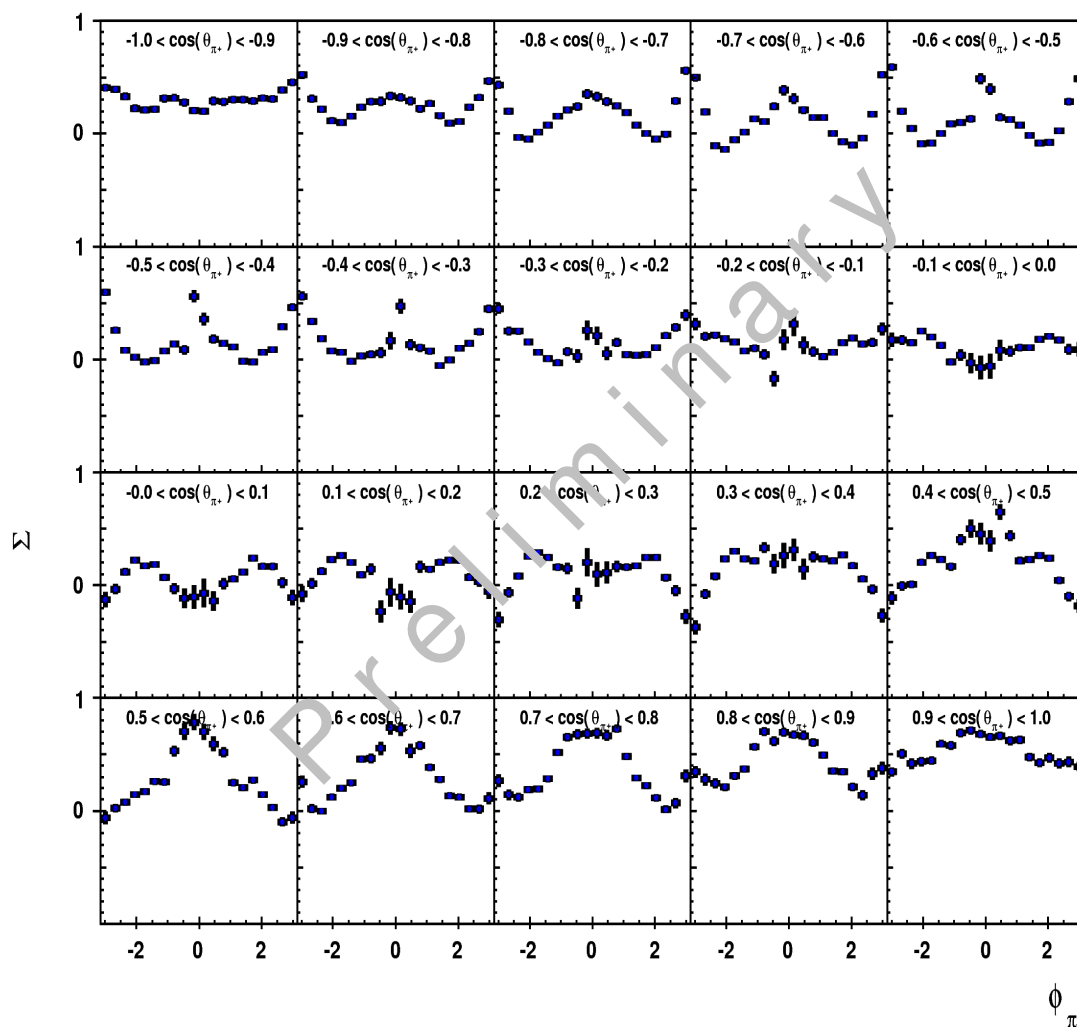


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$\gamma p \rightarrow p \pi^+ \pi^- ()$

- Photon energy of 1150 – 1200 MeV
- Each square is an bin in  $\cos\theta^*$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- We see a non-zero value for  $I^c$  ( $\Sigma$ ).
- $I^c$  is symmetric around the origin.



