

Measurement of beam and target polarization observables in $\vec{\gamma}\vec{p} \rightarrow p\pi^+\pi^-$ using the CLAS spectrometer at Jefferson Lab

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Dissertation Defense



1 Introduction

- Baryon Spectroscopy
- Why is $\pi^+\pi^-$ photoproduction needed ?

2 FROST Experiment

- Jefferson Laboratory in Newport News, VA
- Experimental devices for the FROST experiment

3 Data Analysis

- Kinematic variables
- Previous measurements
- Basic event selection

4 Preliminary Results

- Polarization Observable I^{\odot}
- Q-factor method : Event-based background subtraction
- Polarization Observable \mathbf{P}_z
- Polarization Observable \mathbf{P}_z^{\odot}

5 Summary

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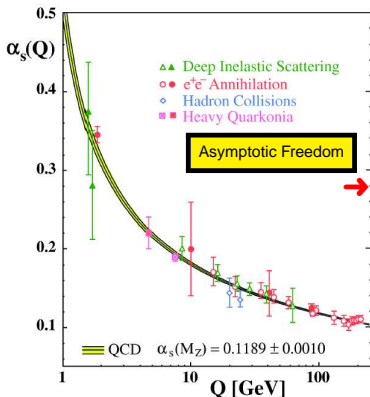
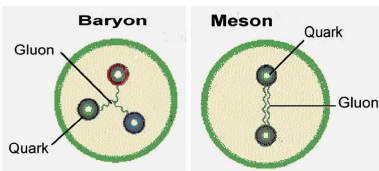
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What are hadrons?



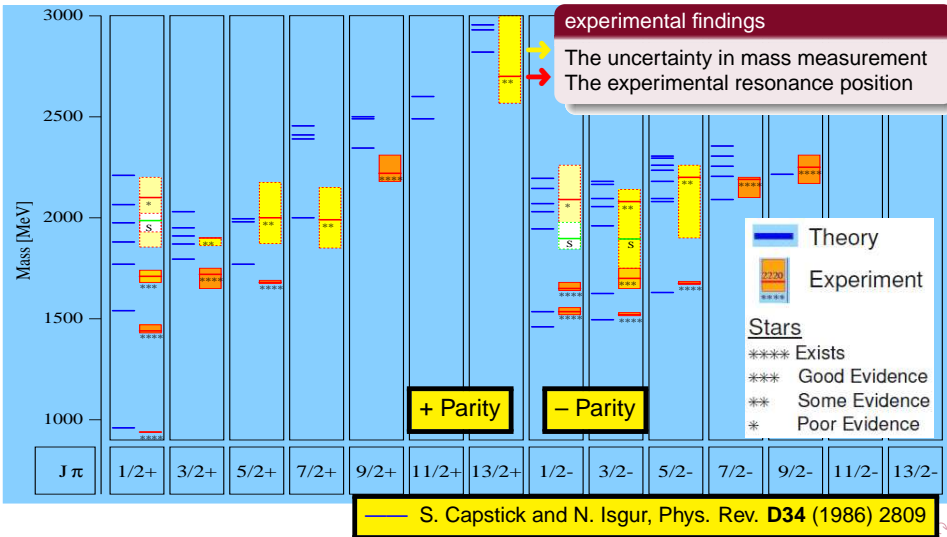
- Hadrons are composed of quarks bound by the strong interaction.
 - Baryon: qqq
 - Meson: $q\bar{q}$
- Quantum Chromodynamics (QCD)
 - QCD is the theory of strong interactions; the strong force describes the interactions of quarks and gluons making up hadrons.
- Strong interaction processes **at larger distances and at small (soft) momentum transfers** belong to the realm of non-perturbative QCD.
 - **Constituent quark models** are the most successful models for making predictions about **the properties of baryon resonances** in the non-perturbative region of QCD.

The N^* Program in JLab

→ The study of **the properties of baryon resonances**

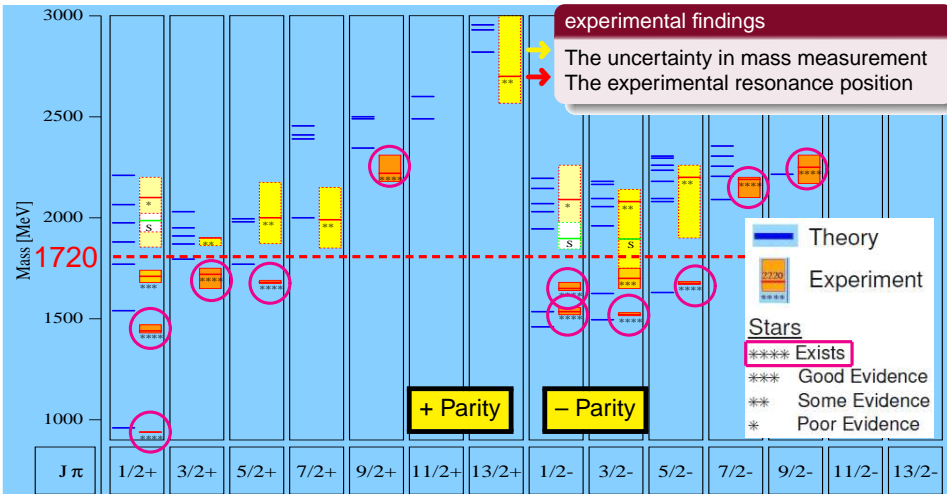
The spectrum of N^* resonances

Constituent quark model: Gluon-exchange model



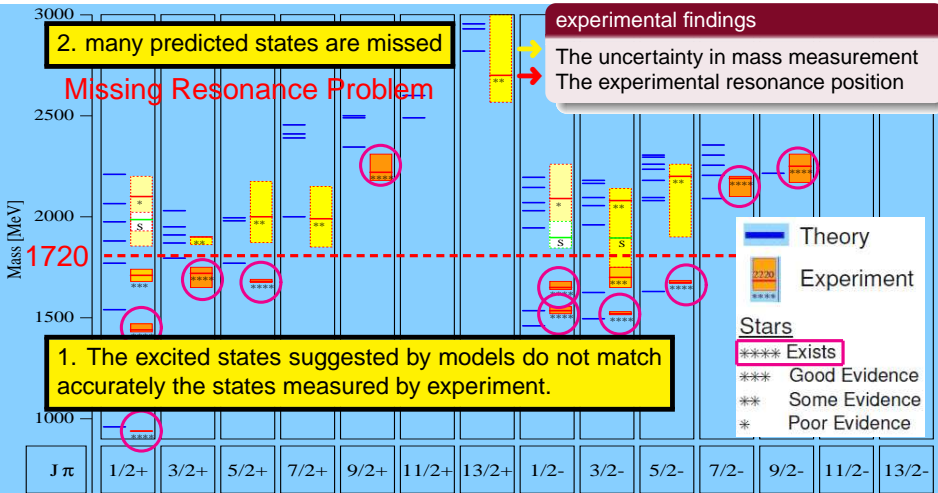
The spectrum of N^* resonances

Constituent quark model: N^* resonances (Isospin $\frac{1}{2}$)



The spectrum of N^* resonances

Constituent quark model: N^* resonances (Isospin $\frac{1}{2}$)

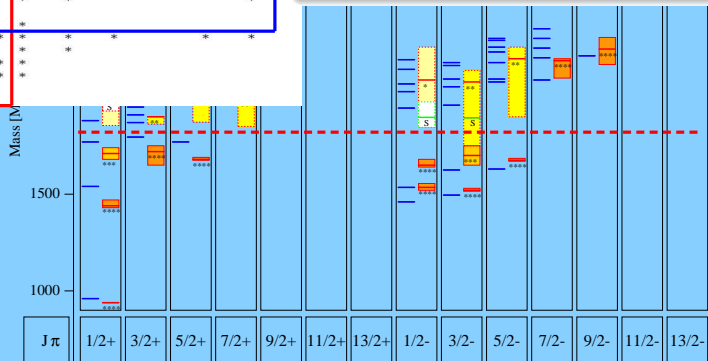


The spectrum of N^* resonances

Particle	L_{2I-2J} status	Overall status	Status as seen in —							
			$N\pi$	$N\eta$	ΔK	ΣK	$\Delta\pi$	$N\rho$	$N\gamma$	
$N(939)$	P_{11}	****								
$N(1440)$	P_{11}	****	****	*			***	*	***	
$N(1520)$	D_{13}	****	****	***			***	***	***	
$N(1535)$	S_{11}	****	****	****			*	**	***	
$N(1650)$	S_{11}	****	****	*	***	**	***	**	***	
$N(1675)$	D_{15}	****	****	*	*		****	*	***	
$N(1680)$	F_{15}	****	****	*			****	****	***	
$N(1700)$	D_{13}	***	***	**	**	*	**	*	***	
$N(1710)$	P_{11}	***	***	**	**	*	**	*	***	
$N(1720)$	P_{13}	****	****	*	**	*	*	**	***	
$N(1900)$	F_{13}	**	**				*			
$N(1990)$	F_{17}	**	**	*	*	*		*		
$N(2000)$	F_{15}	**	**	*	*	*	*	**		
$N(2080)$	D_{13}	**	**	*	*	*		*		
$N(2090)$	S_{11}	*	*						*	
$N(2100)$	F_{11}	*	*	*						
$N(2190)$	G_{17}	****	****	*	*	*	*	*	*	
$N(2200)$	D_{15}	***	**	*	*					
$N(2220)$	H_{19}	****	****	*						
$N(2250)$	G_{19}	****	****	*						
$N(2600)$	I_{113}	***	***							
$N(2700)$	K_{113}	**	**							

The status of the N resonances

- Nearly all existing data result from $N\pi$ channel.
 - ◇ If the missing resonances did not couple to $N\pi$, they would not have been discovered.
- Photoproduction data accumulated mainly cover masses up to 1.7 GeV.
- Missing resonances problem appears above 1.7 GeV.
- The CLAS-FROST data used in this analysis covers the region above $W \sim 1.7$ GeV.



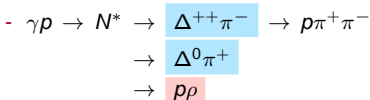
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$N(2700)$	K_{113}	**	**	*	*	*		*	*

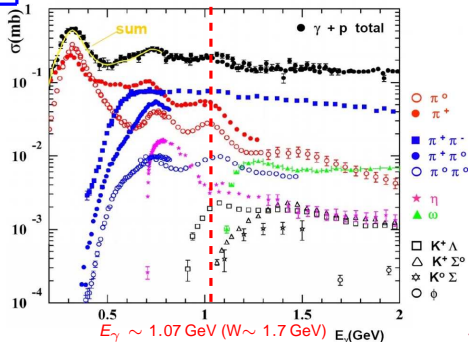
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◇ The decay channel of $\pi^+\pi^-$ photoproduction :

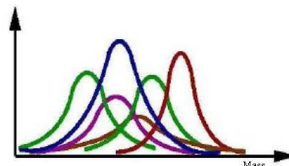


◇ The biggest cross section contribution is from $\pi^+\pi^-$ photoproduction above $W \sim 1.7$ GeV.



Why is $\pi^+\pi^-$ photoproduction needed?

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$N(1700)$	D_{13}	***	*** **	** *	*	** *		***
$N(1710)$	P_{11}	***	*** **	** *	*	** *		***
$N(1720)$	P_{13}	****	**** **	** *	*	* **		***
$N(1900)$	T_{13}	**	**					*
$N(1990)$	F_{17}	**	** *	*	*			*
$N(2000)$	F_{15}	**	** *	*	*	*	**	*
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$N(2700)$	K_{113}	**	**					



Polarization observables

- The excited states are found as broadly overlapping resonances.
- The **polarization observables** can isolate single resonances from other interference terms.
 - **polarization observables** are very sensitive to small resonant contributions.

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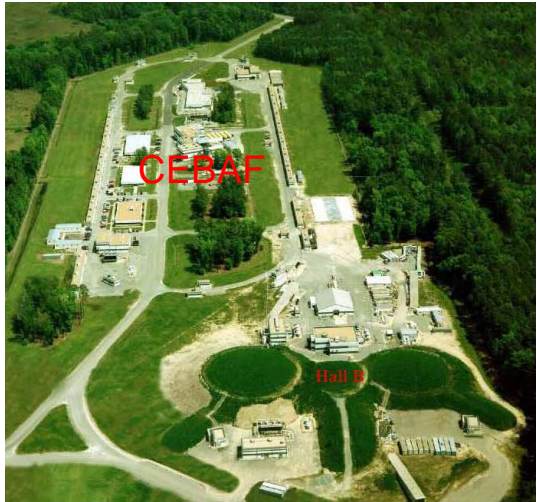
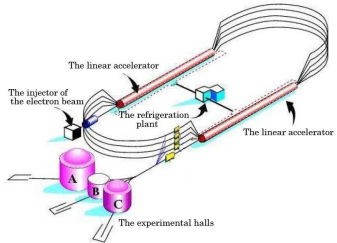
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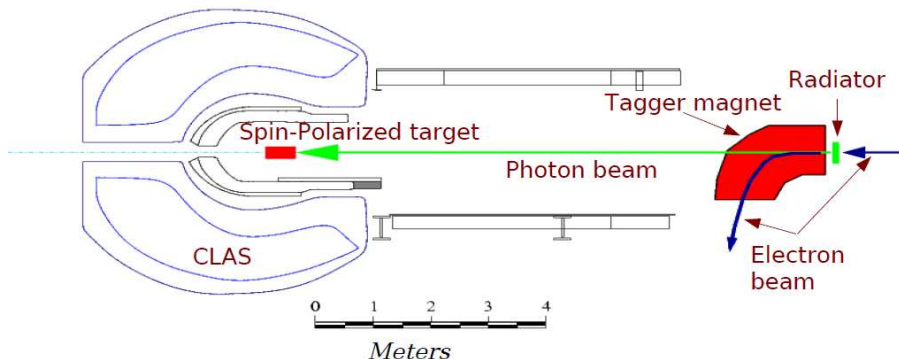
Jefferson Laboratory in Newport News, VA



- The continuous electron beam accelerator facility (CEBAF) can deliver a continuous electron beam up to **6 GeV**.

