

## **RooFit Programmers Tutorial**

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# RooFit design philosophy



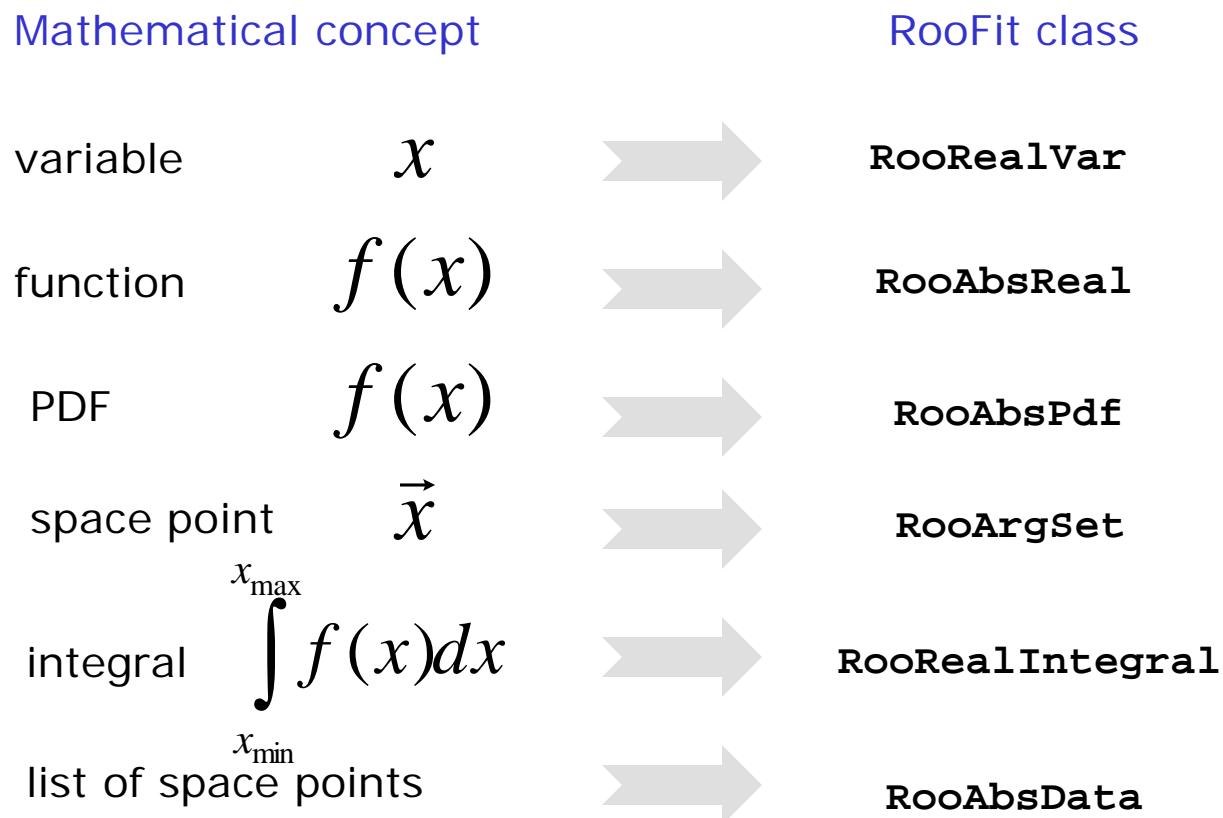
Mathematical concepts as C++ objects

General rules for RooFit classes

# RooFit core design philosophy

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- Mathematical objects are represented as C++ objects



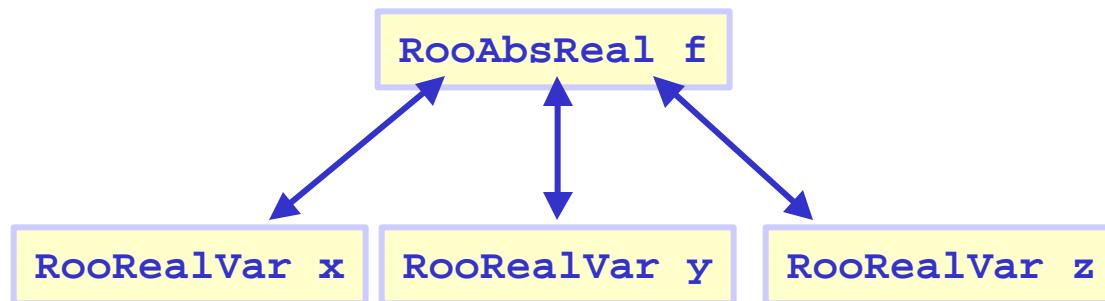
# RooFit core design philosophy

- Represent relations between variables and functions as client/server links between objects

Math

$$f(x,y,z)$$

RooFit  
diagram



RooFit  
code

```
RooRealVar x("x","x",5) ;  
RooRealVar y("y","y",5) ;  
RooRealVar z("z","z",5) ;  
RooBogusFunction f("f","f",x,y,z) ;
```

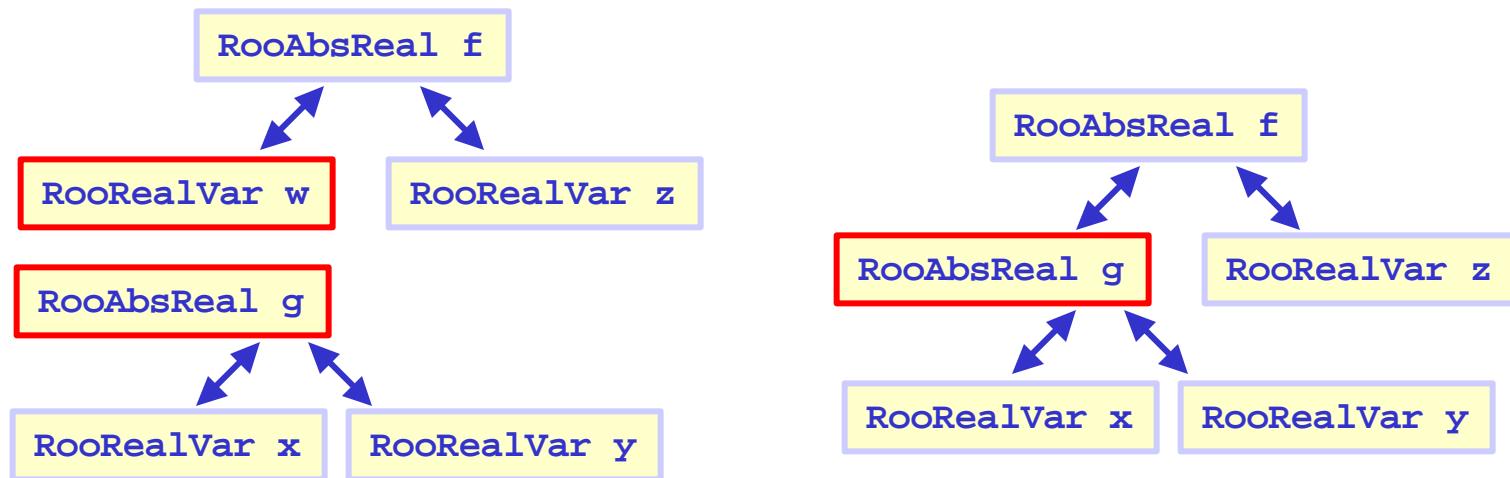
# RooFit core design philosophy

- Composite functions → Composite objects

Math

$$f(w,z) \quad g(x,y) \quad \longrightarrow \quad f(g(x,y),z) = f(x,y,z)$$

RooFit  
diagram



RooFit  
code

```
RooRealVar x("x","x",2) ;  
RooRealVar y("y","y",3) ;  
RooGooFunc g("g","g",x,y) ;  
  
RooRealVar w("w","w",0) ;  
RooRealVar z("z","z",5) ;  
RooFooFunc f("f","f",w,z) ;
```