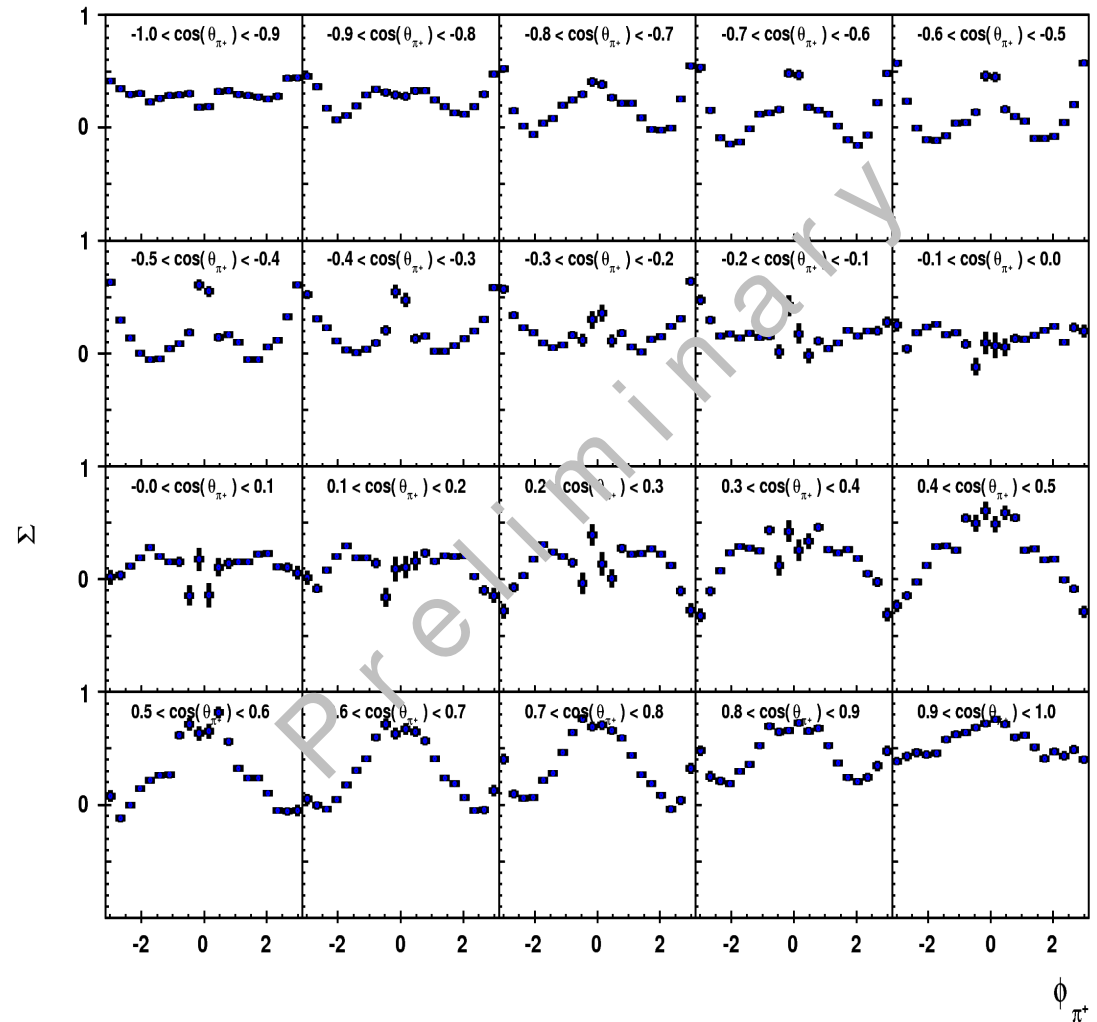


# Preliminary Results : $I^c$

$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)}$$

↓  $\gamma p \rightarrow p \pi^+ \pi^-()$

- Photon energy of 1200 – 1250 MeV
- Each square is an bin in  $\cos\theta^*$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- We see a non-zero value for  $I^c$  ( $\Sigma$ ).
- $I^c$  is symmetric around the origin.