Experimental devices for the FROST experiment

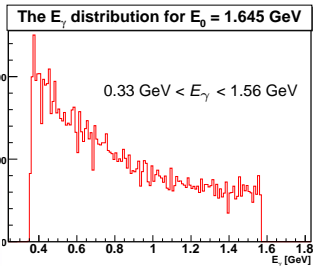
- The broad-range photon tagging system
- The FROzen Spin Target (FROST)
- The CEBAF Large Acceptance Spectrometer (CLAS)



The tagging system in Hall B

JLAB Hall B bremsstrahlung photon tagger

- $E_\gamma = 20\text{-}95\%$ of E_0
- E_γ up to ~ 5.5 GeV

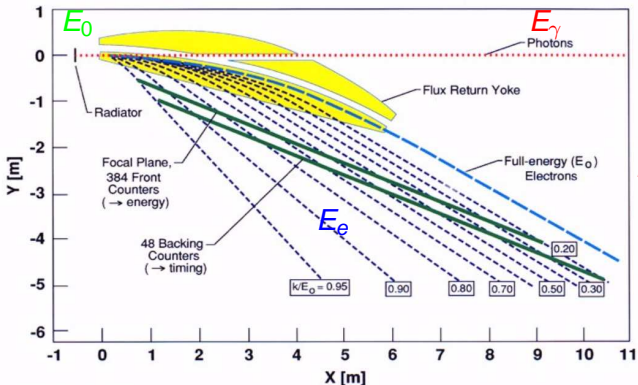


$$E_\gamma = E_0 - E_e$$

E_γ : The energy of the emitted photon

E_0 : The energy of the incident electron

E_e : the energy of the outgoing electron



The tagging system in Hall B

JLAB Hall B bremsstrahlung photon tagger

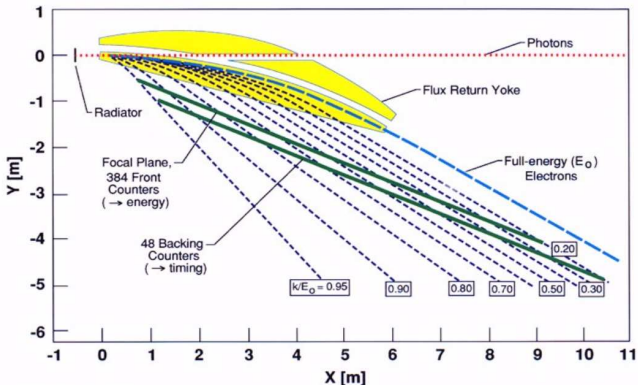
- Circularly polarized photon beam
- Linearly polarized photon beam

amorphous radiator

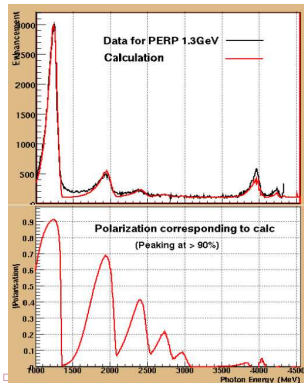
longitudinally polarized electron beam

oriented diamod radiator

unpolarized electron beam



linearly polarized beam



CEBAF Large Acceptance Spectrometer (CLAS)



target + start counter

Drift chambers

argon/CO₂ gas, 35,000 cells



Time-of-flight counters

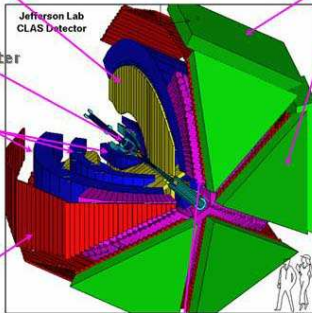
plastic scintillators, 684 photomultipliers

Torus magnet

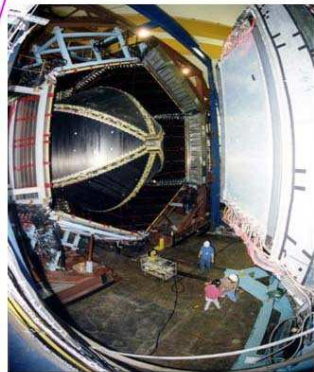
6 superconducting coils

Electromagnetic calorimeters

Lead/scintillator, 1296 photomultipliers

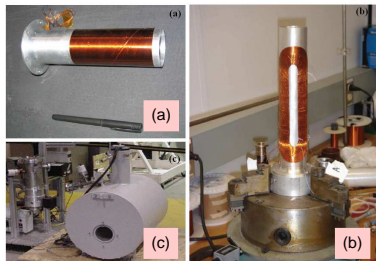


Gas Cherenkov counters



The FROzen-Spin Target (FROST)

1 High magnetic field (5 T)



(a) The longitudinal holding magnet. (0.56 T)
(g9a : Nov. 2007 - Feb. 2008)

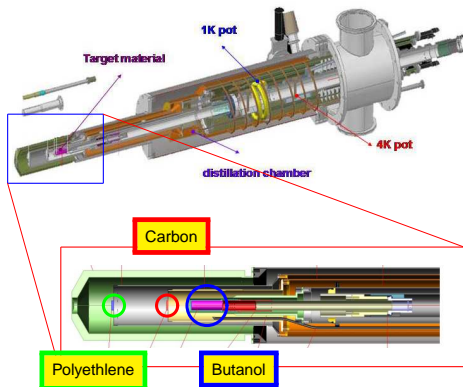
- ◇ Average target polarization
~ 82 % (+Pol) and 85 % (-Pol)

(b) The transversal holding magnet. (0.50 T)
(g9b : March 2010 - August 2010)

(c) The polarizing magnet. (5 T)

2 Low temperature

28 mK (w/o beam) and 30mK (w/ beam)



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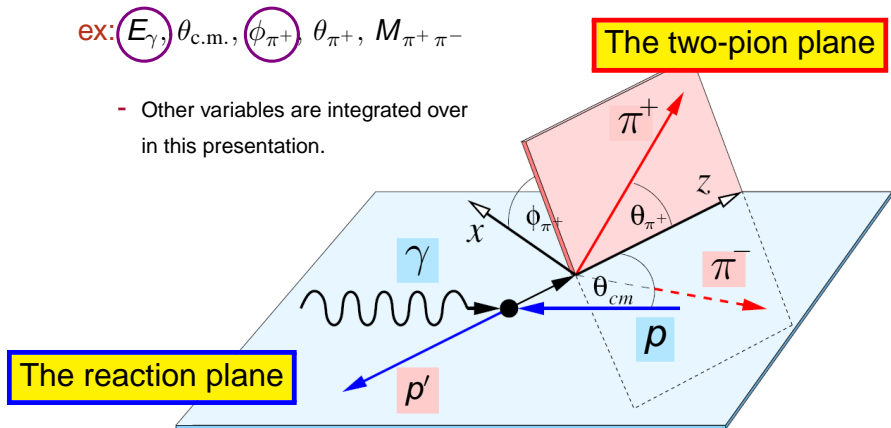
5 Summary

Photoproduction of $\pi^+\pi^-$ off the proton: Kinematics

- The $\pi^+\pi^-$ photoproduction requires 5 independent variables.

ex: E_γ , $\theta_{\text{c.m.}}$, ϕ_{π^+} , θ_{π^+} , $M_{\pi^+\pi^-}$

- Other variables are integrated over in this presentation.



The differential cross section for $\gamma p \rightarrow p\pi^+\pi^-$

The differential cross section for $\gamma p \rightarrow p\pi^+\pi^-$

(without measuring the polarization of the recoiling nucleon)

$$\frac{d\sigma}{dx_i} = \sigma_0 \left\{ (1 + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}) + \delta_{\odot} (\mathbf{I}^{\odot} + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}^{\odot}) \right. \\ \left. + \delta_I [\sin 2\beta (\mathbf{I}^{\mathbf{s}} + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}^{\mathbf{s}}) + \cos 2\beta (\mathbf{I}^{\mathbf{c}} + \vec{\Lambda}_i \cdot \vec{\mathbf{P}}^{\mathbf{c}})] \right\}$$

- σ_0 : The unpolarized cross section
- β : The angle between the direction of polarization and the x-axis
- x_i : The kinematic variables
- δ_{\odot}, I : The degree of polarizat^on of the photon beam $\Rightarrow \delta_{\odot}$, and δ_I
- $\vec{\Lambda}_i$: The polarization of the initial nucleon $\Rightarrow (\Lambda_x, \Lambda_y, \Lambda_z)$
- $\mathbf{I}^{\odot}, \mathbf{s}, \mathbf{c}$: The observable arising from use of polarized photons $\Rightarrow \mathbf{I}^{\odot}, \mathbf{I}^{\mathbf{s}}, \mathbf{I}^{\mathbf{c}}$
- $\vec{\mathbf{P}}$: The polarization observable $\Rightarrow (\mathbf{P}_x, \mathbf{P}_y, \mathbf{P}_z)$ ($\mathbf{P}_x^{\odot}, \mathbf{P}_y^{\odot}, \mathbf{P}_z^{\odot}$) ($\mathbf{P}_x^{\mathbf{s}}, \mathbf{P}_y^{\mathbf{s}}, \mathbf{P}_z^{\mathbf{s}}$) ($\mathbf{P}_x^{\mathbf{c}}, \mathbf{P}_y^{\mathbf{c}}, \mathbf{P}_z^{\mathbf{c}}$)

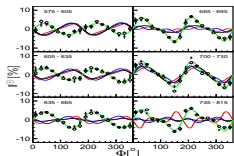
15 Observables

Previous measurements

The data used for this analysis :

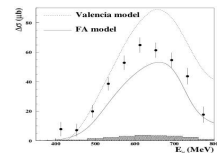
1. circularly-polarized beam
2. longitudinally-polarized target

$$\frac{d\sigma}{dx_i} = \sigma_0 \left\{ (1 + \Lambda_z \cdot \mathbf{P}_z) + \delta_{\odot} (\mathbf{I}^{\odot} + \Lambda_z \cdot \mathbf{P}_z^{\odot}) \right\}$$



\mathbf{I}^{\odot} : Phys.Rev.Lett. 103, 052002

(2009, Crystal Ball at MAMI, TAPS, and A2 Collaboration)

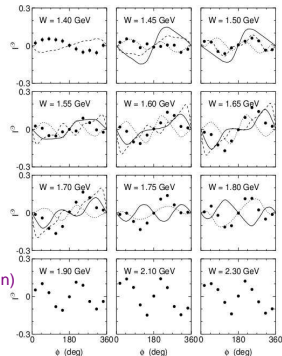


\mathbf{P}_z^{\odot} : Eur.Phys.J. A 34, 11-21 (2007, GDH Collaboration)

- The helicity-dependent total cross-section difference

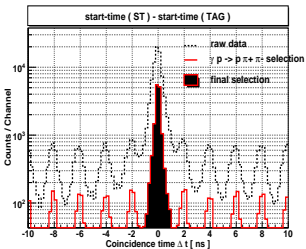
$$\Delta\sigma = (\sigma_{3/2} - \sigma_{1/2})$$

\mathbf{I}^{\odot} : Phys.Rev.Lett. 95, 162003 (2005, CLAS Collaboration)

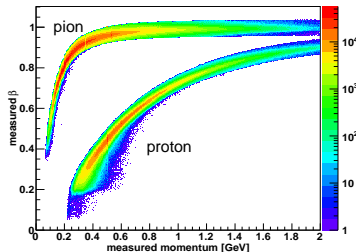


Basic event selection

photon selection



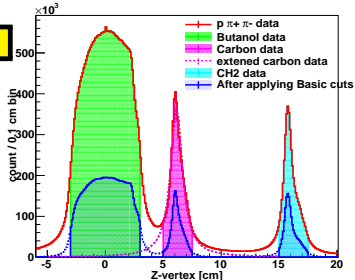
proton and pion selection



Basic Cuts

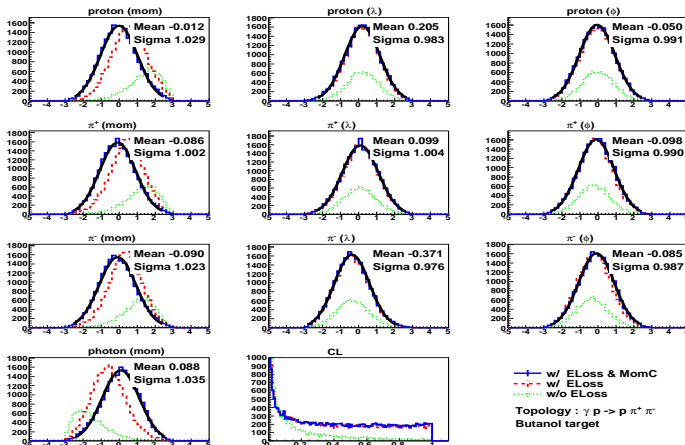
- photon selection
: $|\Delta t| < 1.2$ ns
- proton selection
: $|\Delta\beta| < 0.032$
- pion selection
: $|\Delta\beta| < 0.044$
- vertex cut (Butanol)
: $|Z_{\text{vertex}}| < 3$ cm
- accidental cut
: one photon selection
- confidence-level cut
: CL-cut $> 5\%$

vertex cut



Basic event selection

● The kinematic fitting



● Basic Cuts

- photon selection : $|\Delta t| < 1.2 \text{ ns}$
- proton selection : $|\Delta\beta| < 0.032$
- pion selection : $|\Delta\beta| < 0.044$
- vertex cut (Butanol) : $|Z_{\text{vertex}}| < 3 \text{ cm}$
- accidental cut : one photon selection
- confidence-level cut : CL-cut $> 5\%$