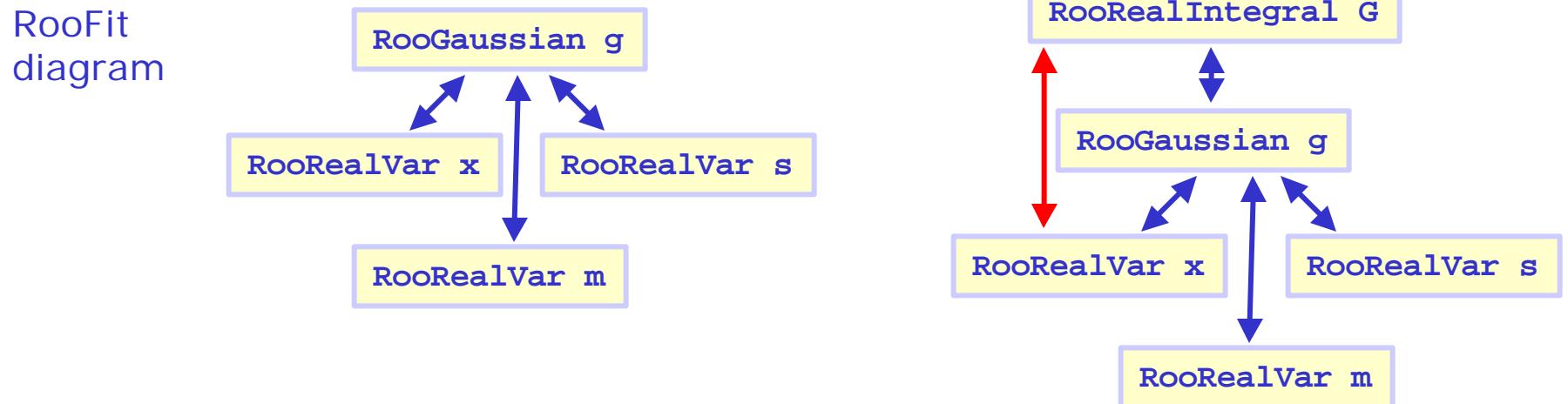
```
RooRealVar x("x","x",2) ;  
RooRealVar y("y","y",3) ;  
RooGooFunc g("g","g",x,y) ;  
  
RooRealVar z("z","z",5) ;  
RooFooFunc f("f","f",g,z) ;
```

# RooFit core design philosophy

- Represent integral as an object,  
instead of representing integration as an action

Math

$$g(x,m,s) \longrightarrow \int_{x_{\min}}^{x_{\max}} g(x,m,s) dx = G(m,s,x_{\min},x_{\max})$$



RooFit code

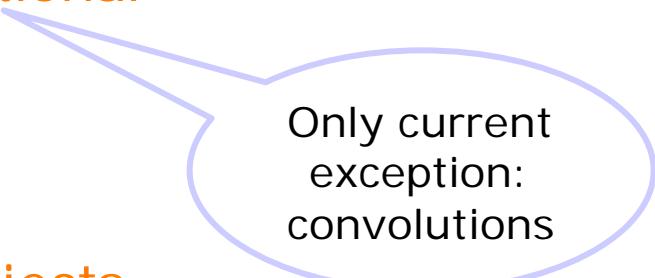
```
RooRealVar x("x","x",2,-10,10)
RooRealVar s("s","s",3);
RooRealVar m("m","m",0);
RooGaussian g("g","g",x,m,s)
```

```
RooAbsReal *G =
    g.createIntegral(x);
```

## RooFit designed goals for easy-of-use in macros

---

- Mathematical concepts mimicked as much as possible in class design
  - Intuitive to use
- Every object that can be constructed through composition should be **fully functional**
  - No implementation level restrictions
  - No zombie objects
- All methods must work on all objects
  - Integration, toyMC generation, etc
  - No half-working classes



Only current exception:  
convolutions

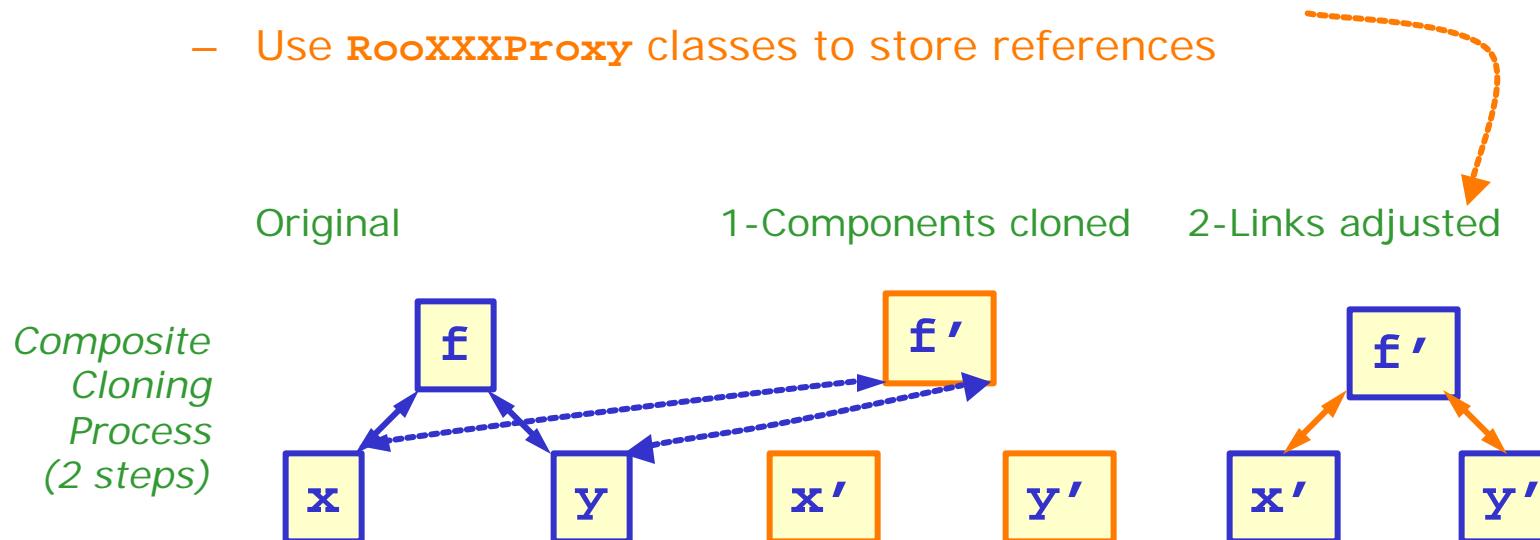
## RooFit designed for easy-of-use in macros

---

- At the same time, RooFit class structure designed to facilitate **lightweight implementation-level classes**
  - All value representing classes inherit from a common base class: **RooAbsArg**
- **RooAbsArg** and other intermediate abstract base classes handle bulk of the logistics
  - In most cases only *one* method is required: **evaluate()**
  - Implementation of common techniques such as integral calculation or ToyMC generator not mandatory
  - Base classes provide default numerical/generic methods
- RooAbsArg implementation must follow a **minimal set of coding rules**

# Coding rules for RooAbsArg derived classes

1. Write well-behaved classes.
  - RooAbsArg objects classes are not glorified **structs**, well-defined copy semantics are essential:  
**write a functional copy constructor**
2. Every concrete class must have a **clone()** method
3. Do not store pointers to other **RooAbsArg** objects
  - Many high-level RooFit operations, such as plotting, fitting and generating, clone composite PDFs and need to readjust links
  - Use **RooXXXProxy** classes to store references