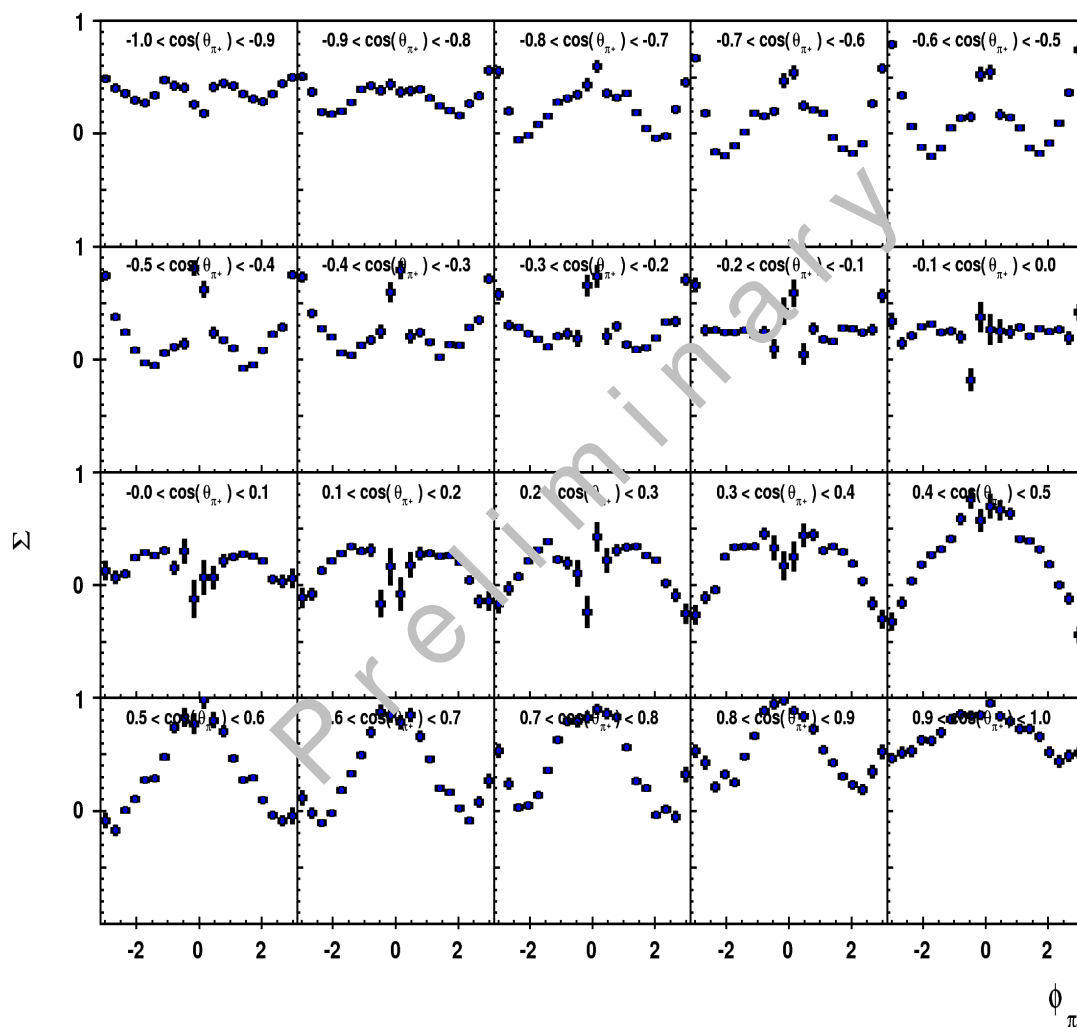


# Preliminary Results : $I^c$

$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)}$$

$\gamma p \rightarrow p \pi^+ \pi^- ()$

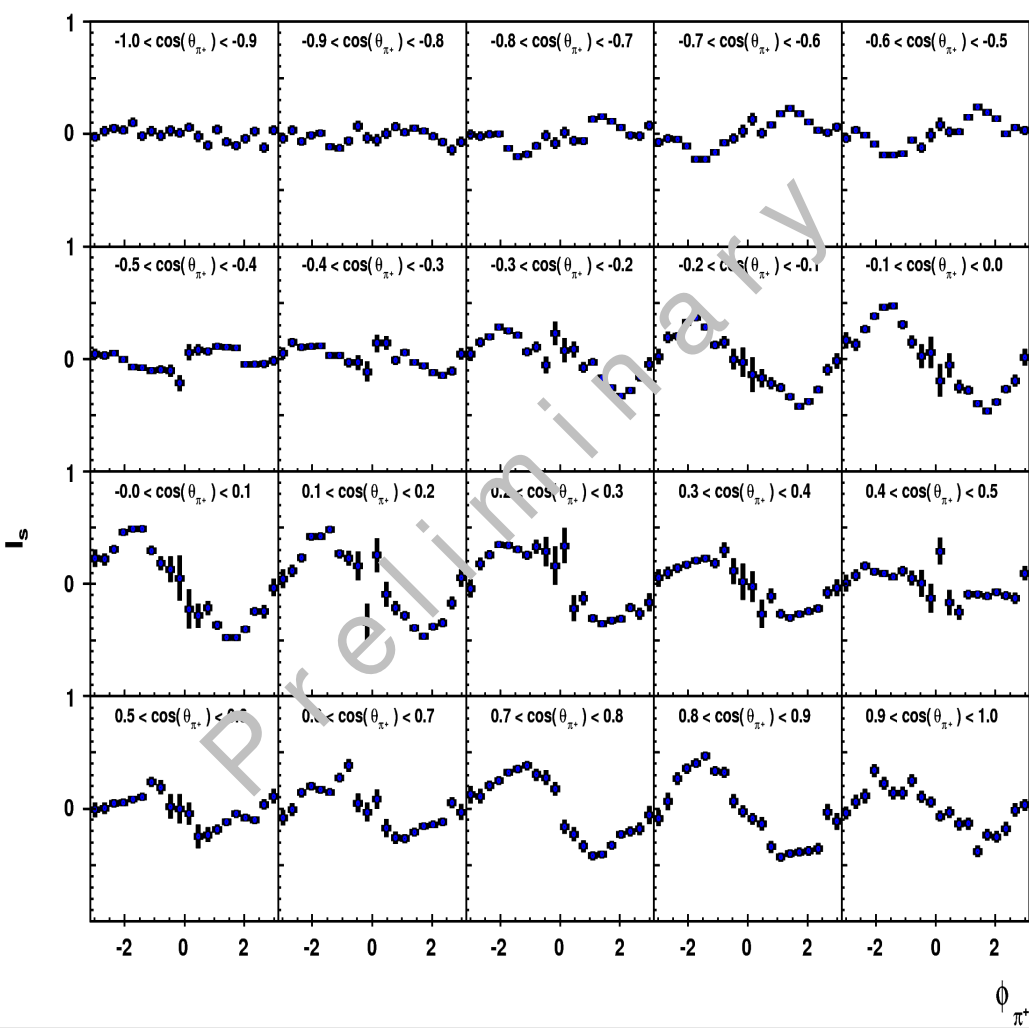
- Photon energy of 1250 – 1300 MeV
- Each square is an bin in  $\cos\theta^*$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- We see a non-zero value for  $I^c$  ( $\Sigma$ ).
- $I^c$  is symmetric around the origin.



# Preliminary Results : $I^s$

$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)}$$

$\gamma p \rightarrow p \pi^+ \pi^- ()$

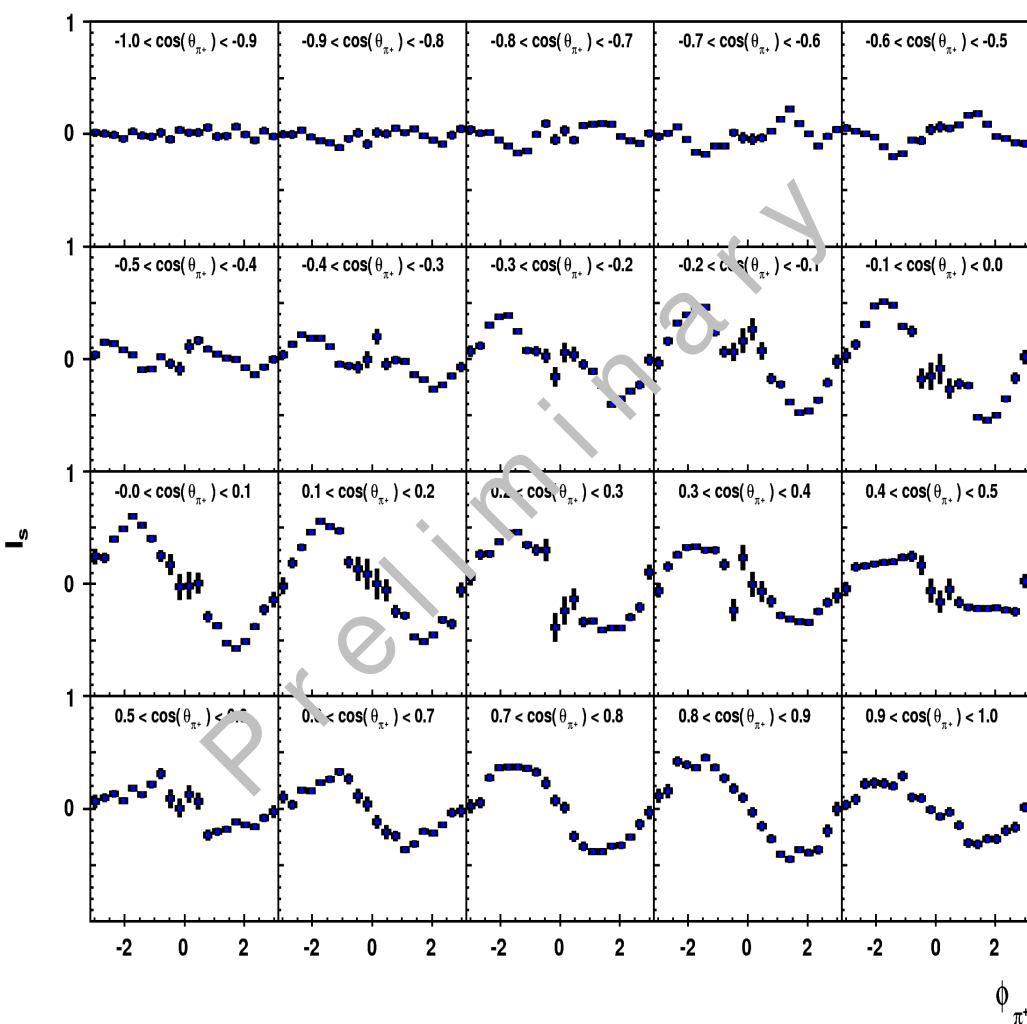


- Photon energy of 1100 – 1150 MeV
- Each square is an bin in  $\cos\theta^+$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- $I^s$  is antisymmetric around the origin.