● Corrections

- Energy-loss correction
- Photon-energy correction
- Momentum correction

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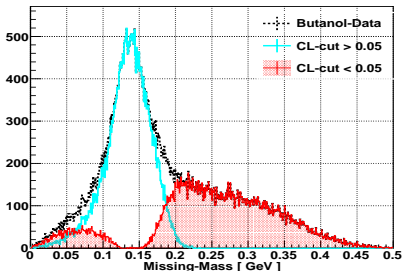
5 Summary

Polarization observable I

Polarization observable I^\odot

$$I^\odot(\mathbf{W}, \phi_{\pi^+}) = \frac{1}{\bar{\delta}_\odot(\mathbf{W})} \frac{\left\{ N(\rightarrow; \mathbf{W}, \phi_{\pi^+})_{beam} - N(\leftarrow; \mathbf{W}, \phi_{\pi^+})_{beam} \right\}}{\left\{ N(\rightarrow; \mathbf{W}, \phi_{\pi^+})_{beam} + N(\leftarrow; \mathbf{W}, \phi_{\pi^+})_{beam} \right\}}$$

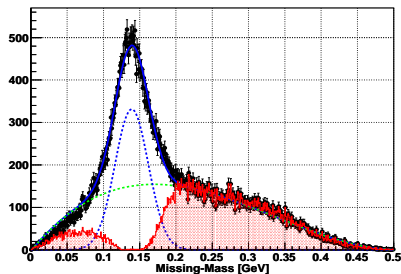
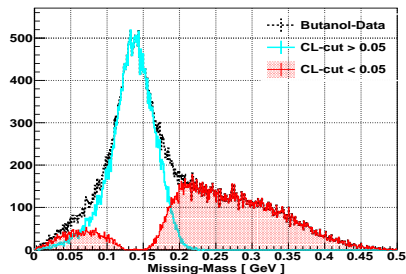
- ◇ $\bar{\delta}_\odot(\mathbf{W})$: The average degree of the photon beam polarizations.
- ◇ $\rightarrow (\leftarrow)$: the direction of the beam polarization is parallel (anti-parallel) to the beam.
- ◇ Beam-helicity asymmetry for the unpolarized target and circularly-polarized photon beam.



example :

- Topology : $\gamma p \rightarrow p\pi^+(\pi^-)$.
- W : 1.60 GeV.
- $\theta_{c.m.}, \phi_{\pi^+}, \theta_{\pi^+}, M_{\pi^+\pi^-}$ are integrated over.
- **Using the 5 % Confidence Level Cut**
- There is still an effect of background events.

The background effect in Beam-Helicity Asymmetry I

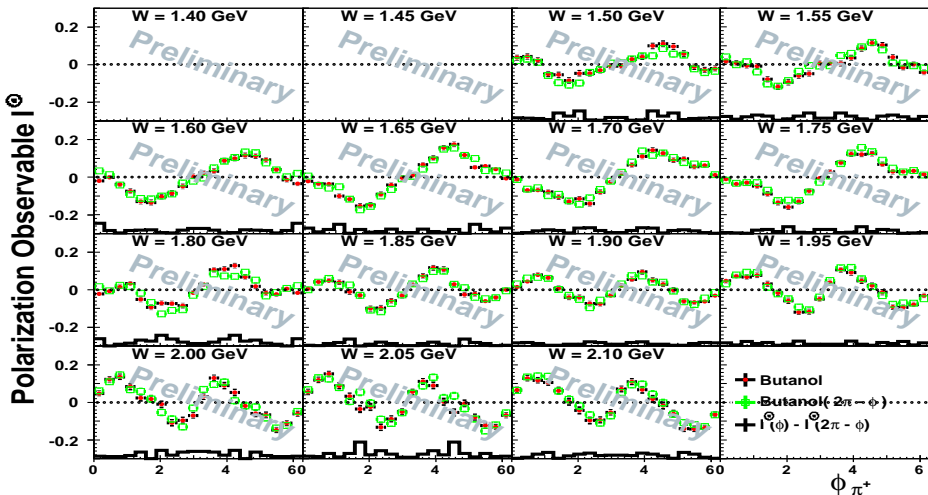


● Fitting function : Gaussian + Chebyshev pol.

- Butanol data are composed of
 - free-proton data
 - bound-nucleon data & background data
- After applying CL-cut, there are still bound-nucleon and background events.
- These bound-nucleon and background events have a small influence on the beam asymmetry.

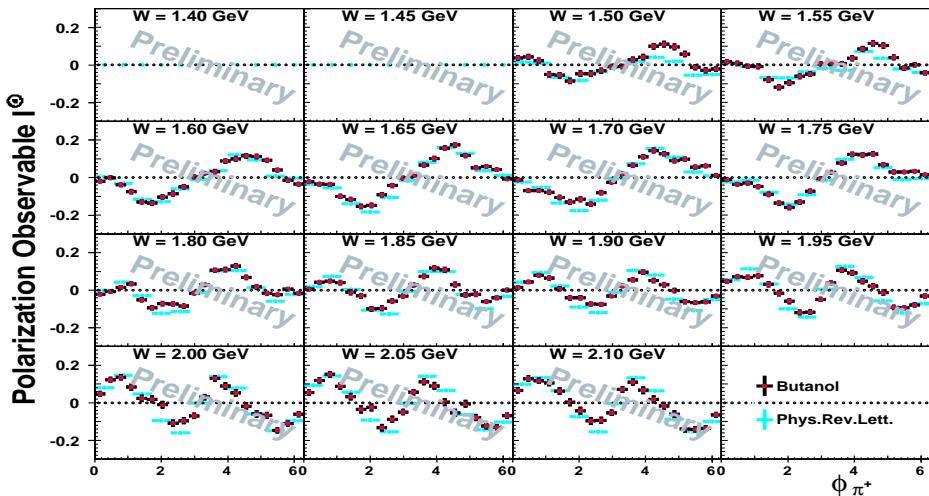
Check the symmetry of polarization observable I^\odot

- Kinematic variables $\theta_{c.m.}$, θ_{π^+} , $M_{\pi^+\pi^-}$ are integrated over.
- Butanol($2\pi - \phi$): $-I^\odot(2\pi - \phi)$



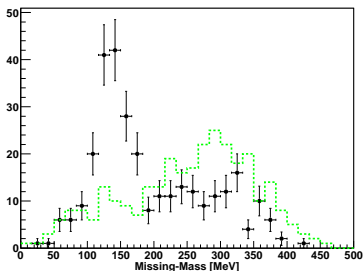
Beam-Helicity Asymmetry I^{\odot} with the published data

I^{\odot} : Phys.Rev.Lett. 95, 162003 (2005, CLAS Collaboration)



Q-factor method

- The Q-factor method is used to subtract background :
 - The Q-factor is an event-based quality factor which denotes the probability that each seed event is a signal event.
- Find the input for the Q-factor method :
 - Step 1) The 300 nearest neighbors from the butanol seed event are selected. (in black)
 - Step 2) A seed event in the carbon sample is chosen which is kinematically closest to the butanol seed event.
 - Step 3) The 300 nearest neighbors for the carbon seed event are selected. (in green)



- The distance between event a and b, $D_{a,b}^2$:

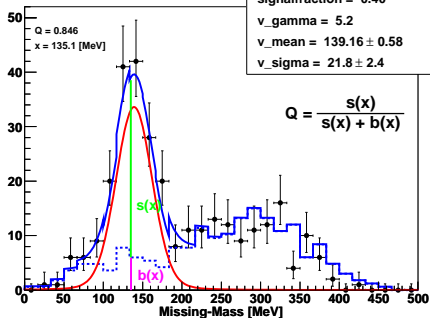
$$D_{a,b}^2 = \sum_{i=1}^4 \left(\frac{\Gamma_i^a - \Gamma_i^b}{\Delta_i} \right)^2$$

Γ_i : W , $\theta_{\text{c.m.}}^{\text{proton}}$, ϕ_{π^+} , θ_{π^+}

Δ_i : the maximum range of the kinematic variable Γ_i

Q-factor method

For each event,



The total function (in blue) is:

$$f(x) = N \cdot [f_s \cdot S(x) - (1 - f_s) \cdot B(x)]$$

→ There are four parameters decided.

- 1 $S(x)$: the Voigt function (Γ , *mean*, and σ)
- 2 $B(x)$: the background function
 - g9b carbon distribution (in green)
- 3 N : a normalization constant
- 4 f_s : the signal fraction with $[0,1]$

→ event-based scale factor, s is the parameter to scale the carbon distribution.

$$Q = \frac{s(x)}{s(x) + b(x)}$$

- 1 x : the missing mass of the seed event
- 2 $s(x)$: $f_s \cdot S(x)$
- 3 $b(x)$: $(1 - f_s) \cdot B(x)$

$$s = \frac{(1-f_s) \cdot (\# \text{ of nearest butanol events})}{(\# \text{ of nearest carbon events})} = 1 - f_s$$

Q-factor method

● The order to decide four parameters is:

Step1 Variables for the Voigt function are decided.

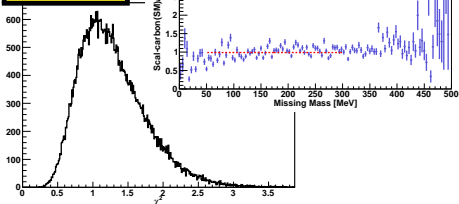
- *mean* : [139, 140] MeV
- σ : [5, 200] MeV
- Γ : the small fixed value from a similar fit to the fully integrated distribution.

Step2 event-based scale factor, s ($= 1 - f_s$) are decided by the following two plots:

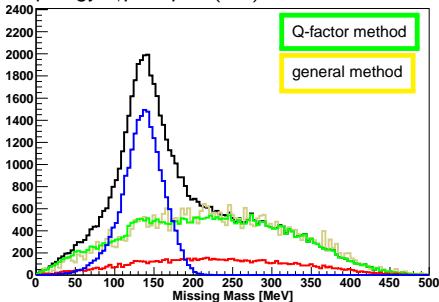
general-method/Q-factor

χ^2 / ndf	323 / 62
Prob	5.962e-37
p0	0.9881 ± 0.0086

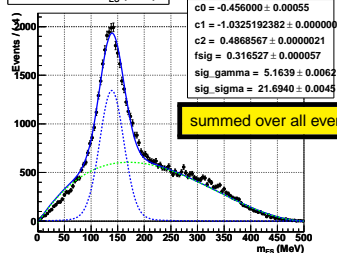
χ^2 distribution



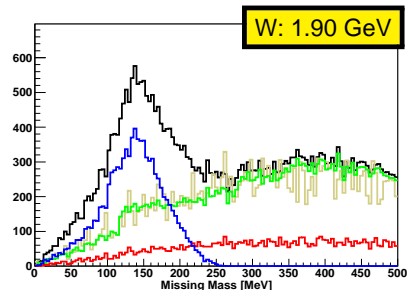
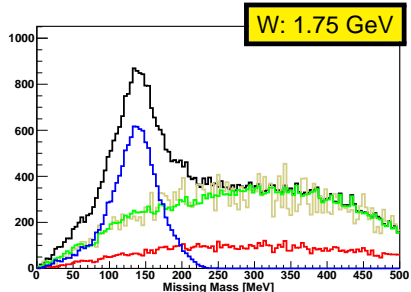
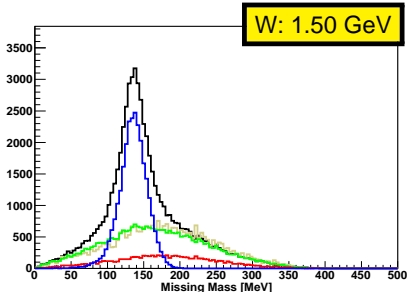
Topology: $\gamma p \rightarrow p\pi^+(\pi^-)$ and W: 1.6 GeV



A RooPlot of "m_{ES} (MeV)"