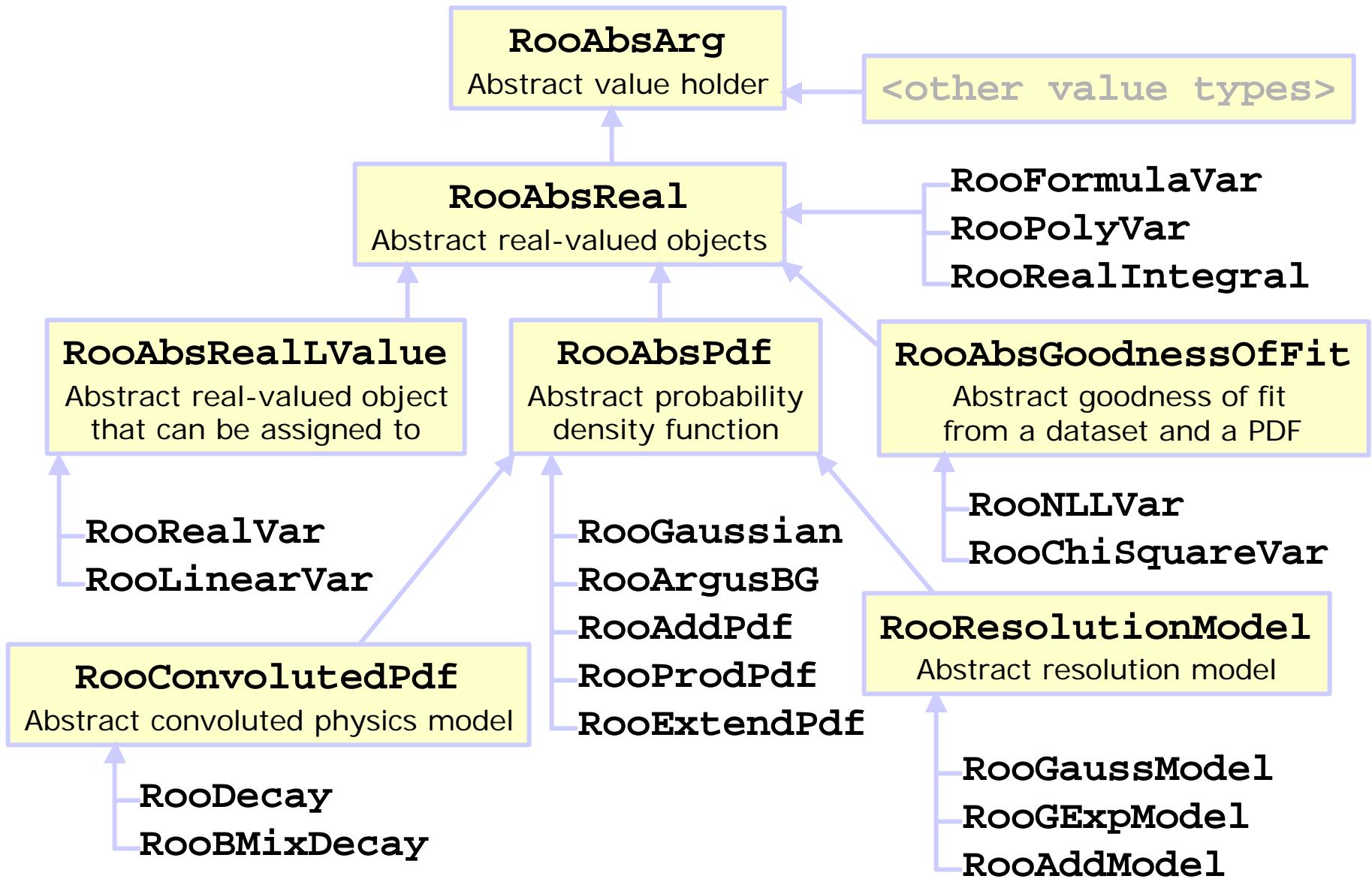
## Class hierarchy



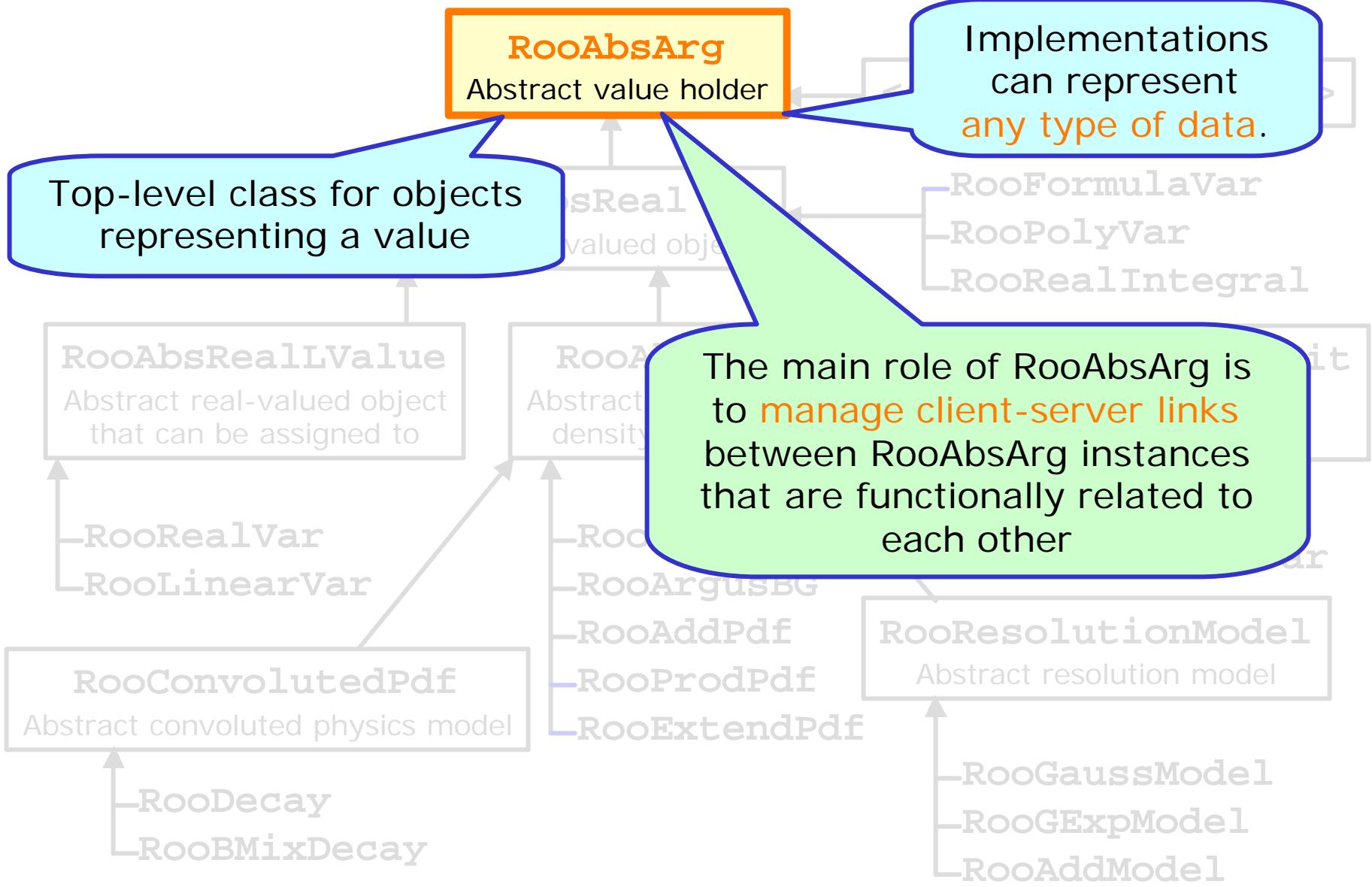
Introduction of various abstract base classes