# Preliminary Results : $I^s$

$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)}$$

$\gamma p \rightarrow p \pi^+ \pi^- ()$



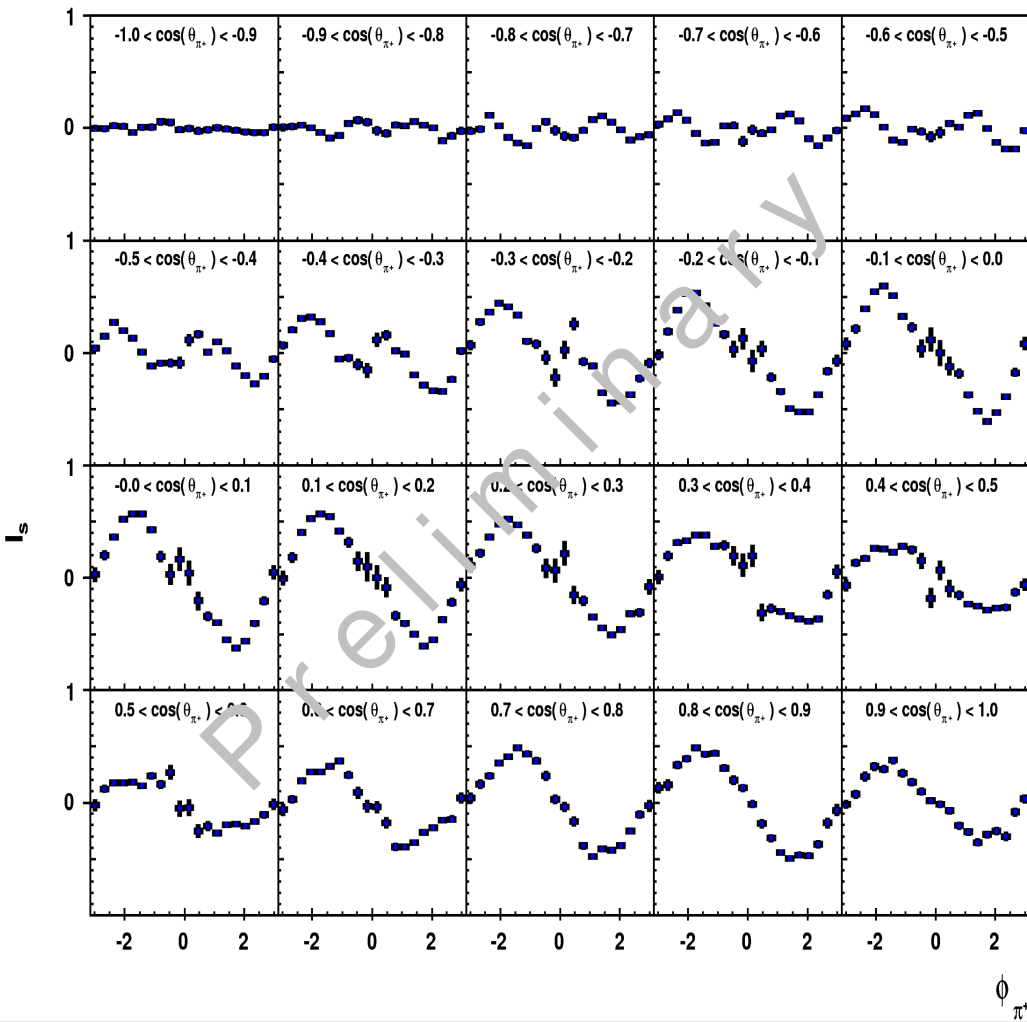
- Photon energy of 1150 – 1200 MeV
- Each square is an bin in  $\cos\theta^+$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- $I^s$  is antisymmetric around the origin.