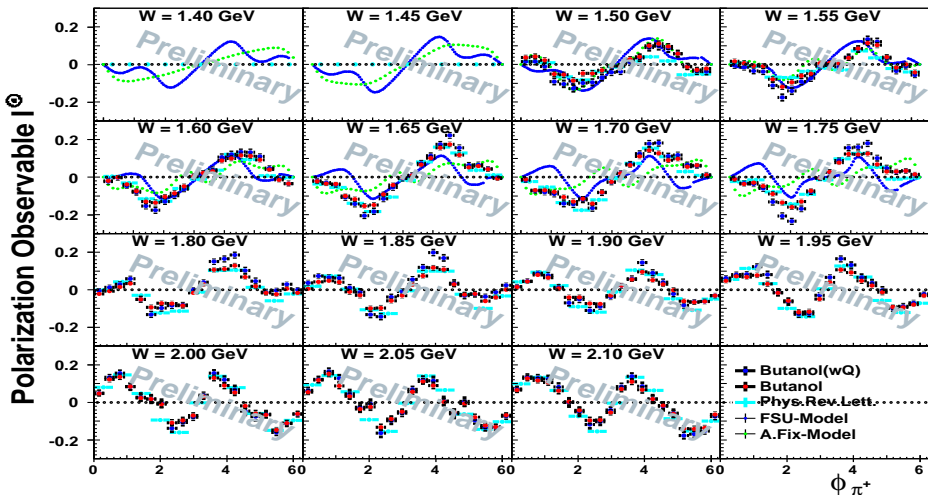
Q-factor method



- ◇ Topology: $\gamma p \rightarrow p\pi^+(\pi^-)$.
- ◇ The Q-factor method is used as an **event-based dilution factor** to subtract background.
- ◇ From the butanol (C_4H_9OH) data, the free proton data is extracted on an event-by-event basis. **No overall dilution factor is necessary.**

Beam-Helicity Asymmetry I^{\odot} with models

- FSU-model calculated by Winston Roberts
- A.Fix-model calculated by Alexander Fix (Eur. Phys. J. A 25, 115-135, 2005)

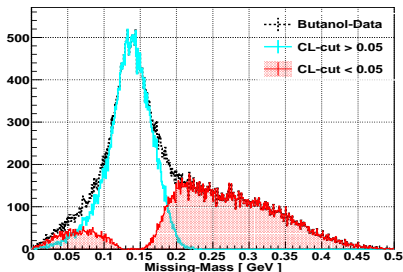


Polarization observable P_z

Polarization observable P_z

$$P_z(\mathbf{W}, \phi_{\pi^+}) = \frac{1}{\bar{\Lambda}_z(\mathbf{W})} \frac{\left\{ N(\Rightarrow; \mathbf{W}, \phi_{\pi^+})_{target} - N(\Leftarrow; \mathbf{W}, \phi_{\pi^+})_{target} \right\}}{\left\{ N(\Rightarrow; \mathbf{W}, \phi_{\pi^+})_{target} + N(\Leftarrow; \mathbf{W}, \phi_{\pi^+})_{target} \right\}}$$

- ◇ $\bar{\Lambda}_z(\mathbf{W})$: The average degree of the target polarizations.
- ◇ \Rightarrow (\Leftarrow) : the direction of the target polarization is parallel (anti-parallel) to the beam.
- ◇ Target asymmetry for the linearly-polarized target and unpolarized photon beam.

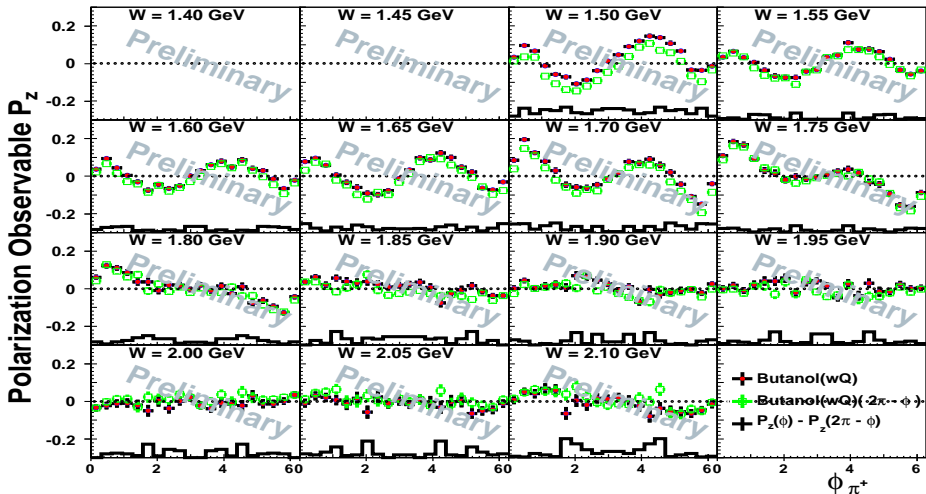


example :

- Topology : $\gamma p \rightarrow p\pi^+(\pi^-)$.
- W : 1.60 GeV.
- $\theta_{c.m.}, \phi_{\pi^+}, \theta_{\pi^+}, M_{\pi^+\pi^-}$ are integrated over.
- Using the 5 % Confidence Level Cut & Q-factor method

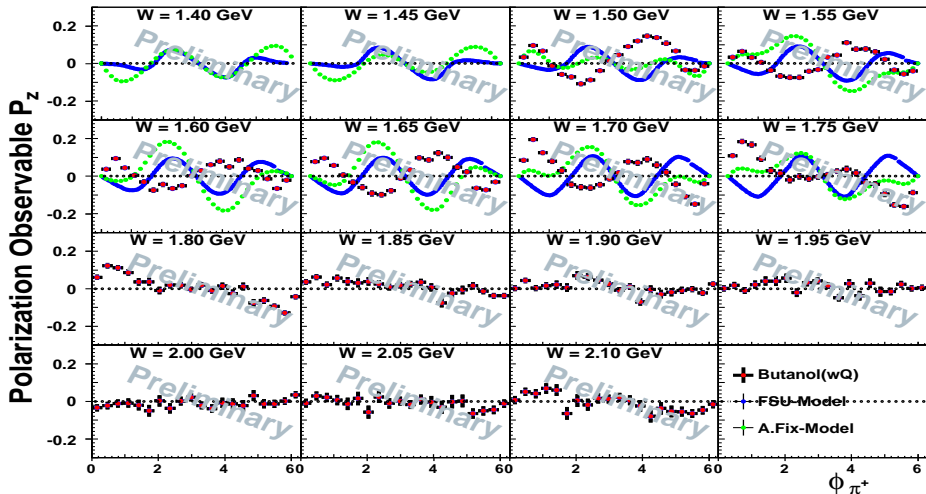
Check the symmetry of polarization observable P_z

- Kinematic variables $\theta_{c.m.}$, θ_{π^+} , $M_{\pi^+\pi^-}$ are integrated over.
- Butanol(wQ) ($2\pi - \phi$) : $-P_z(2\pi - \phi)$



Target Asymmetry P_z with models

- FSU-model calculated by Winston Roberts
- A.Fix-model calculated by Alexander Fix (Eur. Phys. J. A 25, 115-135, 2005)

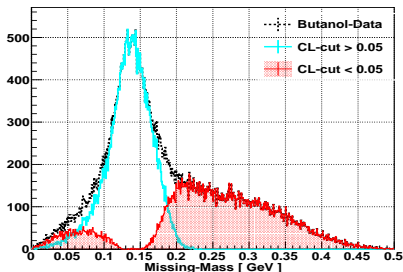


Polarization observable \mathbf{P}_z^\odot

Polarization observable P_z^\odot

$$P_z^\odot(\mathbf{W}, \phi_{\pi^+}) = \frac{1}{\bar{\Lambda}_z(\mathbf{W}) \cdot \bar{\delta}_\odot} \frac{\left\{ N(\mathbf{W}, \phi_{\pi^+})_{3/2} - N(\mathbf{W}, \phi_{\pi^+})_{1/2} \right\}}{\left\{ N(\mathbf{W}, \phi_{\pi^+})_{3/2} + N(\mathbf{W}, \phi_{\pi^+})_{1/2} \right\}}$$

- ◇ $\bar{\Lambda}_z(\mathbf{W})$: The average degree of the target polarizations.
- ◇ $\bar{\delta}_\odot(\mathbf{W})$: The average degree of the photon beam polarizations.
- ◇ Helicity Difference for the linearly-polarized target and circularly-polarized photon beam.

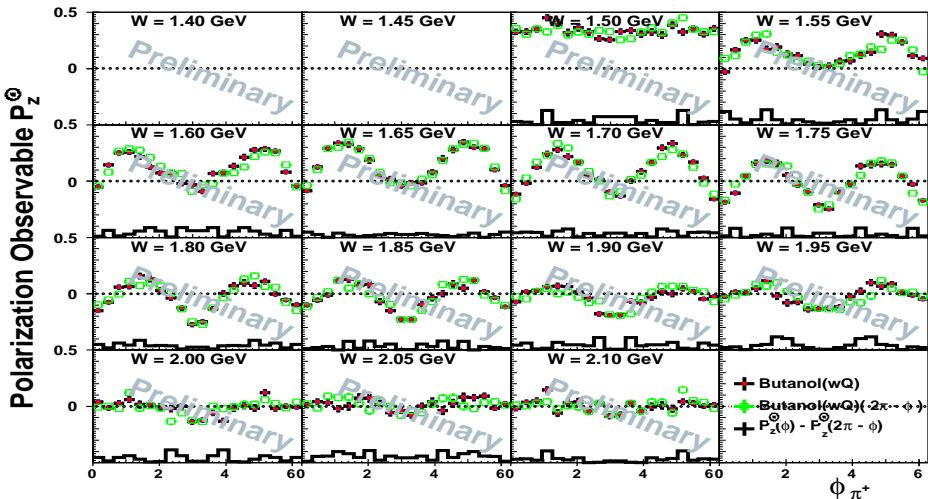


example :

- Topology : $\gamma p \rightarrow p\pi^+(\pi^-)$.
- W : 1.60 GeV.
- $\theta_{\text{c.m.}}, \phi_{\pi^+}, \theta_{\pi^+}, M_{\pi^+\pi^-}$ are integrated over.
- Using the 5 % Confidence Level Cut & Q-factor method

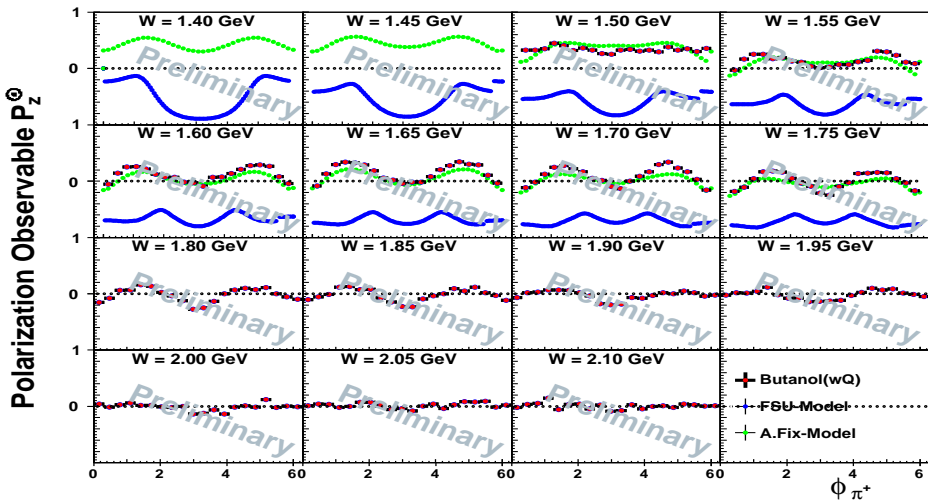
Check the symmetry of polarization observable P_z^\odot

- Kinematic variables $\theta_{c.m.}$, θ_{π^+} , $M_{\pi^+\pi^-}$ are integrated over.
- Butanol(wQ) $(2\pi - \phi) : P_z^\odot(2\pi - \phi)$



Helicity Difference P_z^\odot

- FSU-model calculated by Winston Roberts
- A.Fix-model calculated by Alexander Fix (Eur. Phys. J. A 25, 115-135, 2005)



Outline

1 Introduction

- Baryon Spectroscopy
- Why is $\pi^+\pi^-$ photoproduction needed ?

2 FROST Experiment

- Jefferson Laboratory in Newport News, VA
- Experimental devices for the FROST experiment

3 Data Analysis

- Kinematic variables
- Previous measurements
- Basic event selection

4 Preliminary Results

- Polarization Observable I^{\odot}
- Q-factor method : Event-based background subtraction
- Polarization Observable P_z
- Polarization Observable P_z^{\odot}

5 Summary

Summary

- ◇ Polarization Observable I^{\odot} using the FROST data is in good agreement with the previously published CLAS data.
- ◇ Polarization Observables P_z and P_z^{\odot} will be first-time measurements for double-pion photoproduction.
- ◇ The comparison between results from the butanol target and the butanol weighted by the Q-factor (event-based background subtraction) shows that the Q-factor method is very useful tool to extract the polarization observables.
- ◇ The comparison with model predictions provides the basis for significant improvements for the models.