Coding examples

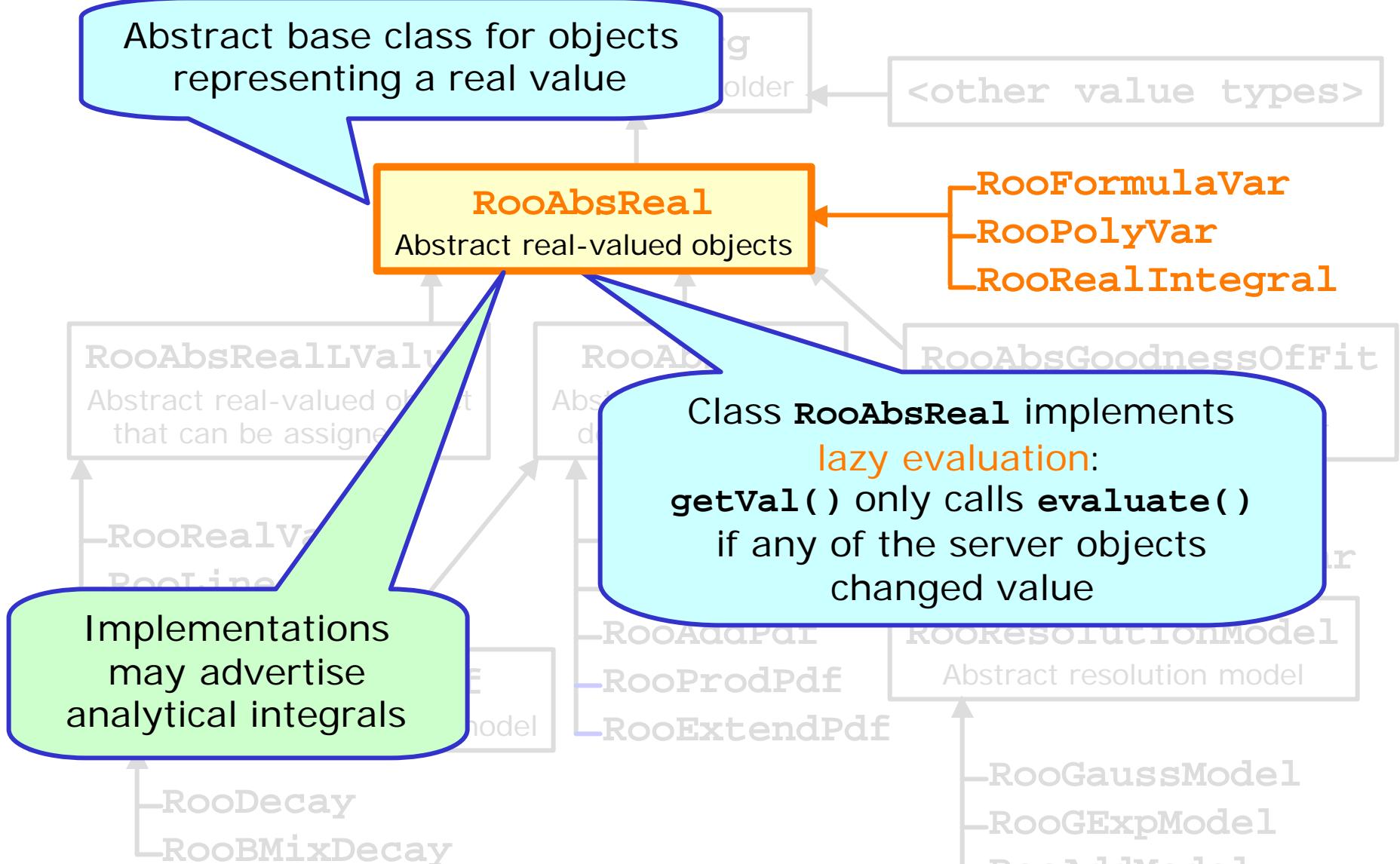
## Hierarchy of classes representing a value or function