# Preliminary Results : $I^s$

$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)}$$

$\gamma p \rightarrow p \pi^+ \pi^- ()$

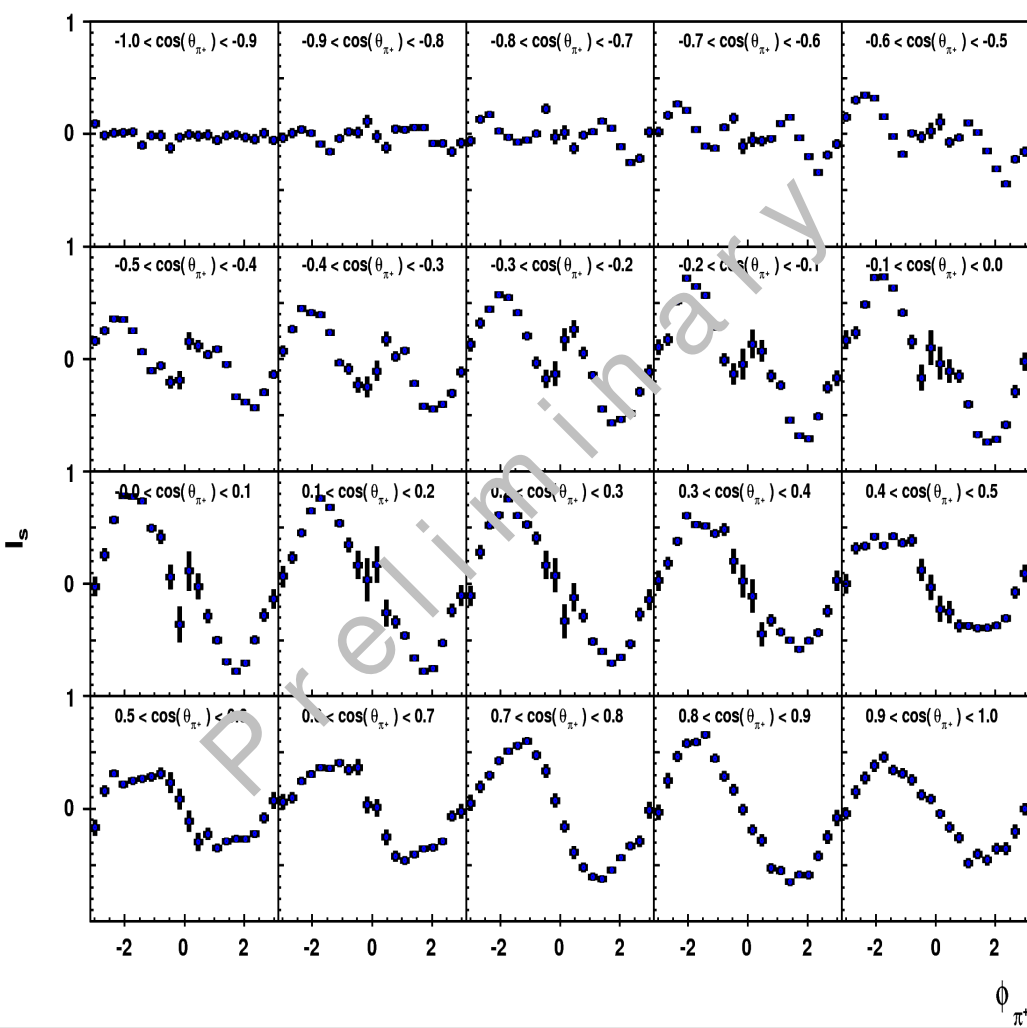


- Photon energy of 1200 – 1250 MeV
- Each square is an bin in  $\cos\theta^+$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- $I^s$  is antisymmetric around the origin.

# Preliminary Results : $I^s$

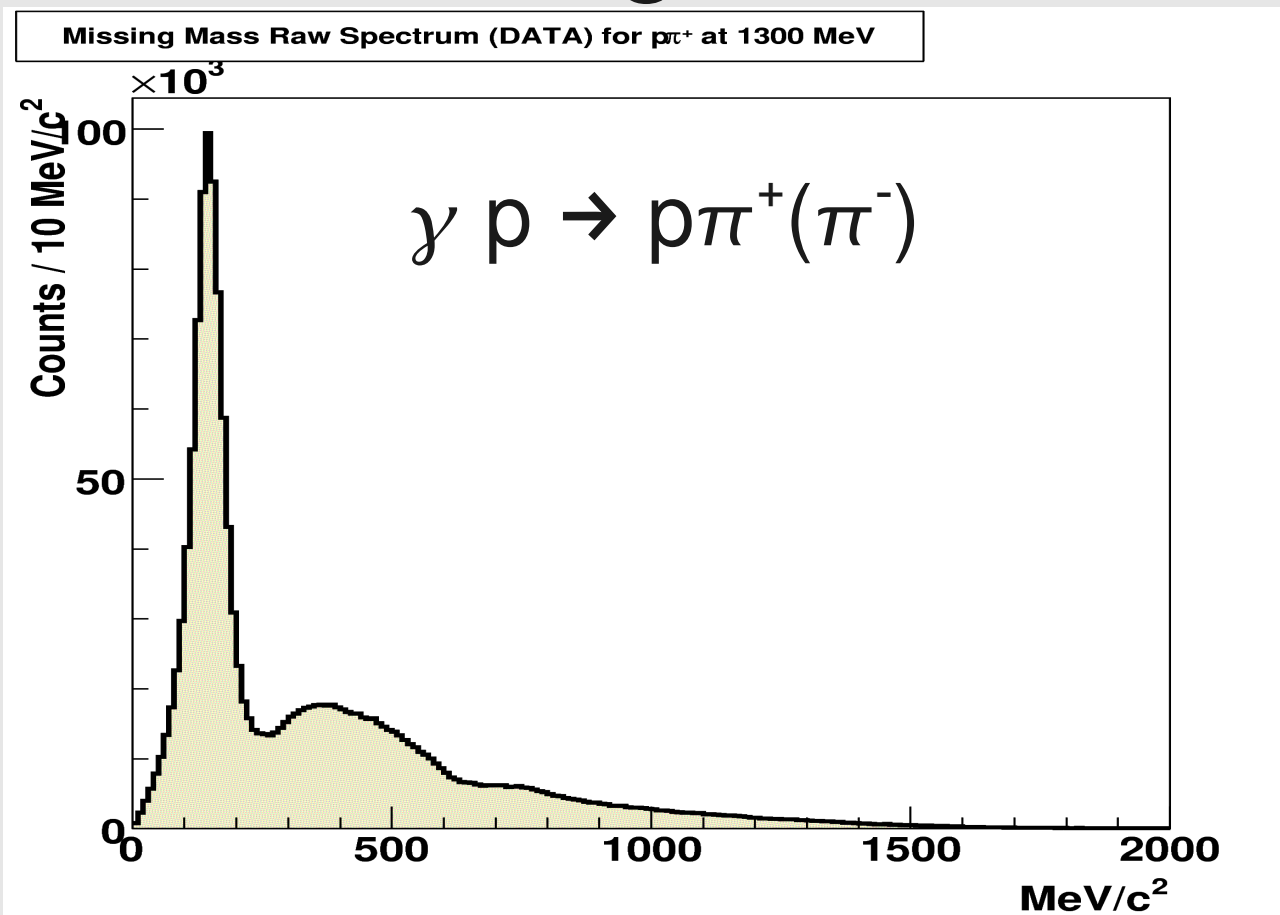
$$\frac{[(\delta_l^{para} + \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} - \delta_l^{perp}) I^c \cos(2\beta)]}{2 + (\delta_l^{para} - \delta_l^{perp}) I^s \sin(2\beta) + (\delta_l^{para} + \delta_l^{perp}) I^c \cos(2\beta)}$$

$\gamma p \rightarrow p \pi^+ \pi^- ()$



- Photon energy of 1250 – 1300 MeV
- Each square is an bin in  $\cos\theta^+$  of the  $\pi^+$ .
- Y-axis is the value of the observable.
- X-axis is the  $\phi$  of the  $\pi^+$ .
- $I^s$  is antisymmetric around the origin.