Korea Multi-Purpose Accelerator Complex

Proton Accelerator Research Center



① Accelerator & Klystron Building

② Experimental Hall

③ Ion Facility Building

④ Utility Building

⑤ Substation

⑥ Cooling Tower

⑦ Water Storages

⑧ Main Office Building

⑨ Regional Cooperation Building

⑩ Dormitory

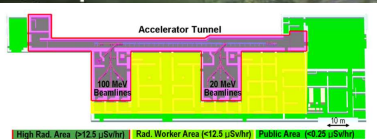
⑪ Information Center

Korea Multi-Purpose Accelerator Complex

Proton Accelerator Research Center



① Accelerator & Klystron Building ② Experimental Hall



❖ User Program Development (2003~)

Research Fields	Sub-categories
Nano Science & Technology	Ion-cutting, Nano-particle shaping & fabrication, Carbon nano-tube, nano-wire, Nano-machining
Information Technology	High power semiconductor, Semiconductor manufacturing R&D, Proton lithography
Space Technology	Radiation hard electronic device, Radiation effect on materials
Bio-Technology	Mutation of plants & micro-organisms
Medical research	Low energy proton therapy study, Biocompatible material, Biological radiation effects, New RI production R&D
Materials Science	Proton irradiation effects with various materials Gemstone coloration
Energy & Environment	New microorganism development for bio fuel (ethanol, butanol), New materials for fuel cell ; electrolyte, nano catalyst, organic solar cell
Nuclear & Particle Physics	Detector R&D, Nuclear data, TLA (Thin Layer Activation)

Back up



Quark

Three Generations
of Matter (Fermions)

	I	II	III	
mass→	3 MeV	1.24 GeV	172.5 GeV	0
charge→	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin→	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name→	u up	c charm	t top	γ photon
Quarks	6 MeV	95 MeV	4.2 GeV	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	d down	s strange	b bottom	g gluon
<2 eV	<0.19 MeV	<18.2 MeV	90.2 GeV	
0	0	0	0	
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z weak force	
0.511 MeV	106 MeV	1.78 GeV	80.4 GeV	
-1	-1	-1	±1	
$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
e electron	μ muon	τ tau	W weak force	

Bosons (Forces)

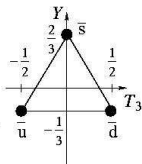
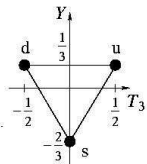
- electric charge $Q : I_z + \frac{\beta + S + C + B + T}{2}$

ex:

- $Q(u) = \frac{1}{2} + \frac{1/3+0+0+0+0}{2} = +\frac{2}{3}$
- $Q(d) = -\frac{1}{2} + \frac{1/3+0+0+0+0}{2} = -\frac{1}{3}$
- $Q(s) = 0 + \frac{1/3-1+0+0+0}{2} = -\frac{1}{3}$
- $Q(c) = 0 + \frac{1/3+0+1+0+0}{2} = +\frac{2}{3}$
- $Q(b) = 0 + \frac{1/3+0+0-1+0}{2} = -\frac{1}{3}$
- $Q(t) = 0 + \frac{1/3+0+0+0+1}{2} = +\frac{2}{3}$

	d	u	s	c	b	t
J - total angular momentum	+1/2	+1/2	+1/2	+1/2	+1/2	+1/2
Q - electric charge	-1/3	+2/3	-1/3	+2/3	-1/3	+2/3
I - isospin	1/2	1/2	0	0	0	0
I_z - isospin z-component	-1/2	+1/2	0	0	0	0
β - baryon number	+1/3	+1/3	+1/3	+1/3	+1/3	+1/3
S - strangeness	0	0	-1	0	0	0
C - charm	0	0	0	+1	0	0
B - bottomness	0	0	0	0	-1	0
T - topness	0	0	0	0	0	+1

Hadron : SU(3)



- ◇ **Y** : the hypercharge = β (baryon number) + **S**(strangeness)
- ◇ **T₃** : the isospin z-component
- ◇ Young Tableaux for SU(n) : $\dim \text{YT} = N/D$

Meson

octet

singlet

$$\bar{\mathbf{3}} \otimes \mathbf{3} = \mathbf{8} \oplus \mathbf{1}$$

Baryon

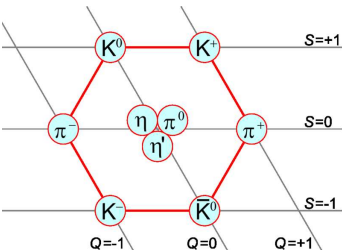
decuplet

octet

singlet

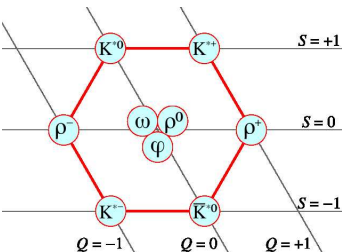
$$(\mathbf{3} \otimes \mathbf{3}) \otimes \mathbf{3} = (\mathbf{6} \oplus \mathbf{3}) \otimes \mathbf{3} = \mathbf{10} \oplus \mathbf{8} \oplus \mathbf{8} \oplus \mathbf{1}$$

Meson



- ◆ The $J^P = 0^-$ pseudoscalar meson nonet
- ◆ $n^{2s+1} l_J J^{PC} : 1^1 S_0 0^{-+}$
 - $n = 1, l = 0, s = 0,$ and $J = 0$

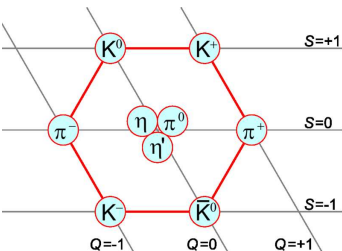
$l=1$	$l=1/2$	$l=0$	$l=0$
$\pi^+ : u\bar{d}$ ($Q=1:S=0$)	$K^+ : u\bar{s}$ ($Q=1:S=1$)	$\frac{\eta}{\sqrt{6}}$ ($Q=0:S=0$)	$\frac{\eta' (958)}{\sqrt{3}}$ ($Q=0:S=0$)
$\pi^0 : \frac{1}{\sqrt{2}}(d\bar{d} - u\bar{u})$ ($Q=0:S=0$)	$K^0 : d\bar{s}$ ($Q=0:S=1$) $K^0 : d\bar{s}$ ($Q=0:S=-1$)		
$\pi^- : \bar{u}d$ ($Q=-1:S=0$)	$K^- : \bar{u}s$ ($Q=-1:S=-1$)		



- ◆ The $J^P = 1^-$ vector meson nonet
- ◆ $n^{2s+1} l_J J^{PC} : 1^3 S_1 1^{-+}$
 - $n = 1, l = 0, s = 1,$ and $J = 1$

$l=1$	$l=1/2$	$l=0$	$l=0$
$\rho^+ : u\bar{d}$ ($Q=1:S=0$)	$K^{*+} : u\bar{s}$ ($Q=1:S=1$)	$\phi(1020)$ $s\bar{s}$ ($Q=0:S=0$)	$\frac{\omega(782)}{\sqrt{2}}$ ($Q=0:S=0$)
$\rho^0 : \frac{1}{\sqrt{2}}(d\bar{d} - u\bar{u})$ ($Q=0:S=0$)	$K^{*0} : d\bar{s}$ ($Q=0:S=1$) $\bar{K}^{*0} : \bar{d}s$ ($Q=0:S=-1$)		
$\rho^- : \bar{u}d$ ($Q=-1:S=0$)	$K^{*-} : \bar{u}s$ ($Q=-1:S=-1$)		

Meson



- ◇ The $J^P = 0^-$ pseudoscalar meson nonet

$$\pi^\pm (139.5) : I^G(J^P) = 1^-(0^-)$$

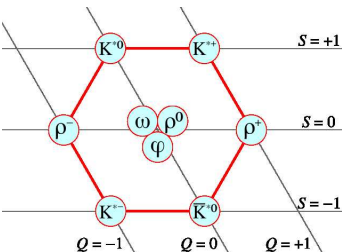
$$\pi^0 (135) : I^G(J^{PC}) = 1^-(0^{-+})$$

$$K^\pm (494) : I(J^P) = \frac{1}{2}(0^-)$$

$$K^0 (498) : I(J^P) = \frac{1}{2}(0^-)$$

$$\eta (548) : I^G(J^{PC}) = 0^+(0^{-+})$$

$$\eta' (958) : I^G(J^{PC}) = 0^+(0^{-+})$$



- ◇ The $J^P = 1^-$ vector meson nonet

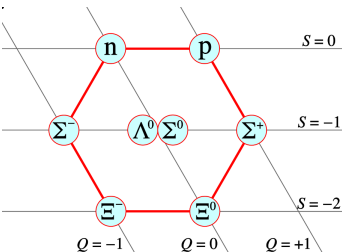
$$\rho(770) : I^G(J^P) = 1^+(1^{--})$$

$$K^*(892) : I(J^P) = \frac{1}{2}(1^-)$$

$$\omega(783) : I^G(J^{PC}) = 0^-(1^{--})$$

$$\phi(1020) : I^G(J^{PC}) = 0^-(1^{--})$$

Baryon



◇ The $J^P = \frac{1}{2}^+$ baryon octet

$$p(938) : I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$$

$$n(939) : I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$$

$$\Sigma^+(1189) : I(J^P) = 1(\frac{1}{2}^+)$$

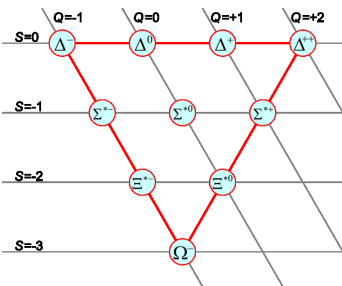
$$\Sigma^-(1197) : I(J^P) = 1(\frac{1}{2}^+)$$

$$\Lambda^0(1115) : I(J^P) = 0(\frac{1}{2}^+)$$

$$\Sigma^0(1192) : I(J^P) = 1(\frac{1}{2}^+)$$

$$\Xi^0(1315) : I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$$

$$\Xi^-(1322) : I(J^P) = \frac{1}{2}(\frac{1}{2}^+)$$



◇ The $J^P = \frac{3}{2}^+$ baryon decuplet

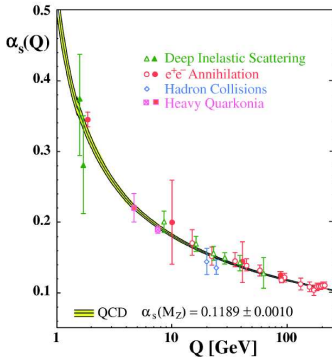
$$\Delta(1232) : I(J^P) = \frac{3}{2}(\frac{3}{2}^+)$$

$$\Delta^*(1385) : I(J^P) = 1(\frac{3}{2}^+)$$

$$\Xi^*(1530) : I(J^P) = \frac{1}{2}(\frac{3}{2}^+)$$

$$\Omega^-(1672) : I(J^P) = 0(\frac{3}{2}^+)$$

Quantum Chromodynamics (QCD)



- QCD is the theory of strong interactions; the strong force describes the interactions of quarks and gluons making up hadrons.

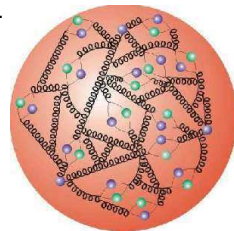
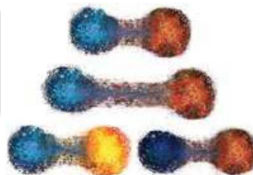
1. Asymptotic Freedom

When the exchange momentum Q is great, quarks and gluons interact very weakly.

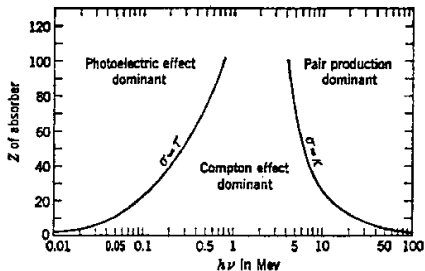
→ The inside of the proton at high energies, a "dense soup" of quarks and gluons.

2. Confinement

Force between quarks does not diminish as they are separated.



The γ -N interaction



● What happen in the γ -N interaction ?

- ◇ No interaction
- ◇ Photoelectric effect
- ◇ Compton scattering effect
- ◇ Pair production effect
- ◇ Hadronic interaction

◇ Photoelectric effect

- Photon undergoes an interaction with an absorber atom in which the photon completely disappears. In this place, an energetic photoelectron is ejected

◇ Compton scattering effect

- The compton effect is equivalent to inelastic collision of photon with electrons. Part of the photon energy is lost to the electron, and a less-energetic photon bounce off.

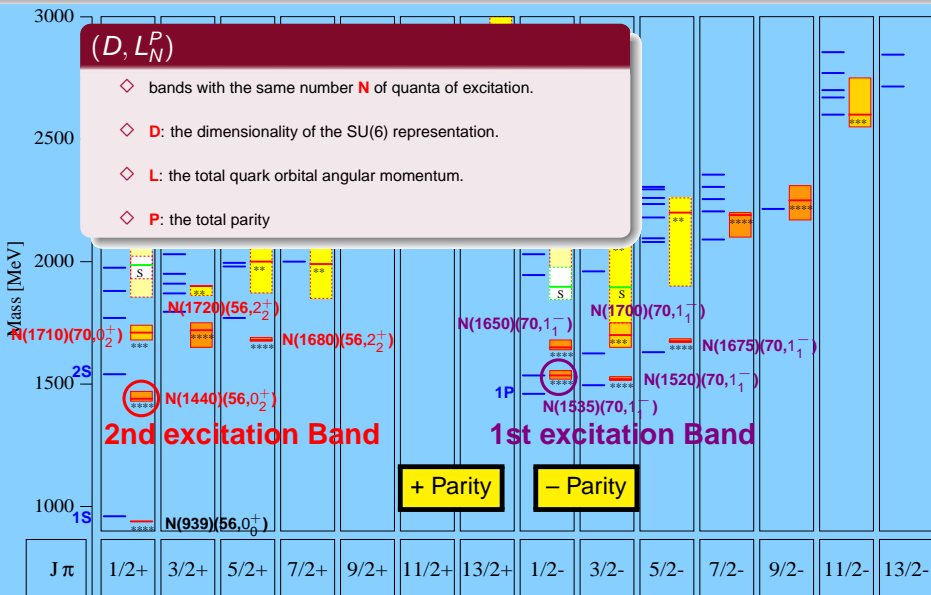
◇ Pair production

- At the vicinity of an atom, a photon with energy greater than 1.02 MeV creates a positron-electron pair, and such a process is called pair production.