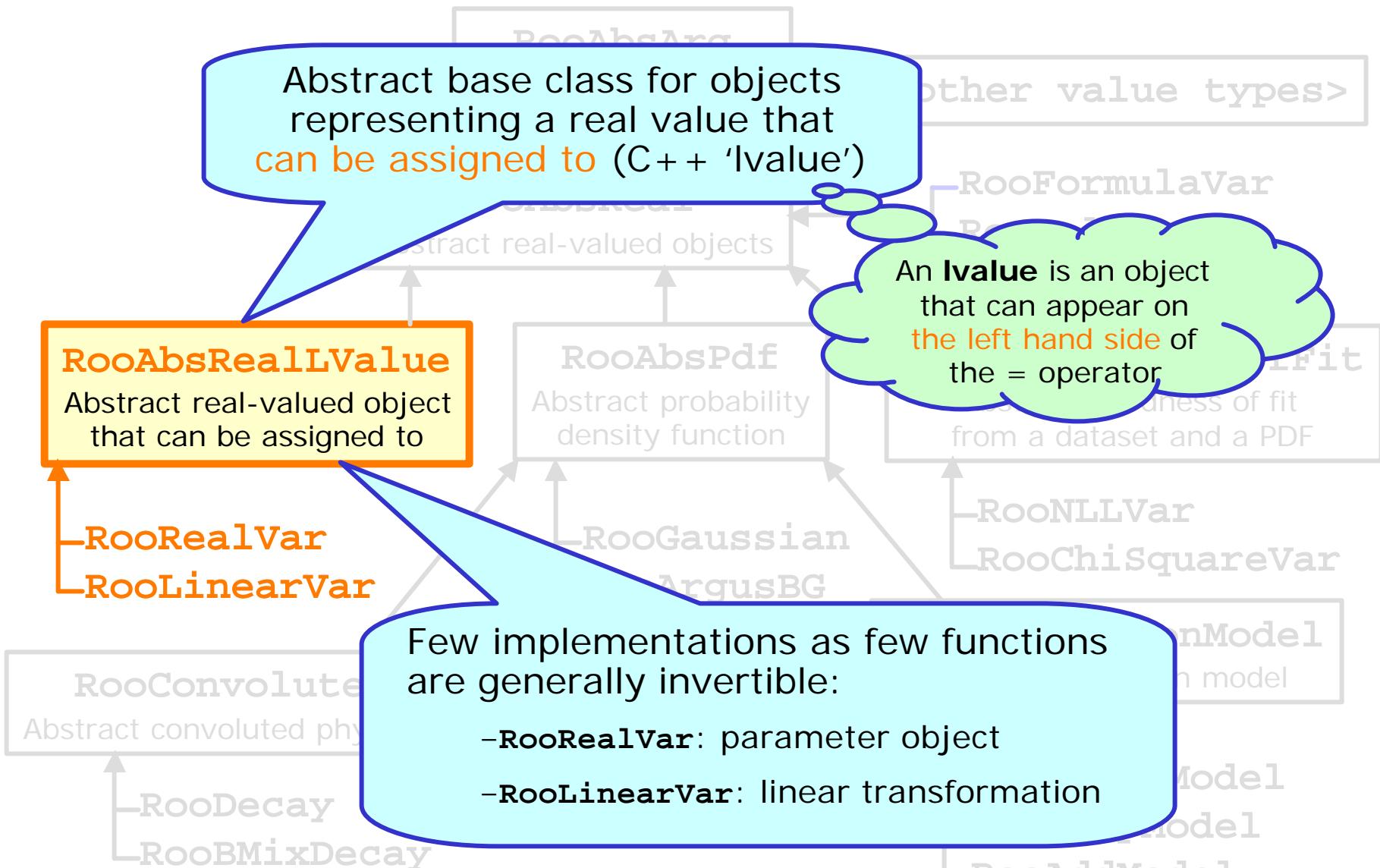
## Class **RooAbsArg**



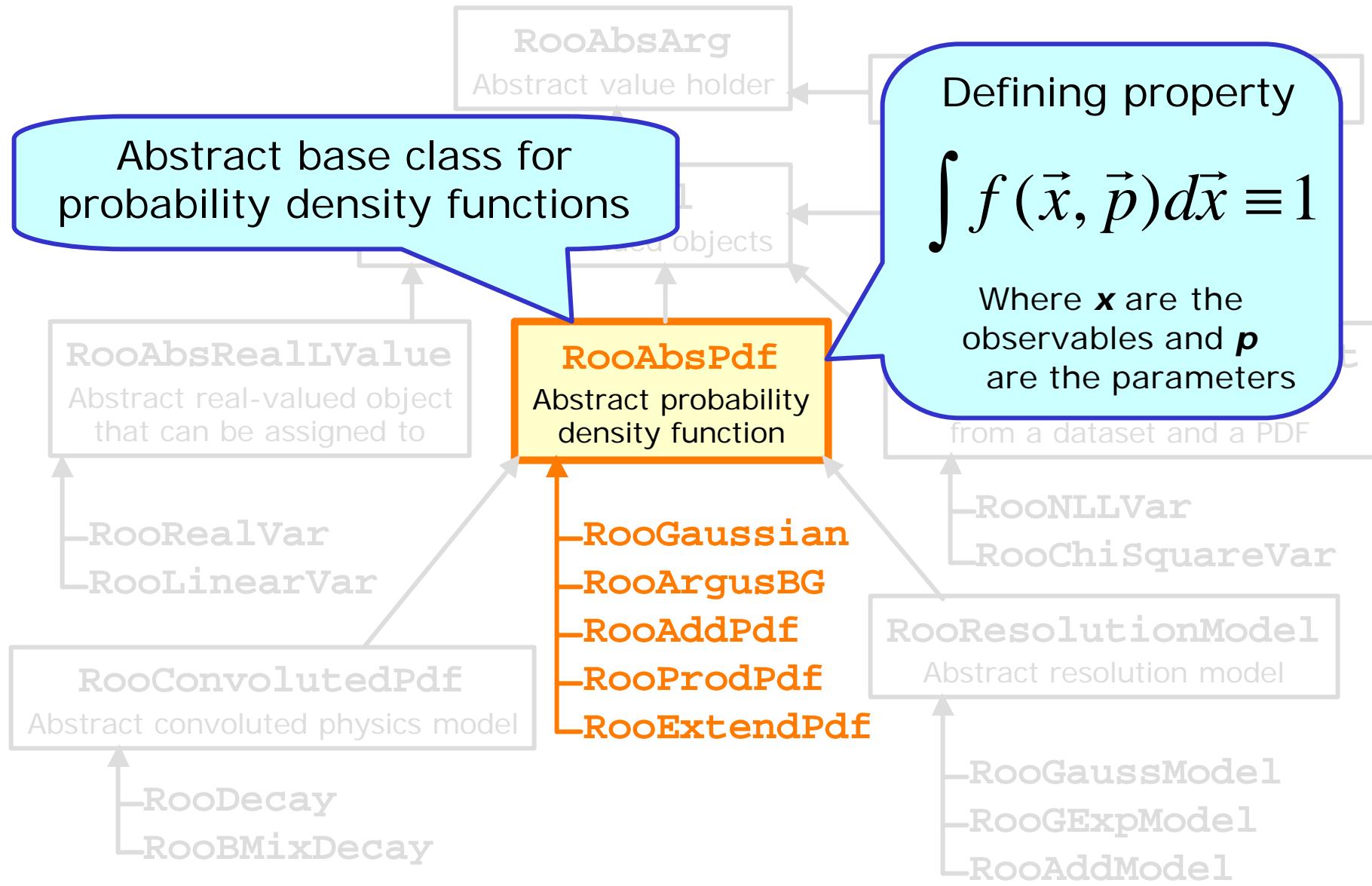
## Class **RooAbsReal**



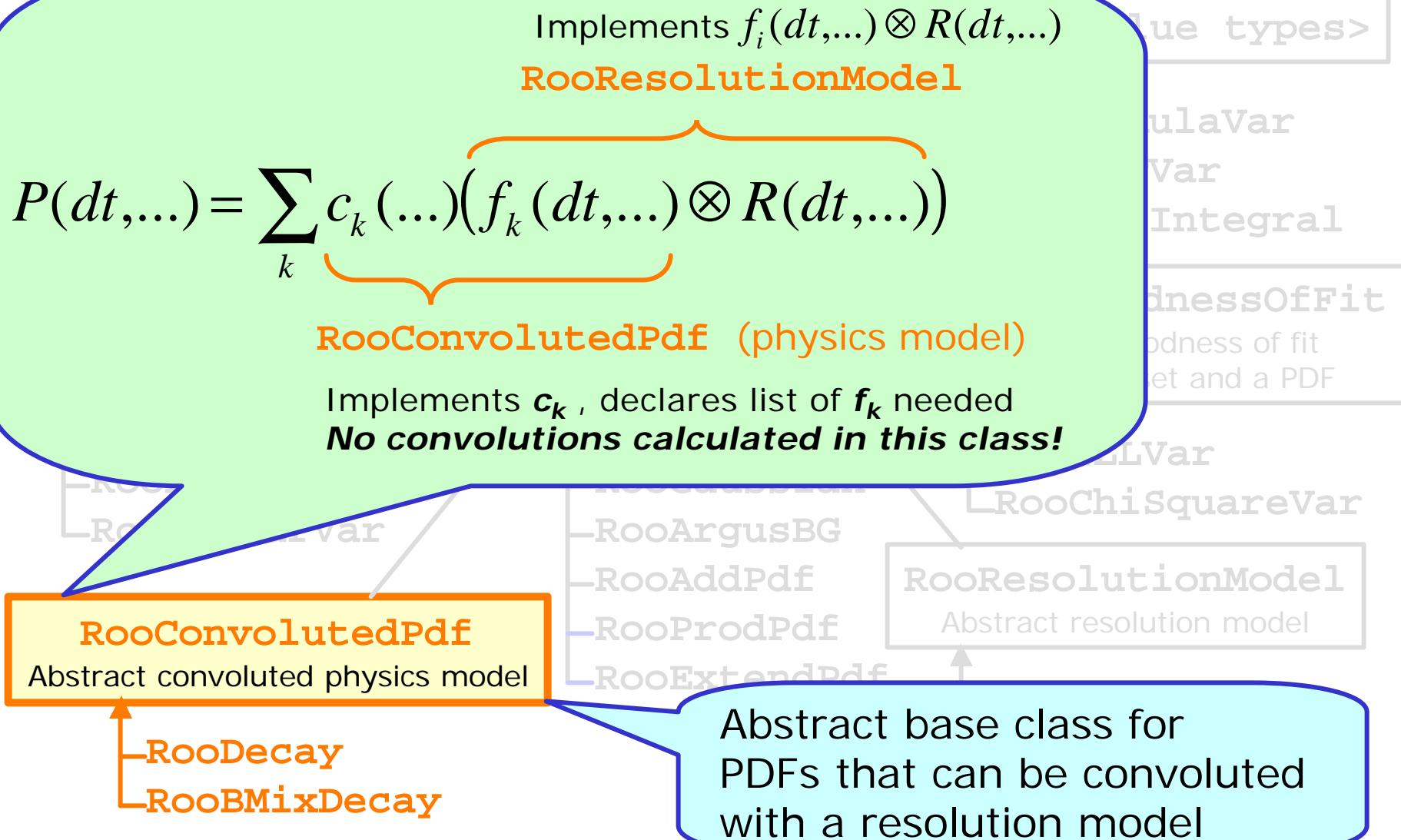
# Class `RooAbsRealValue`



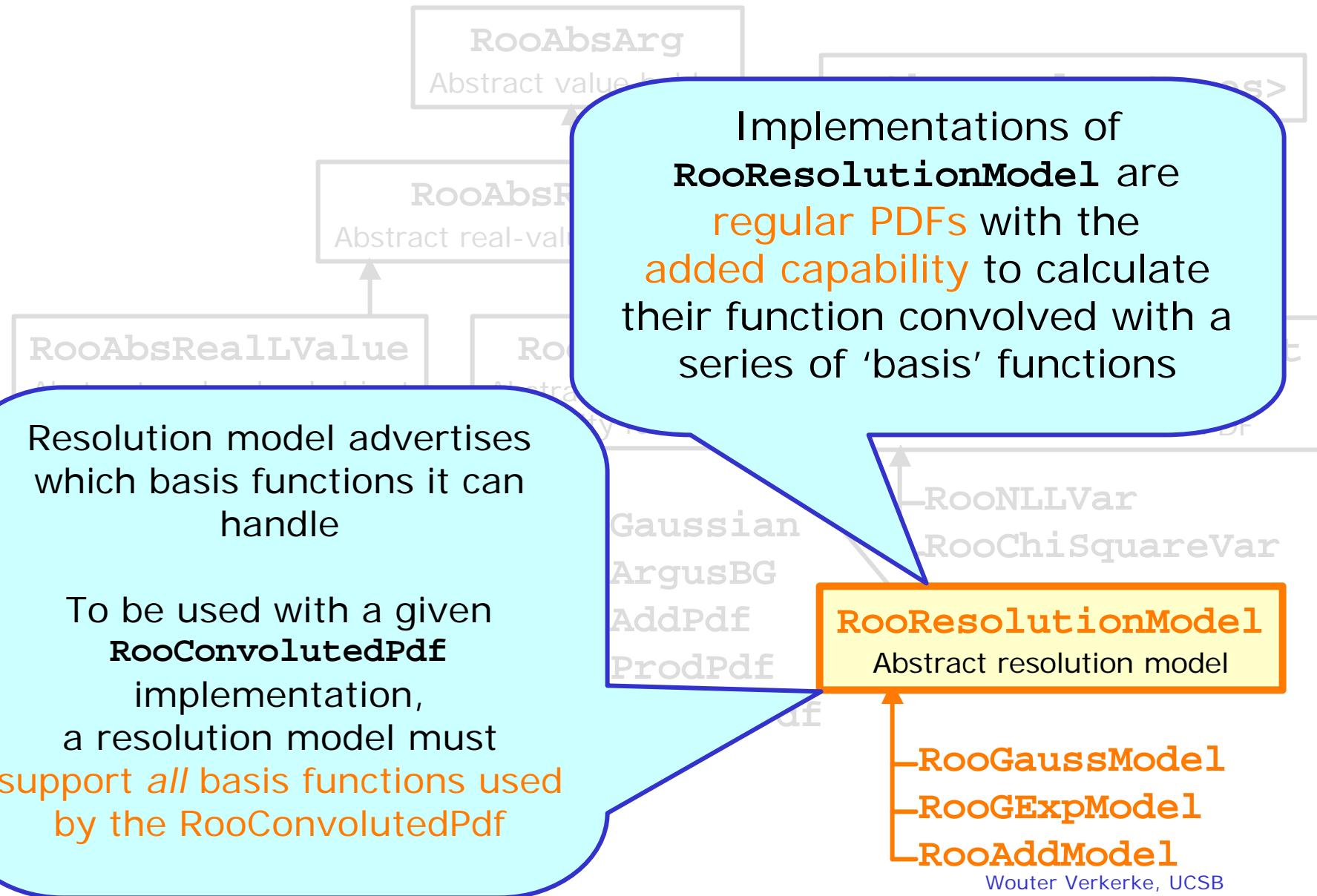
## Class **RooAbsPdf**



## Class `RooConvolvedPdf`



## Class **RooResolutionModel**



## Class `RooAbsGoodnessOfFit`

Provides the framework for efficient calculation of goodness-of-fit quantities.