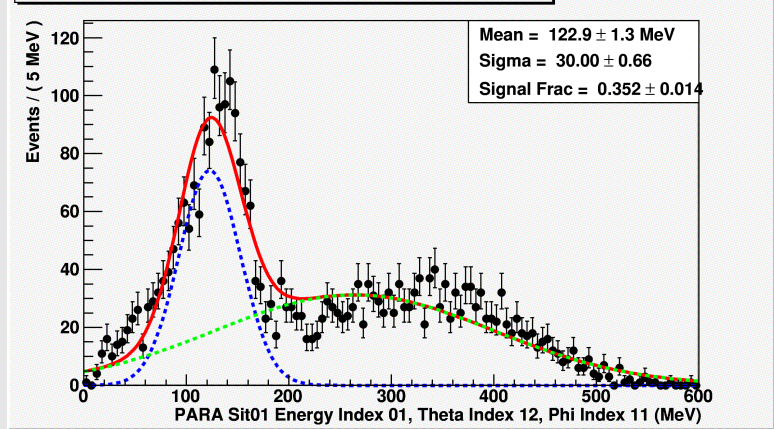
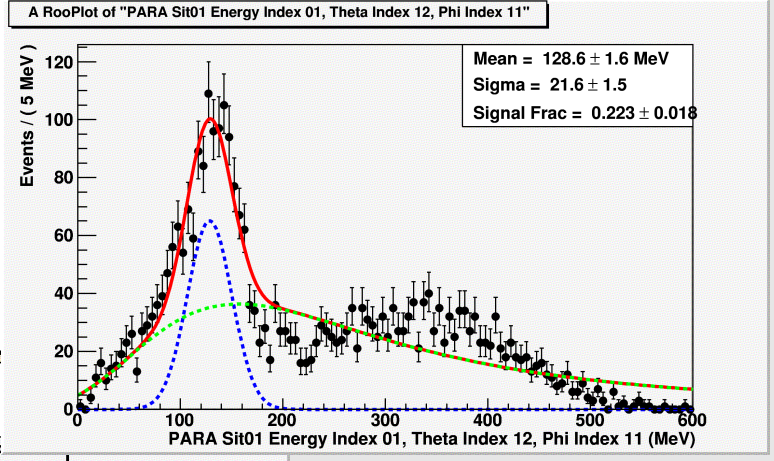
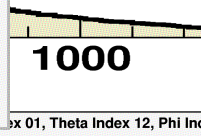
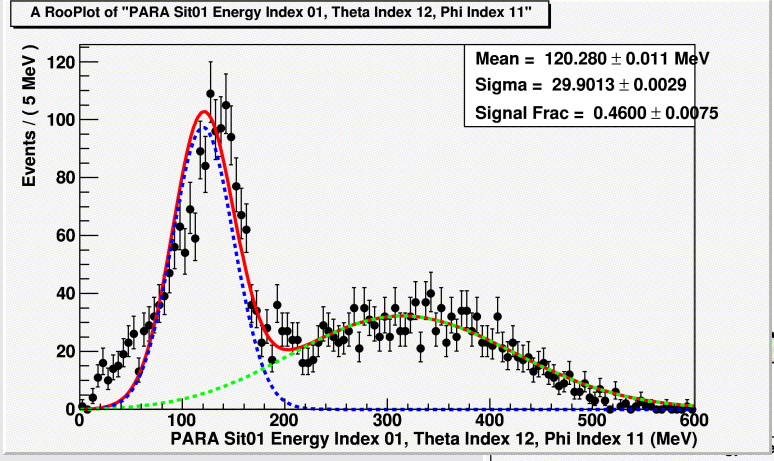
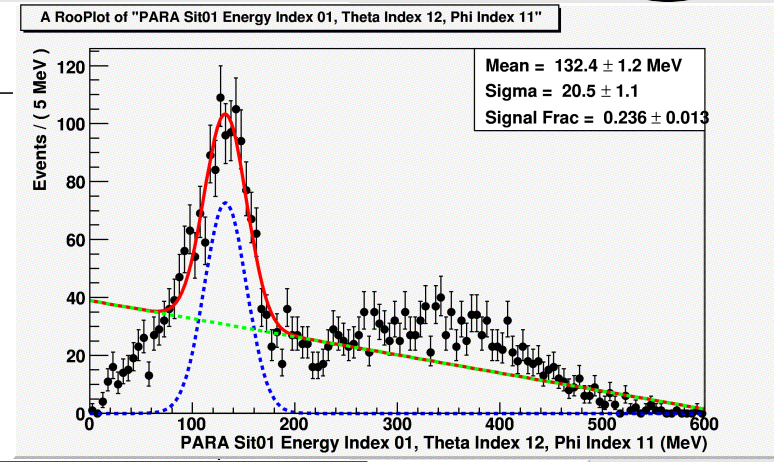
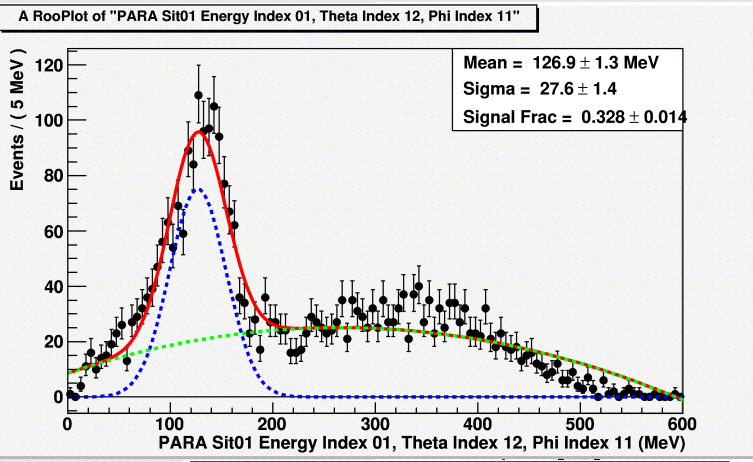
# Background