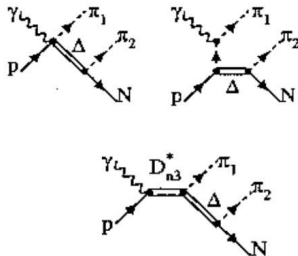
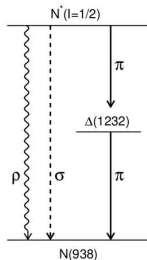
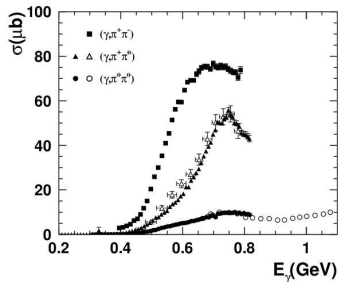
The spectrum of N^* resonances

 (D, L_N^P)

- ◇ bands with the same number N of quanta of excitation.
- ◇ D : the dimensionality of the SU(6) representation.
- ◇ L : the total quark orbital angular momentum.
- ◇ P : the total parity



Double pion-production in the second resonance region



- ◇ Total cross section of the three isospin channels of double pion production on the proton.
- ◇ Possible resonance contributions to double pion production in the second resonance region.
 - $N^*(l=1/2) \rightarrow N(938)\rho$
 $\rightarrow N(938)f_0(600)$
 $\rightarrow \delta(1232)\pi \quad \rightarrow N(938)\pi\pi$
- ◇ An important contribution is assigned to the $\gamma p \rightarrow \Delta^{++}\pi^-$ channel while the $\gamma p \rightarrow \Delta^0\pi^+$ channel is negligible.

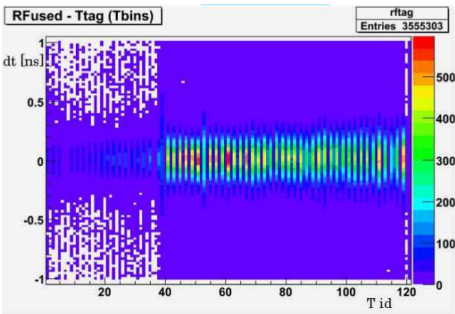
Calibration

● The process of the data acquisition

- Step 1** A trigger is detected. (The g9a experiment has used a trigger which required at least one charged particle in CLAS spectrometer.)
- Step 2** Time counters in detectors start measuring the time.
- Step 3** When a signal is detected, they stop and record the data.

● The calibration of all detector components

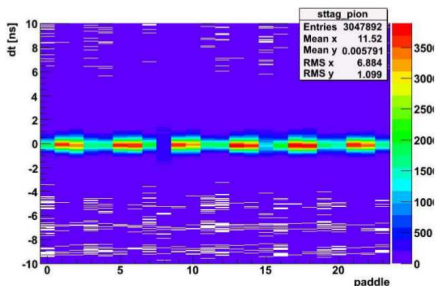
- ◇ The calibration aligns their timing with the beam radio frequency time (RF or accelerator time).
- ◇ An electron beam bucket is supplied to the target about every 2 ns.



● Tagger Calibration

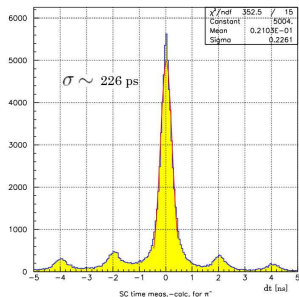
- ◇ $dt = (T_{\text{reconstructed in the tagger at the target center}} - T_{\text{RF time identified nearest bucket at the target center}})$
- ◇ T counter is matched to the RF bucket

Calibration



● ST Calibration

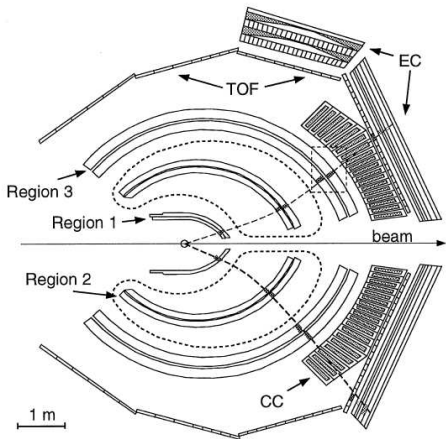
- ◇ $dt = (\text{RF vertex time}) - (\text{ST vertex time})$
- ◇ offsets are around zero



● TOF Calibration

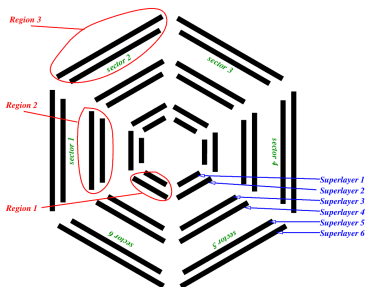
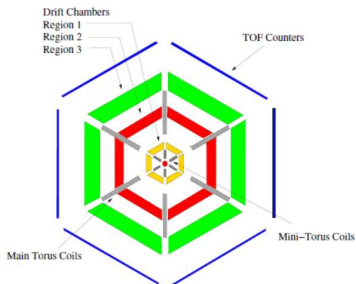
- ◇ $dt = (\text{RF vertex time}) - (\text{TOF vertex time})$
- ◇ The time-of-flight times are corrected for the flight time back to the target.
- ◇ Particle identification in CLAS relies on the combination of measured charged-particle momenta (from DC) and the flight time from the target to the respective TOF counters.

Drift chamber(DC) Calibration

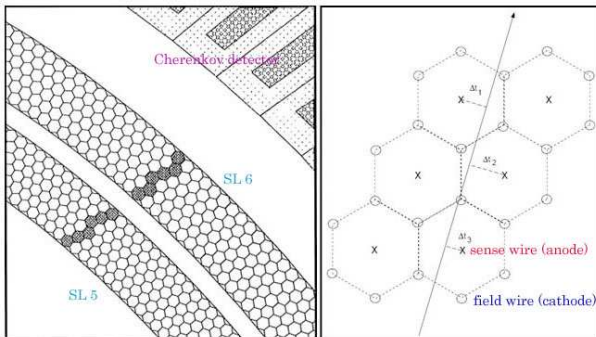


$$p = qBR$$

- ◇ p : the momentum
- ◇ q : the sign of the charge
- ◇ R : the radius of the curvature
- ◇ B : the magnetic field

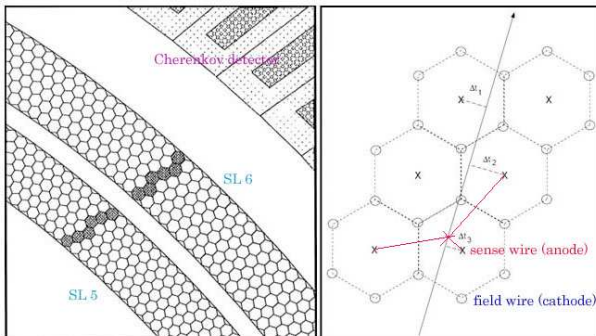


Drift chamber(DC) Calibration



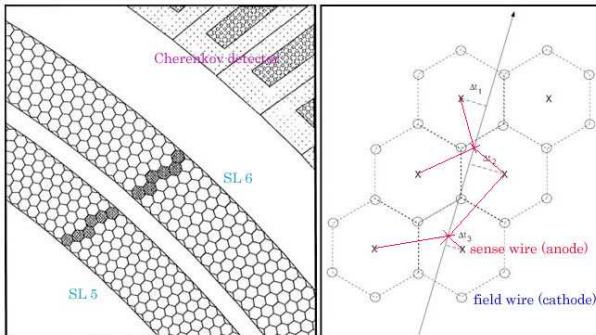
- ◇ The DC are in a magnetic field and produce the curvature of the particle.
 - Thin wires are fixed in a volume filled with the gas mixture (90% argon and 10% CO₂).
 - The DC has a quasi-hexagonal pattern as the cell form with six field wires (cathodes) surrounding one sense wire (anode)
 - A traversing charged particle ionizes the gas inside these cells and the electrons drift to the sense wire.

Drift chamber(DC) Calibration



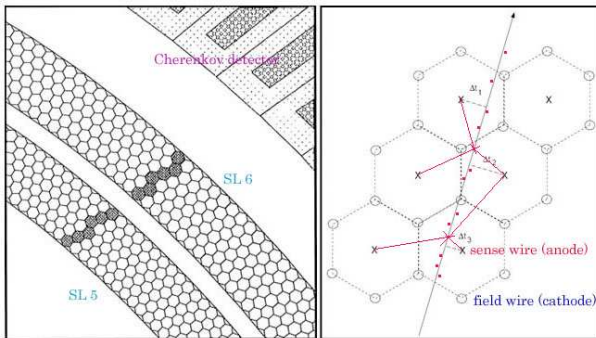
- ◇ The fitted DOCA and drift time is found.
 - DOCA means the distance of closest approach of the charged particle to the sense wire.

Drift chamber(DC) Calibration



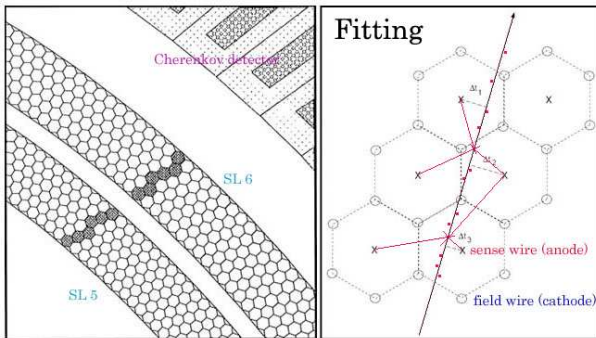
- ◇ The fitted DOCA and drift time is found.

Drift chamber(DC) Calibration



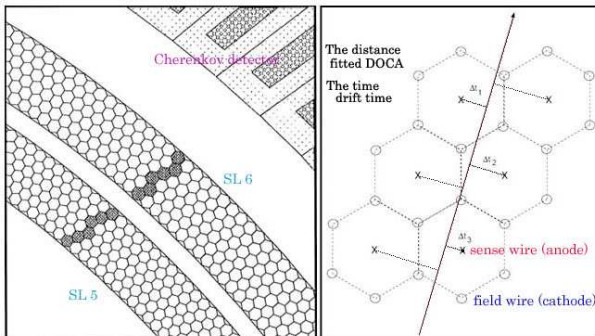
- ◇ The fitted DOCA and drift time is found.

Drift chamber(DC) Calibration

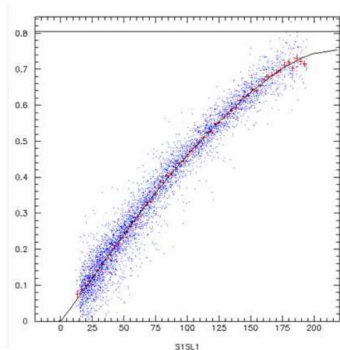
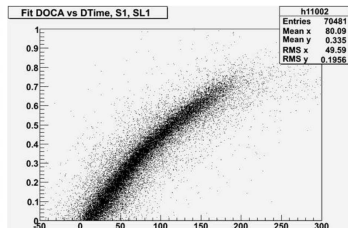


- ◇ The fitted DOCA and drift time is found.

Drift chamber(DC) Calibration

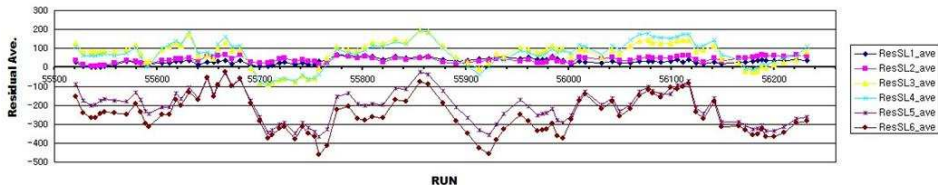


- ◇ The fitted DOCA and drift time is found.
- ◇ The drift velocity function is found using fitting.
- ◇ The calculated DOCA is found using the velocity and the drift time.

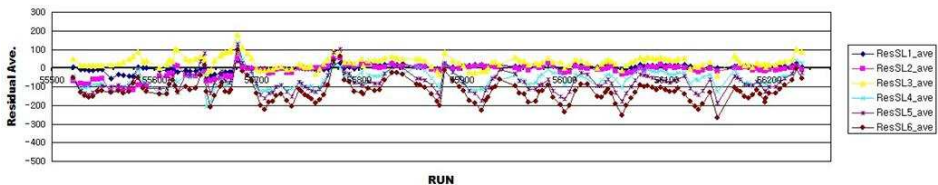


Drift chamber(DC) Calibration

DC Residuals Ave. (7/3 ~7/11)



DC_Residuals Ave. (8/30~9/4)



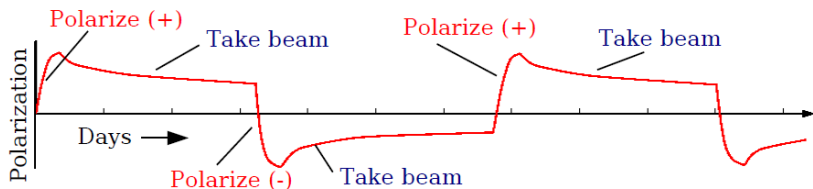
- ◇ Average DC residuals before starting (the top) and after finishing (the bottom) DC calibration in the g9a dataset.