A goodness-of-fit quantity is a function that is calculated from

- A dataset
- the PDF value for each point in that dataset

**RooAbsGoodnessOfFit**

Abstract goodness of fit  
from a dataset and a PDF

**RooNLLVar**

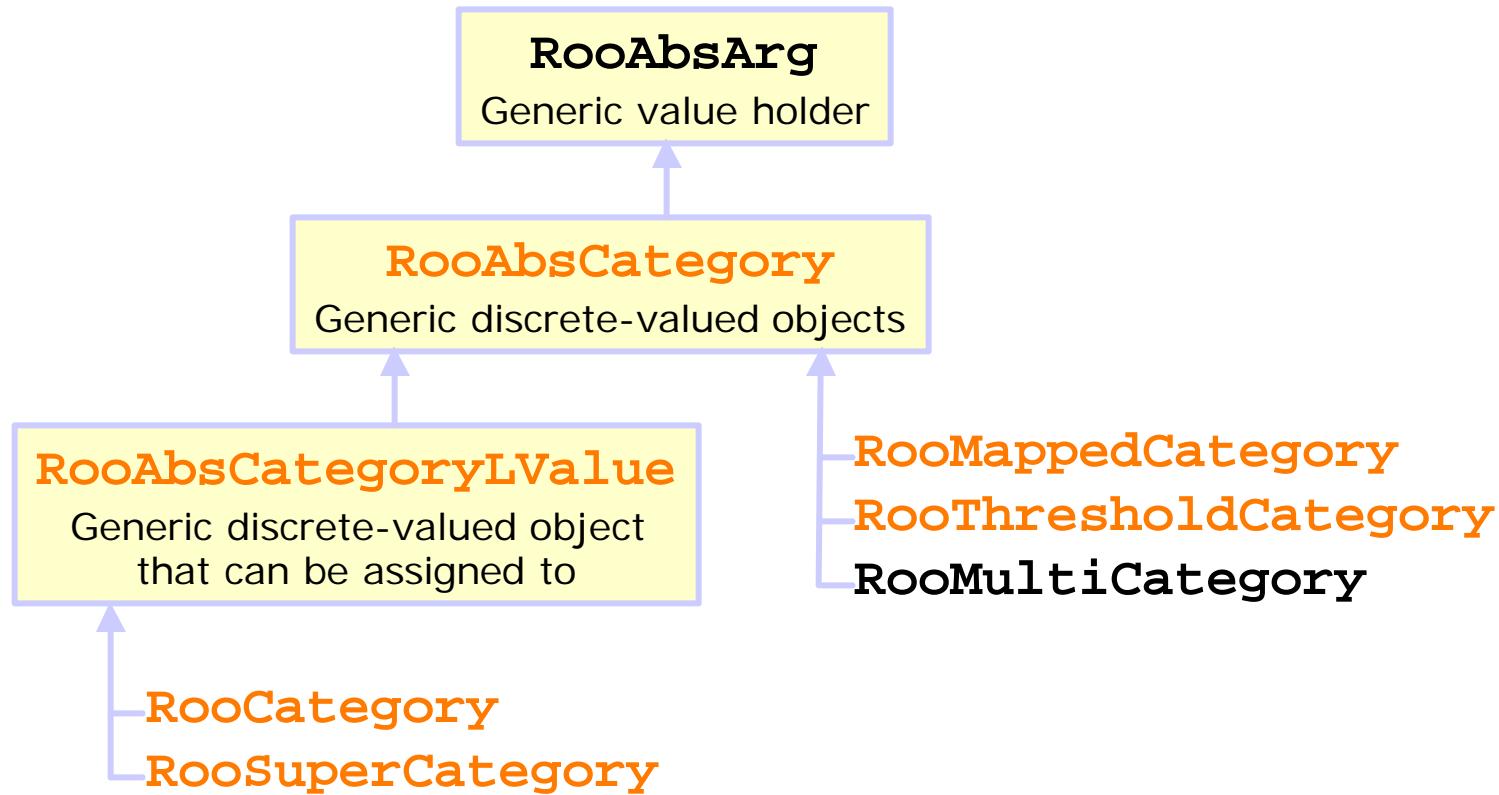
**RooChiSquareVar**

Built-in support for

- **Automatic constant-term optimization**  
activated when used by `RooMinimizer(MINUIT)`
- **Parallel execution on multi-CPU hosts**
- Efficient **calculation of RooSimultaneous** PDFs