# Background

Spectrum (DATA) for  $p\pi^+$  at 1300 MeV

$$\gamma p \rightarrow p\pi^+(\pi^-)$$





# Q-Values

- Traditional (side-band) background subtraction requires binning in the kinematic variables and is therefore limited by statistics.
- This method is statistics-independent and uses unbinned fits.
- $Q$  is the “probability” that an event is from signal,  $(1-Q)$  is the chance its background.
- Can be used “universally” weight an event in any distribution.
- The good : Event-based background determination, statistic-independent, “universal” application.
- The bad : Very time consuming and computationally intensive.
- For further information see: M. Williams, M. Bellis, C. A. Meyer, CLAS-Note: 2007-013

# Q-Values : The procedure

- Find/Get 4-vecs, angles, photon energy for first event (this is the “seed” event).
- Out of all of the kinematic variables, pick a “reference coordinate”.
- Loop through all other events finding/getting the 4-vecs, angles, photon energy.
- Find the 100 events that are closest to the seed event in terms of the non-reference kinematic variables.
- Using these 100 events, perform a fit to the reference coordinate using a signal and background function. Not a fit to a histo and therefore unbinned.
- Extract Q value for seed event by finding the number of events in signal peak at the value of the reference coordinate of the seed event in the fit.  
 $Q = s/(s+b)$ ; s=events
- “Q” is the chance that the seed event is a signal event, “(1-Q)” is the chance that the seed event is from background.
- Rinse and repeat for all events.

# Q-Values : The procedure

- Find/Get 4-vecs, angles, photon energy for first event (this is the “seed” event).
- Out of all of the kinematic variables, pick a “reference coordinate”.
- Loop through all other events finding/getting the 4-vecs, angles, photon energy.
- Find the 100 events that are closest to the seed event in terms of the non-reference kinematic variables.

$$d_{ij}^2 = \sum_{k=1}^n \left[ \frac{\xi_k^i - \xi_k^j}{r_k} \right]^2$$

$n$  = number of kinematic variables  
 $i$  = seed event  
 $j$  = the next event (in loop over events)  
 $r$  = range of kinematic variable

- Use significance
- Expected Q
- “Q” that the seed event is from background.

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- Rinse and repeat for all events.

# Q-Values : The procedure

- Find/Get 4-vecs, angles, photon energy for first event (this is the “seed” event).
- Out of all of the kinematic variables, pick a “reference coordinate”.
- Loop through all other events finding/getting the 4-vecs, angles, photon energy.
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- Using these 100 events, perform a fit to the reference coordinate using a signal and background function. Not a fit to a histo and therefore unbinned.
- Extract Q value for seed event by finding the number of events in signal peak at the value of the reference coordinate of the seed event in the fit.  
 $Q = s/(s+b)$ ;  $s$ =events in the signal;  $b$ =events in background.
- “Q” is the chance that the seed event is a signal event, “(1-Q)” is the chance that the seed event is from background.
- Rinse and repeat for all events.