Residual = calculated DOCA - fitted DOCA

The Frozen-Spin Target (FROST)

Operation is more complicated:

- (1) Polarize target material via DNP at 5 T and 0.5 K (**Polarizing Mode**)
- (2) After optimum polarization is obtained, turn off microwaves and 5 T magnet
- (3) Use a 2nd magnet (~ 0.5 T) and very low temperatures to “freeze” the polarization (**Frozen Spin Mode**)
- (4) Polarization will decay very slowly with a time constant of several days
- (5) After polarization decays to about 50 % of its initial value, go back to step 1



A Simple Way to Polarize

Brute Force Polarization

$$P_{\text{te}} = \tanh\left(\frac{\vec{\mu} \cdot \vec{B}}{kT}\right)$$

Disadvantages:

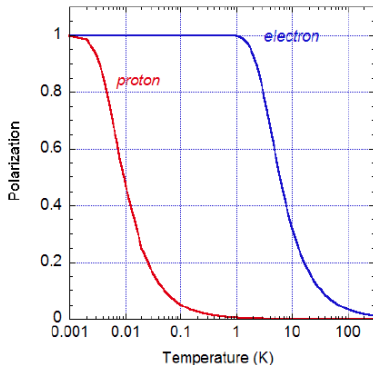
- 1 Requires very large magnet
- 2 Low temperatures require low luminosity
- 3 Polarization can take a very long time (protons slow, electrons fast)

To get high polarization

maximize B

minimize T

5 Tesla



A Better Way – Dynamic Nuclear Polarization

- (1) Use **brute force** to polarize free electrons in the target material.
- (2) Use **microwaves** to “transfer” this polarization to nuclei.

Mutual electron-nucleus spin flips re-arranges the nuclear Zeeman populations to favor one spin state over the other.

For best results:

DNP is performed at B/T conditions where electrons t_1 is short (ms) and nuclear t_1 is long (minutes):

$$\begin{aligned} \text{JLab: } B &= 5 \text{ T} \\ T &= 1 \text{ K} \end{aligned}$$

Materials for DNP Targets

Choice of material dictated by:

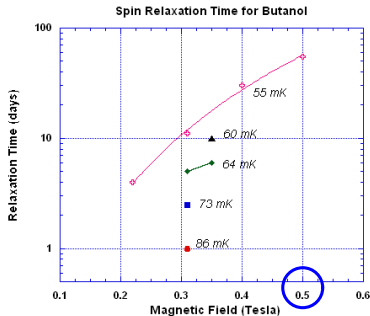
- 1 A maximum polarization
- 2 A resistance to ionization from radiation
- 3 A minimum number of polarizing nucleon

Compromise: Butanol (C_4H_9OH)

- Quality (dilution) factor:

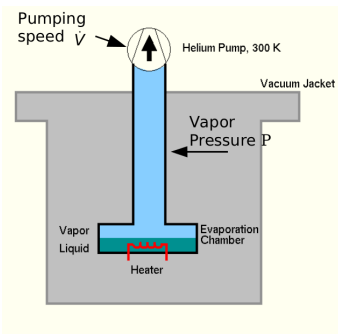
$$f = \vec{N}/N_{\text{total}} = 10/74 \approx 0.13$$

The holding magnet for FROST : 0.5 T

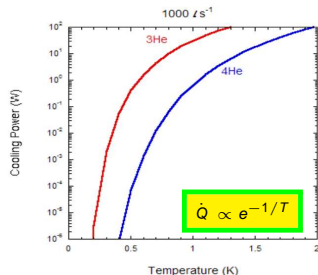
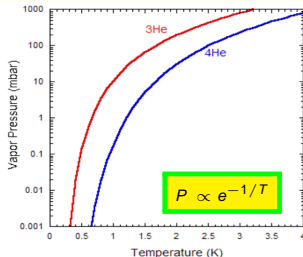


Ch. Bradtke, PhD Thesis, Univ. Bonn, 1999

Refrigeration below 4.2 K - Evaporative Cooling

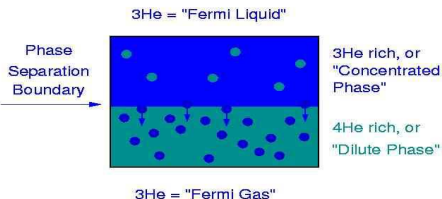


- ◇ In order to evaporate 1 mole of ^4He , the heater, L (~ 80 J/mol) must supply.
- ◇ In absence of a heater,
 - liquid will absorb heat from surroundings and liquid's temperature will drop
- ◇ Cooling power of a evaporation "fridge", \dot{Q} is
 - $\dot{Q} = \dot{n}L = \dot{V}PL$



$^3\text{He}/^4\text{He}$ Dilution Refrigeration

- Below 0.8 K, a $^3\text{He}/^4\text{He}$ mixture will separate into two phases.



The specific heat of a ^3He atom

→ $C_c = 22 \text{ J}/(\text{mol}\cdot\text{K})$

→ $C_d = 106 \text{ J}/(\text{mol}\cdot\text{K})$

- The ^3He atoms move from the concentrated phase to the dilute phase with the heat energy exchange with the surroundings.
- Removing the ^3He from the dilute phase causes the ^3He atoms in the concentrated phase to
 - absorb the heat from its surroundings
 - dissolve into the dilute phase in order to re-establish a thermal equilibrium.

The $^3\text{He}/^4\text{He}$ Dilution Refrigerator for FROST

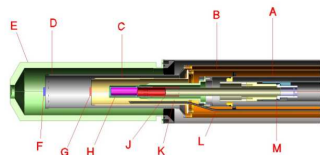
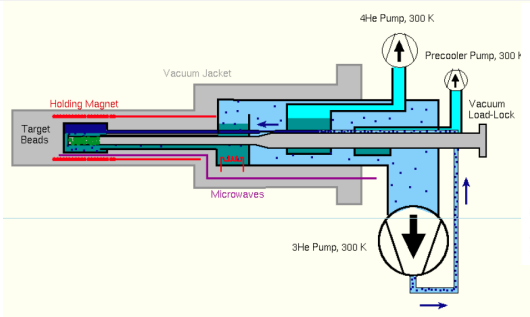
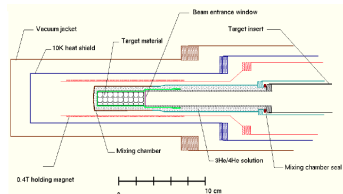
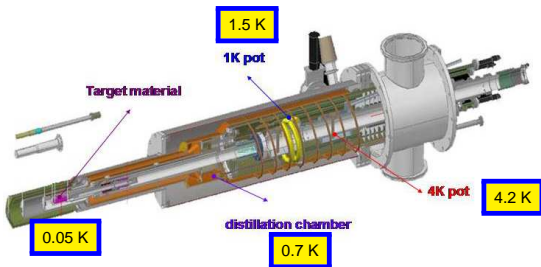


Figure 3.6: A cross section of the target area of FROST: *a*) primary heat exchanger; *b*) 1 K heat shield; *c*) holding coil; *d*) 20 K heat shield; *e*) outer vacuum can (Rohacell extension); *f*) polyethylene target; *g*) carbon target; *h*) butanol target; *j*) target insert; *k*) mixing chamber; *l*) microwave waveguide; *m*) kapton coldseal [10].

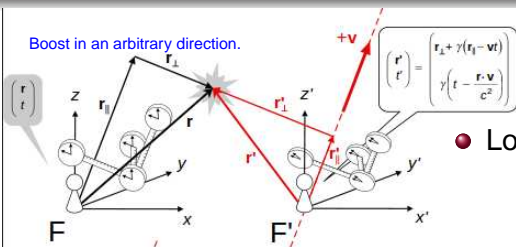


The Frozen-Spin Target - Summary of Results

	Expectation	Result
Base temperature:	50 mK	28 mK (w/o beam) 30 mK (w/ beam)
Cooling Power:	10 μ W (Frozen) 20 mW (Polarizing)	800 μ W @ 50mK 60mW @ 300 mK
Polarization:	80 %	+ 82 % - 85 %
1/e Relaxation Time:	500 hours	2700 hours (+ Pol.) 1600 hours (-Pol.)

Lorentz Boost

Boost in an arbitrary direction.

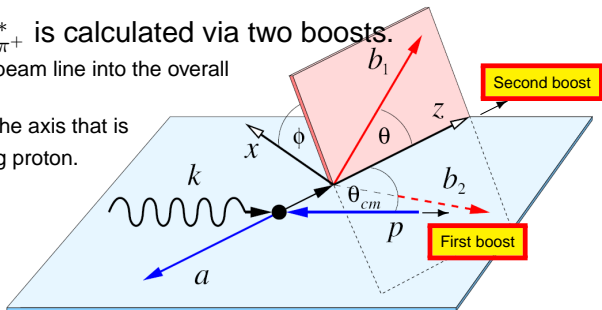


• Lorentz transformation

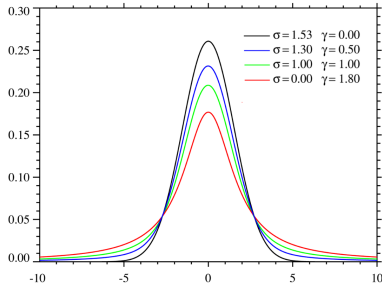
- ◇ how measurements of space and time by two observers are related.
- ◇ The Lorentz transformations are called "boosts" in the stated directions.

• The azimuthal angle, $\phi_{\pi^+}^*$ is calculated via two boosts.

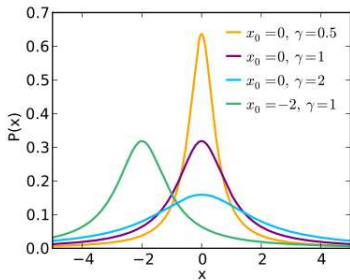
- ◇ The first boost along the beam line into the overall center-of-mass frame.
- ◇ The second boost along the axis that is antiparallel to the recoiling proton.



The voigt function



Voigt function



Breit Wigner function

• A voigt function, $V(x; \sigma, \gamma)$

- ◇ A voigt function is a convolution of a Breit-Wigner function and a Gaussian function

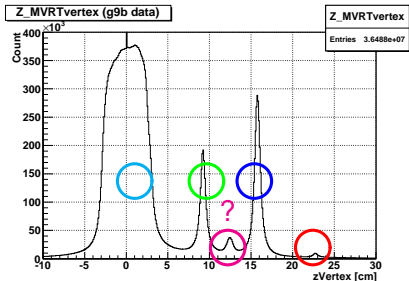
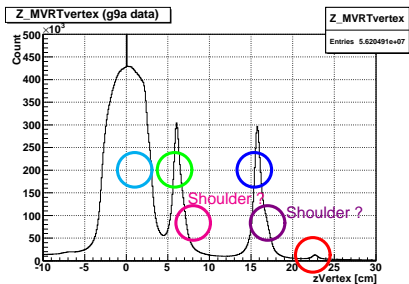
$$V(x; \sigma, \gamma) = \int_{-\infty}^{\infty} G(x'; \sigma) L(x - x'; \gamma) dx'$$

- ◇ $G(x; \sigma)$ is the centered Breit-Wigner function and $L(x; \gamma)$ is the centered Lorentzian function

$$G(x; \sigma) \equiv \frac{e^{-x^2/(2\sigma^2)}}{\sigma\sqrt{2\pi}}$$

$$L(x; \gamma) \equiv \frac{\gamma}{\pi(x^2 + \gamma^2)}$$

Hydrogen contamination of the carbon target (g9a)



(E)outer vacuum can

(F)CH2 target

(G)Carbon target

(H)Butano target



- The holding magnet for g9b is longer than for g9a

so the carbon vertex for g9b is shifted into 3cm downstream

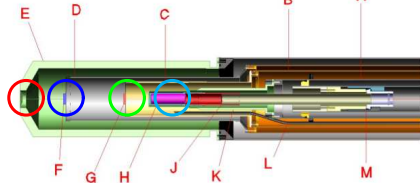


Figure 3.6: A cross section of the target area of FROST: *a*) primary heat exchanger; *b*) 1 K heat shield; *c*) holding coil; *d*) 20 K heat shield; *e*) outer vacuum can (Rohacell extension); *f*) polyethylene target; *g*) carbon target; *h*) butanol target; *j*) target insert; *k*) mixing chamber; *l*) microwave waveguide; *m*) kapton coldseal [10].