# Class tree for discrete-valued objects

---



## Code examples



Implementing a RooAbsReal

Providing analytical integrals

Implementing a RooAbsPdf

Providing an internal generator

Implementing a RooConvolvedPdf/RooResolutionModel

Implementing a RooAbsGoodnessOfFit

# Writing a real-valued function – class **RooAbsReal**

- Class declaration

```
class RooUserFunc : public RooAbsReal {
public:
    RooUserFunc(const char *name, const char *title,
                RooAbsReal &_mean, Double_t _sigma);
    virtual TObject* clone(const char* newname) const {
        return new RooUserFunc(*this,newname);
    }
    inline virtual ~RooUserFunc() { }

protected:
    RooRealProxy x ;
    RooRealProxy mean ;
    RooRealProxy sigma ;

    Double_t evaluate() const ;

private:
    ClassDef(RooUserFunc,0) // Gaussian PDF
};
```

Real-valued functions inherit from **RooAbsReal**

# Writing a function – class `RooAbsReal`

- Mandatory methods

- Constructor → `RooUserFunc(const char *name, const char *title,  
RooAbsReal& _x, RooAbsReal& _mean,  
RooAbsReal& _sigma);`
- Copy constructor → `RooUserFunc(const RooUserFunc& other,  
const char* name=0) ;`
- Clone → `virtual TObject* clone(const char* newname) const {  
return new RooUserFunc(*this,newname);  
}`
- Destructor → `inline virtual ~RooUserFunc() { }`
- **evaluate** → `Double_t evaluate() const ;`  
*Calculates your  
PDF return value*

```
class RooUserFunc : public RooAbsPdf {  
public:  
    RooUserFunc(const char *name, const char *title,  
                RooAbsReal& _x, RooAbsReal& _mean,  
                RooAbsReal& _sigma);  
    RooUserFunc(const RooUserFunc& other,  
                const char* name=0) ;  
    virtual TObject* clone(const char* newname) const {  
        return new RooUserFunc(*this,newname);  
    }  
    inline virtual ~RooUserFunc() { }  
  
protected:  
    RooRealProxy x ;  
    RooRealProxy mean ;  
    RooRealProxy sigma ;  
  
private:  
    ClassDef(RooUserFunc,0) // Gaussian PDF  
};
```

Use copy ctor  
in `clone()`

## Writing a function – class **RooAbsReal**

- Constructor arguments

```
class RooUserFunc : public RooAbsPdf {  
public:  
    RooUserFunc(const char *name, const char *title,  
                RooAbsReal& _x, RooAbsReal& _mean,  
                RooAbsReal& _sigma);  
    (const RooUserFunc& other,  
     const char* name=0) ;  
};
```

Try to be as generic as possible, i.e.

Use **RooAbsReal&** to receive real-valued arguments

Use **RooAbsCategory&** to receive discrete-valued  
arguments

Allows user to plug in either  
a variable (**RooRealVar**) or a function (**RooAbsReal**)

```
private:  
    ClassDef(RooUserFunc,0) // Gaussian PDF  
};
```

## Writing a function – class **RooAbsReal**

- Storing **RooAbsArg** references

Always use proxies to store **RooAbsArg** references:

```
RooRealProxy      for RooAbsReal
RooCategoryProxy for RooAbsCategory
RooSetProxy       for a set of RooAbsArgs
RooListProxy      for a list of RooAbsArgs

r *title,
& _mean,
newname) const {
    return new RooUserFunc(*this,newname);

    ~RooUserFunc() { }

protected:
    RooRealProxy x ;
    RooRealProxy mean ;
    RooRealProxy sigma ;

    Double_t evaluate() const ;

private:
    ClassDef(RooUserFunc,0) // Gaussian PDF
};
```

Storing references  
in proxies allows RooFit  
to adjust pointers

This is essential  
for cloning of  
composite objects

# Writing a function – class **RooAbsReal**

- ROOT-CINT dictionary methods

```
class RooUserFunc : public RooAbsPdf {  
public:  
    RooUserFunc(const char *name, const char *title,  
                RooAbsReal& _x, RooAbsReal& _mean,  
                RooAbsReal& _sigma);  
    RooUserFunc(const RooUserFunc& other,  
                const char* name=0) ;  
    virtual TObject* clone(const char* newname) const {  
        return new RooUserFunc(*this, newname);  
    }  
    inline virtual ~RooUserFunc()  
  
protected:  
    RooRealProxy x ;  
  
private:  
    ClassDef(RooUserFunc,1) // Gaussian PDF  
};
```

Don't forget ROOT **ClassDef** macro  
No semi-colon at end of line!

Description here  
will be used in  
auto-generated  
**THtml**  
documentation

# Writing a function – class **RooAbsReal**

- Constructor implementation

```
RooUserFunc::RooUserFunc(const char *name, const char *title,
                         RooAbsReal& _x, RooAbsReal& _mean,
                         RooAbsReal& _sigma) :
    RooAbsPdf(name,title),
    x("x","Dependent",this,_x),
    mean("mean","Mean",this,_mean),
    sigma("sigma","Width",this,_sigma)
}

RooUserFunc::RooUserFunc(const char *name, const char *title,
                        RooAbsReal& other_x, RooAbsReal& other_mean,
                        RooAbsReal& other_sigma) :
    RooAbsPdf(other_name,"this",other_x),
    mean("mean",this,other_mean),
    sigma("sigma",this,other_sigma)
}

Name and title are for
description only

Double_t arg= x - mean;
return exp(-0.5*arg*arg/(sigma*sigma));
}
```

Initialize the proxies from the **RooAbsArg** method arguments

Pointer to owning object is needed to register proxy

Name and title are for description only

# Writing a function – class **RooAbsReal**

- **Implement a copy constructor!**

```
RooUserFunc::RooUserFunc(const char *name, const char *title,  
                         RooAbsReal& _x, RooAbsReal& _mean,  
                         RooAbsReal& _sigma) :  
    RooAbsPdf(name,title),
```

In the class copy constructor,  
call all *proxy copy constructors*

```
    }  
  
RooUserFunc::RooUserFunc(const RooUserFunc& other,  
                        const char* name) :
```

```
    RooAbsPdf(other.name),  
    x(this,other.x),  
    mean(this,other.mean),  
    sigma(this,other.sigma)
```

```
{
```

```
    Double_t RooUserFunc::operator()  
    {  
        Double_t arg;  
        return exp(-0.5*(arg-  
                           mean)^2/sigma^2);  
    }
```

Pointer to  
owning object  
is (again)  
needed to  
register proxy

# Writing a function – class **RooAbsReal**

- Write evaluate function

```
RooUserFunc::RooUserFunc(const char *name, const char *title,  
                         RooAbsReal& _x, RooAbsReal& _mean,  
                         RooAbsReal& _sigma) :  
    RooAbsPdf(name,title),  
    x("x","Dependent",this,_x),  
    mean("mean","Mean",this,_mean),  
    sigma("sigma","Width",this,_sigma)  
{  
}  
  
RooUserFunc::RooUserFunc(const RooUserFunc& other,  
                         const char* name) :  
    RooAbsPdf(other,name),  
    x("x",this,other.x),  
    mean("mean",this,other.mean),  
    sigma("sigma",this,other.sigma)
```

In **evaluate()**, calculate and return the function value

```
Double_t RooUserFunc::evaluate() const  
{  
    Double_t arg= x - mean;  
    return exp(-0.5*arg*arg/(sigma*sigma));  
}
```

# Working with proxies

- **RooRealProxy/RooCategoryProxy**  
objects automatically cast to the value type they represent
  - Use as if they were fundamental data types

```
RooRealProxy x ;  
Double_t func = x*x ;
```