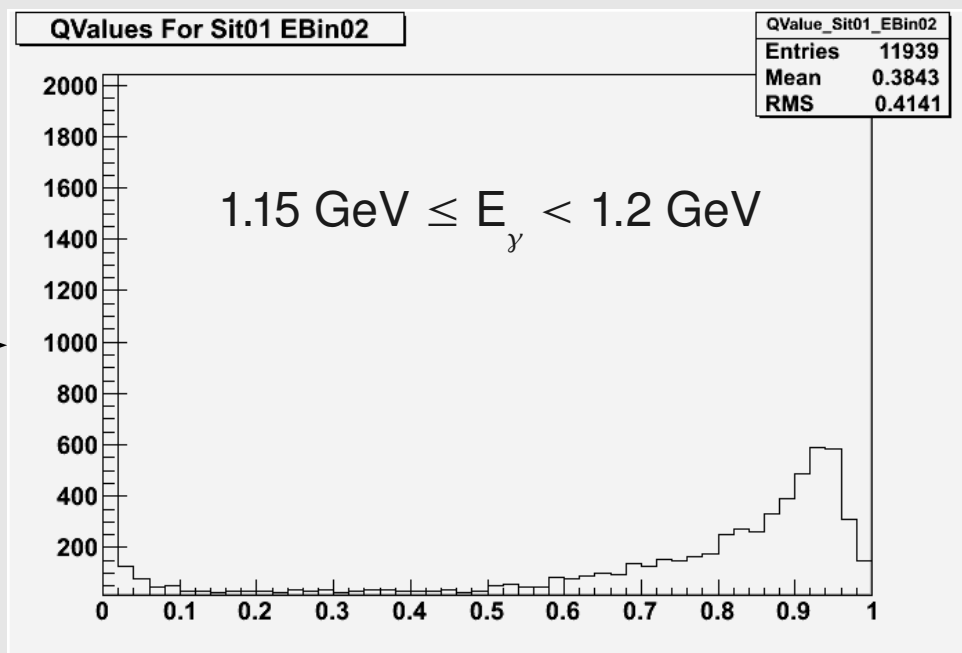
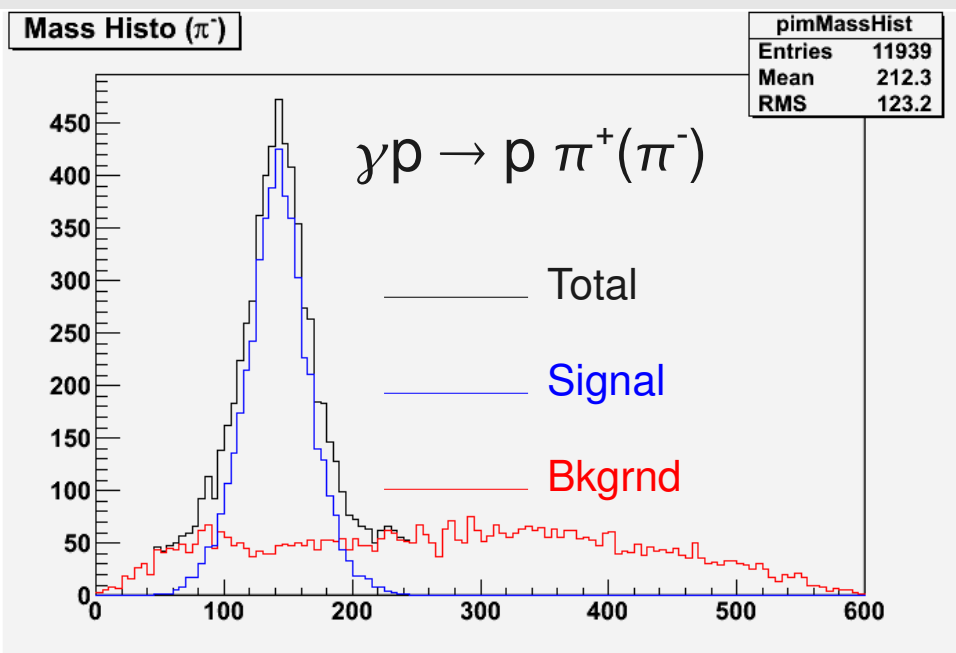
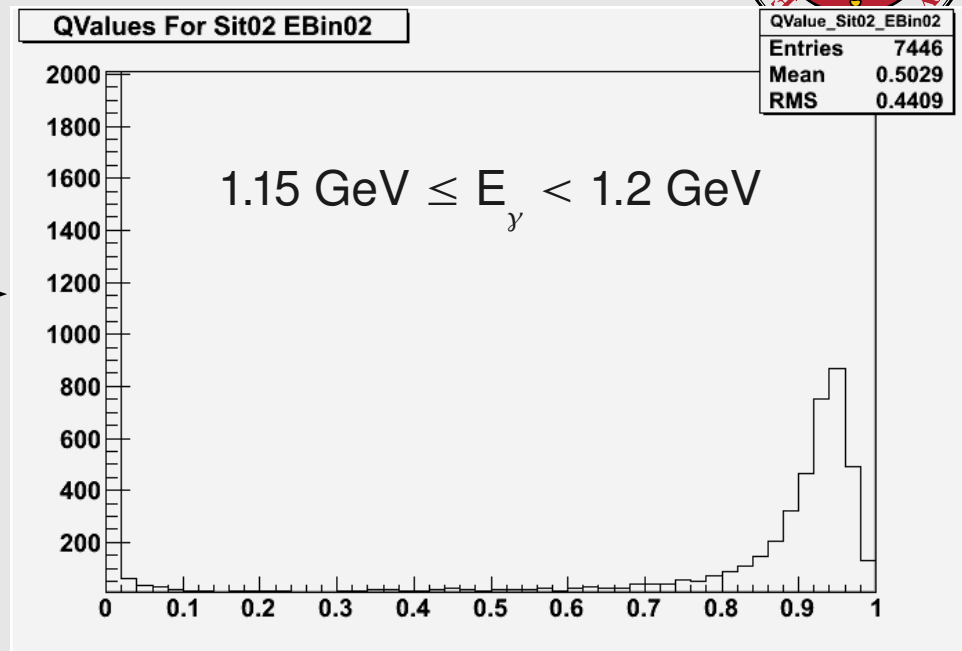
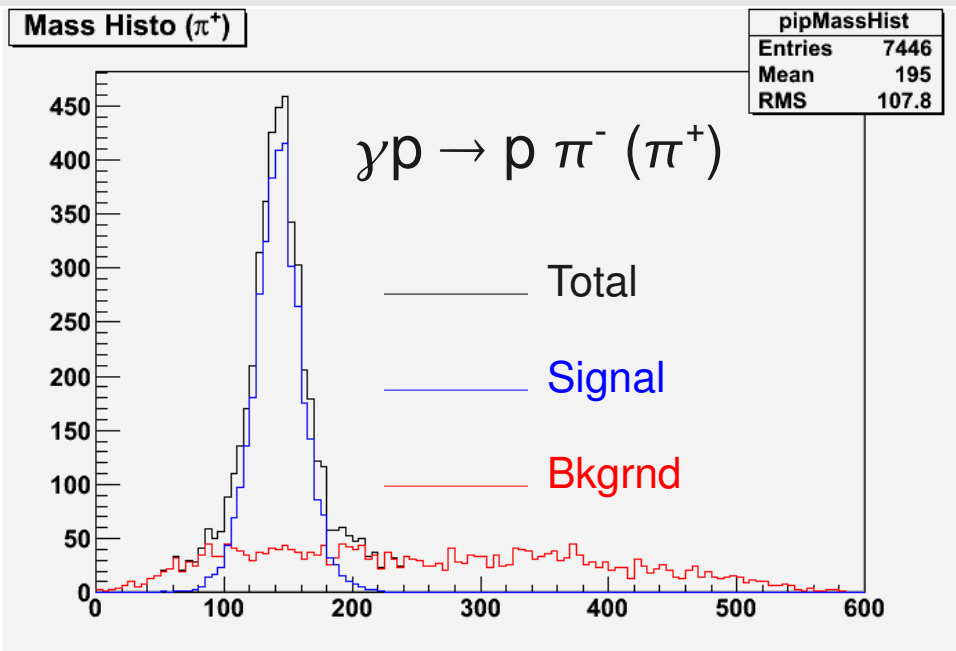
# Q-Values : The procedure

- Find/Get 4-vecs, angles, photon energy for first event (this is the “seed” event).
- Out of all events, find the “seed” event.
- Loop through all events, find the photon energy.
- Find the reference coordinate.
- Using these 100 events, perform a fit to the reference coordinate using a signal and background function. Not a fit to a histo and therefore unbinned.
- Extract Q value for seed event by finding the number of events in signal peak at the value of the reference coordinate of the seed event in the fit.  $Q = s/(s+b)$ ;  $s$ =events in the signal;  $b$ =events in background.
- “Q” is the chance that the seed event is a signal event, “(1-Q)” is the chance that the seed event is from background.
- Rinse and repeat for all events.

$$Q = \frac{s}{s + b}$$

$s$  = number of signal events  
 $b$  = number of background events

# Q-Values



.....Application of this procedure to the g8b data set not yet finalized

# Still to do:

- Get and implement new degree-of-polarization tables from Ken Livingston.
- Re-run data to produce new asymmetry plots and measurements.
- Finalize Q-Value determinations for background subtraction.
- Apply these Q-Values to beam asymmetry measurements.



END