Hydrogen contamination of the carbon target (g9a)

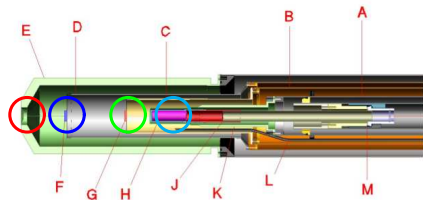
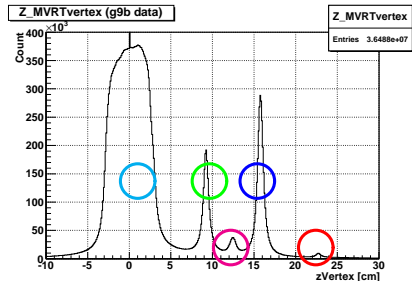
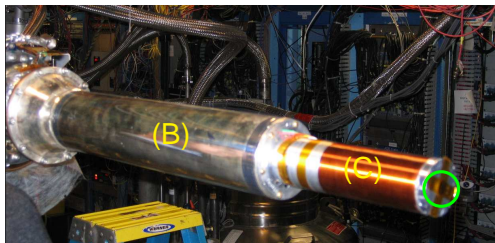
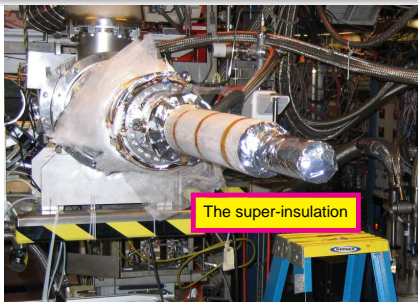
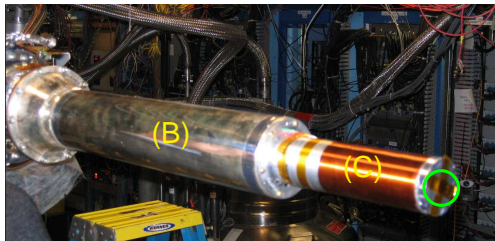
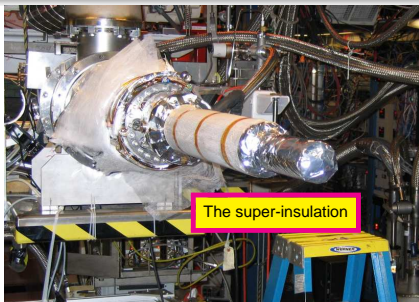
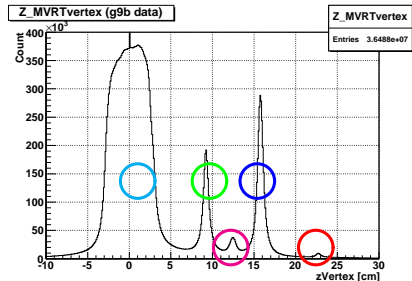


Figure 3.6: A cross section of the target area of FROST: *a*) primary heat exchanger; *b*) 1 K heat shield; *c*) holding coil; *d*) 20 K heat shield; *e*) outer vacuum can (Rohacell extension); *f*) polyethylene target; *g*) carbon target; *h*) butanol target; *j*) target insert; *k*) mixing chamber; *l*) microwave waveguide; *m*) kapton coldseal [10].

Hydrogen contamination of the carbon target (g9a)

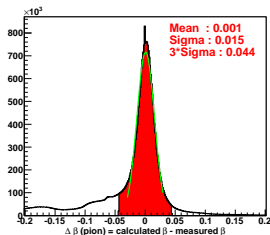
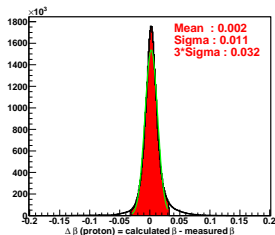
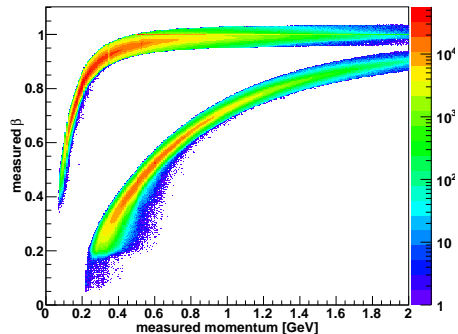
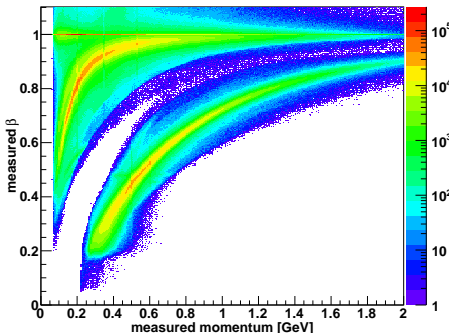


The conclusion :



- The shoulder near the carbon peak in g9a data and 12.5 cm peak in g9b are from super-insulation on the 1K heat shield
- The shoulder near the CH₂ peak in g9a data is from super-insulation on the 20K heat shield
- The distance btw the carbon and super-insulation in g9a may be closer than in g9b
 - This make the carbon data contaminated by the hydrogen in g9a data

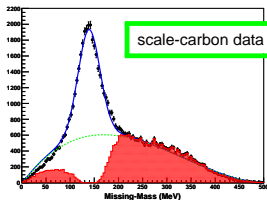
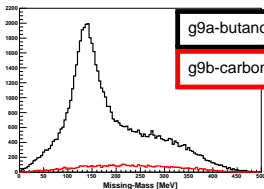
Proton and Pion Selection



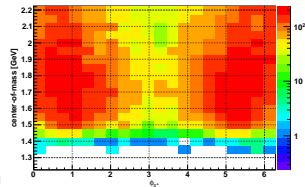
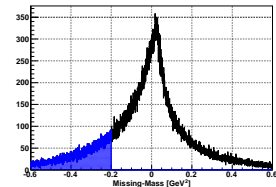
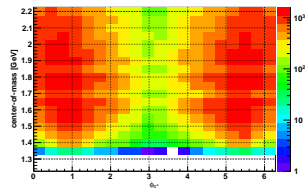
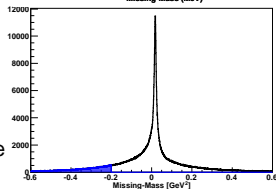
◇ proton selection
: $|\Delta\beta| < 0.032$

◇ pion selection
: $|\Delta\beta| < 0.044$

General method to get the phase space scale factor

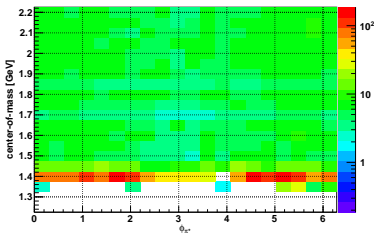


$$\text{scale factor} = \frac{\text{scale-carbon data}}{\text{g9b-carbon data}}$$



- The bound-nucleon events are isolated from the butanol data by a loose cut at $MM^2 < -0.2 \text{ GeV}^2$.

General method to get the scale factor



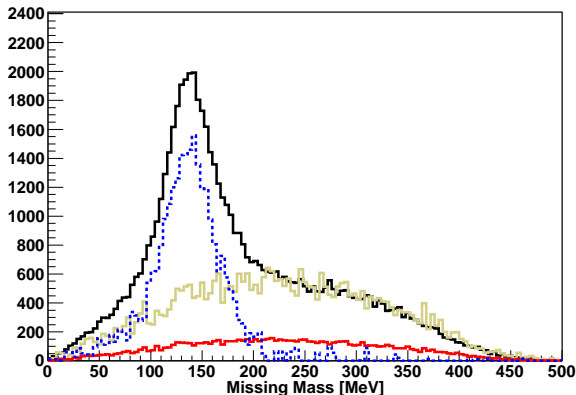
- The phase-space scale factor (W versus $\phi_{\pi^+}^*$)
- This scale factor is calculated by dividing two histograms. (Butanol/Carbon)

scale-carbon data

= scale factor \times carbon data

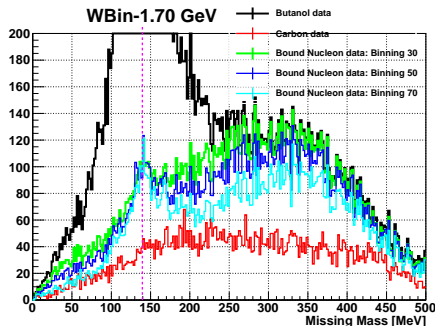
free-proton data

= butanol data - scale-carbon data



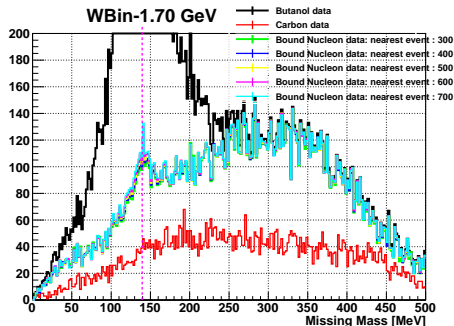
The internal conditions of the Q-factor method

◇ Optimizing the number of binning



→ the proper number of binning is 30.

◇ Optimizing the number of nearest events



→ the proper number of nearest events is 300.

Polarization observable I^\odot

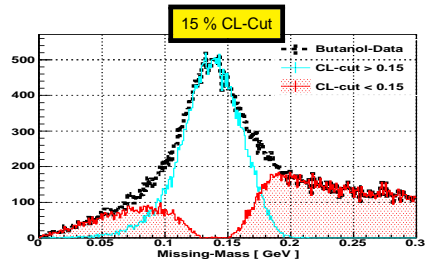
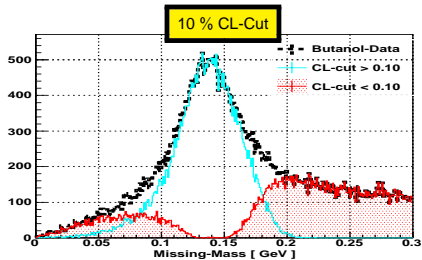
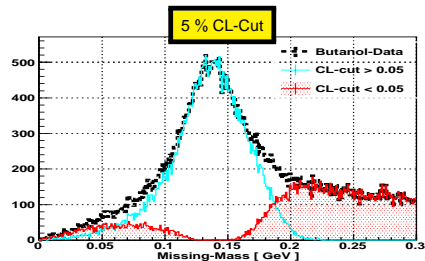
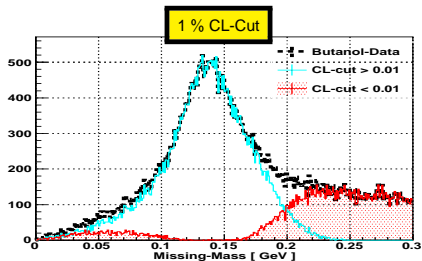
$$I^\odot(\mathbf{W}, \phi_{\pi^+}) = \frac{1}{\bar{\delta}_\odot(\mathbf{W})} \frac{\left\{ N(\rightarrow; \mathbf{W}, \phi_{\pi^+})_{beam} - N(\leftarrow; \mathbf{W}, \phi_{\pi^+})_{beam} \right\}}{\left\{ N(\rightarrow; \mathbf{W}, \phi_{\pi^+})_{beam} + N(\leftarrow; \mathbf{W}, \phi_{\pi^+})_{beam} \right\}}$$

- ◇ $\bar{\delta}_\odot(\mathbf{W})$: The average of the degree of the photon beam polarizations
- ◇ Λ_z : The degree of the target polarizations
- ◇ F : The photon flux (Normalization factor between periods)
- ◇ \rightarrow (\leftarrow) : the direction of the beam polarization is parallel (anti-parallel) to the beam.
- ◇ \Rightarrow (\Leftarrow) : the direction of the target polarization is parallel (anti-parallel) to the beam.
- ◇ Using the dataset with the unpolarized target and circularly-polarized beam

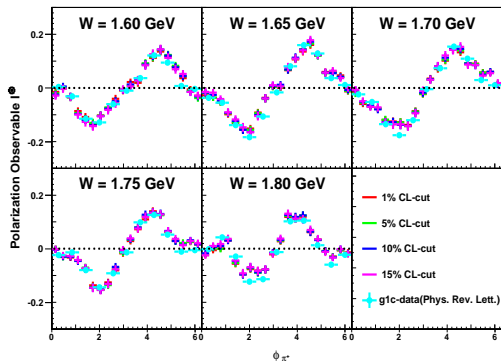
$$N(\rightarrow; \mathbf{W}, \phi_{\pi^+})_{beam} = \frac{N(\rightarrow\Rightarrow; \mathbf{W}, \phi_{\pi^+})_{butanol}}{\Lambda_z(\Rightarrow) \cdot F(\Rightarrow)} + \frac{N(\rightarrow\Leftarrow; \mathbf{W}, \phi_{\pi^+})_{butanol}}{\Lambda_z(\Leftarrow) \cdot F(\Leftarrow)}$$

$$N(\leftarrow; \mathbf{W}, \phi_{\pi^+})_{beam} = \frac{N(\leftarrow\Rightarrow; \mathbf{W}, \phi_{\pi^+})_{butanol}}{\Lambda_z(\Rightarrow) \cdot F(\Rightarrow)} + \frac{N(\leftarrow\Leftarrow; \mathbf{W}, \phi_{\pi^+})_{butanol}}{\Lambda_z(\Leftarrow) \cdot F(\Leftarrow)}$$

Missing mass distribution in several CL-cuts.



The background effect in Beam-Helicity Asymmetry I^{\odot}



- The different CL-cuts have the different background effect. However, they have the similar values in the observable I^{\odot} .
- g9a dataset is not sensitive to distinguish between the beam asymmetry from free-proton, bound-nucleon and background data.