Use as `Double_t`

```
RooCategoryProxy c ;  
if (c=="bogus") {...}
```

Use as `const char*`

- To access the proxied **RooAbsReal/RooAbsCategory** object  
use the `arg()` method

```
RooRealProxy x ;  
RooCategoryProxy c ;  
  
RooAbsReal& xarg = x.arg() ,  
RooAbsCategory& carg = c.arg() ;
```

*NB:* the value or `arg()` may  
change during the lifetime  
of the object  
(e.g. if a composite cloning  
operation was performed)

- Set and list proxy operation completely transparent
  - Use as if they were **RooArgSet/RooArgList** objects

## Lazy function evaluation & caching

---

- Method `getVal()` does not always call `evaluate()`
  - Each `RooAbsReal` object **caches** its last calculated **function value**
  - If **none** of the dependent values **changed**, **no need to recalculate**
- Proxies are used to track changes in objects
  - Whenever a `RooAbsArg` changes value,  
it notifies all its client objects that recalculation is needed
  - Messages passed via client/server links that are installed by proxies
  - Only if recalculate flag is set `getVal()` will call `evaluate()`
- **Redundant calculations are automatically avoided**
  - Efficient optimization technique for expensive objects like integrals
  - No need to hand-code similar optimization in function code:  
`evaluate()` is only called when necessary

# Writing a function – analytical integrals

- **Analytical integrals are optional!**
- Implementation of analytical integrals is separated in two steps
  - Advertisement of available (partial) integrals:
  - Implementation of partial integrals
- Advertising integrals:  
`getAnalyticalIntegral()`

Integration is requested over all variables in set `allVars`

```
Int_t RooUserFunc::getAnalyticalIntegral( RooArgSet& allVars, RooArgSet& analVars ) const
{
    if (matchArgs(allVars,analVars,x)) return 1 ;
    return 0 ;
}
```

Task of `getAnalyticalIntegral()`:

- 1) find the *largest subset* that function can integrate analytically
- 2) Copy largest subset into analVars
- 3) Return unique identification code for this integral

# Writing a function – advertising integrals

Task of `getAnalyticalIntegral()`:

- 1) find the *largest subset* that function can integrate analytically
- 2) Copy largest subset into `analVars`
- 3) Return unique identification code for this integral

```
Int_t RooUserFunc::getAnalyticalIntegral(
    RooArgSet& allVars, RooArgSet& analVars) const
{
    if (matchArgs(allVars, analVars, x)) return 1 ;
    return 0 ;
}
```

Utility method `matchArgs()` does all the work for you:

If `allVars` contains the variable held in proxy `x`  
variable is copied to `analVars` and `matchArgs()` returns `kTRUE`  
If not, it returns `kFALSE`

## Writing a function – advertising multiple integrals

```
Int_t RooUserFunc::getAnalyticalIntegral(
    RooArgSet& allVars, RooArgSet& analVars) const
{
    if (matchArgs(allVars, analVars, x, m)) return 3 ;
    if (matchArgs(allVars, analVars, m)) return 2 ;
    if (matchArgs(allVars, analVars, x)) return 1 ;
    return 0 ;
}
```

If multiple integrals are advertised,  
test for the largest one first

You may advertise analytical integrals for  
both *real-valued* and *discrete-valued* integrands

## Writing a function – implementing integrals

- Implementing integrals: **analyticalIntegral()**
  - One entry point for *all* advertised integrals

Integral identification code  
assigned by `getAnalyticalIntegral()`

```
Double_t RooGaussian::analyticalIntegral(Int_t code) const
{
    static const Double_t root2 = sqrt(2) ;
    static const Double_t rootPiBy2 = sqrt(atan2(0.0,-1.0)/2.0);

    Double_t xscale = root2*sigma;
    return rootPiBy2*sigma*
        (erf((x.max()-mean)/xscale)-erf((x.min()-mean)/xscale));
}
```

Integration limits for real-valued integrands can be accessed via the `min()` and `max()` method of each proxy

Discrete-valued integrands are always summed over *all* states

# Calculating integrals – behind the scenes

- Integrals are calculated by **RooRealIntegral**
  - To create an **RooRealIntegral** for a **RooAbsReal**

```
RooAbsReal* f; // f(x)
RooAbsReal* int_f = f.createIntegral(x) ;

RooAbsReal* g ; // g(x,y)
RooAbsReal* inty_g = g.createIntegral(y) ;
RooAbsReal* intxy_g = g.createIntegral(RooArgSet(x,y)) ;
```

- Tasks of **RooRealIntegral**
  - Structural analysis of composite
  - Negotiate analytical integration with components PDF
  - Provide numerical integration where needed
- **RooRealIntegral** works **universally** on **simple** and **composite** objects

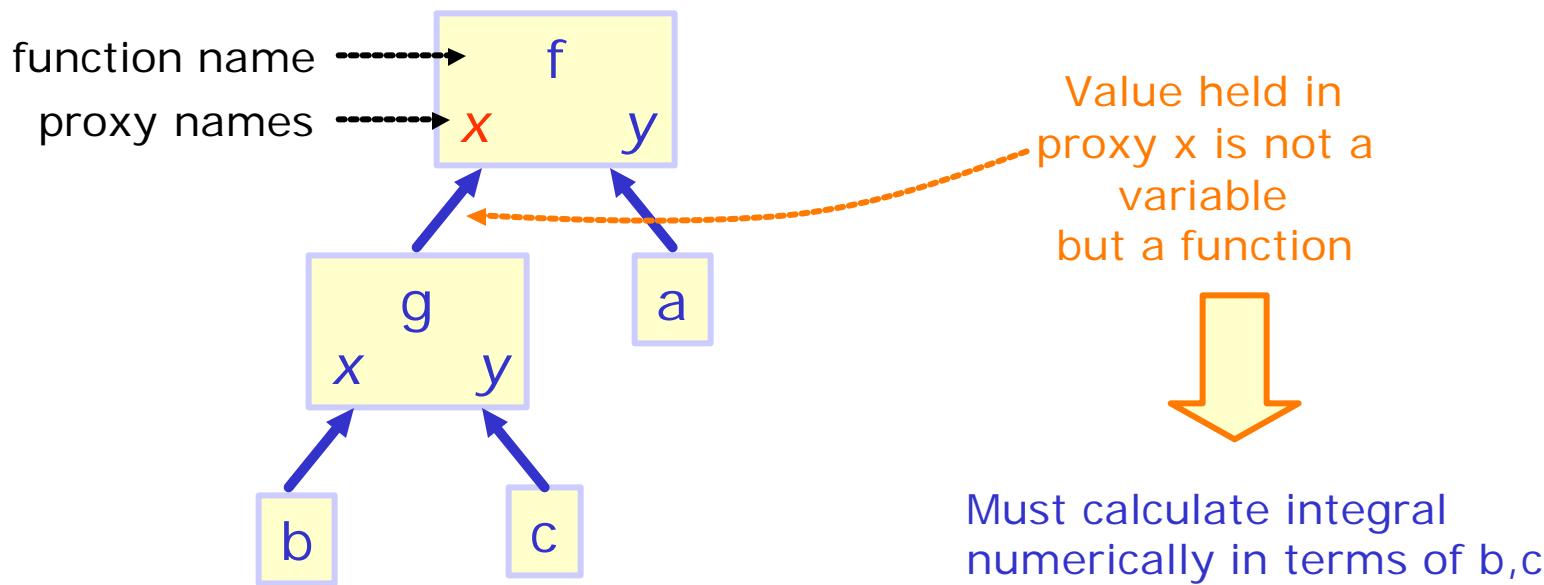
A **RooRealIntegral** is also a **RooAbsReal**

**RooRealIntegral** is RooFit's most complex class!

## Why advertised analytical integrals are sometimes not used

- Integration variable is not a fundamental
  - Suppose  $f(x,y)$  advertises analytical integration over  $x$

$$f(x,a), g(b,c) \rightarrow f(g(b,c),a)$$

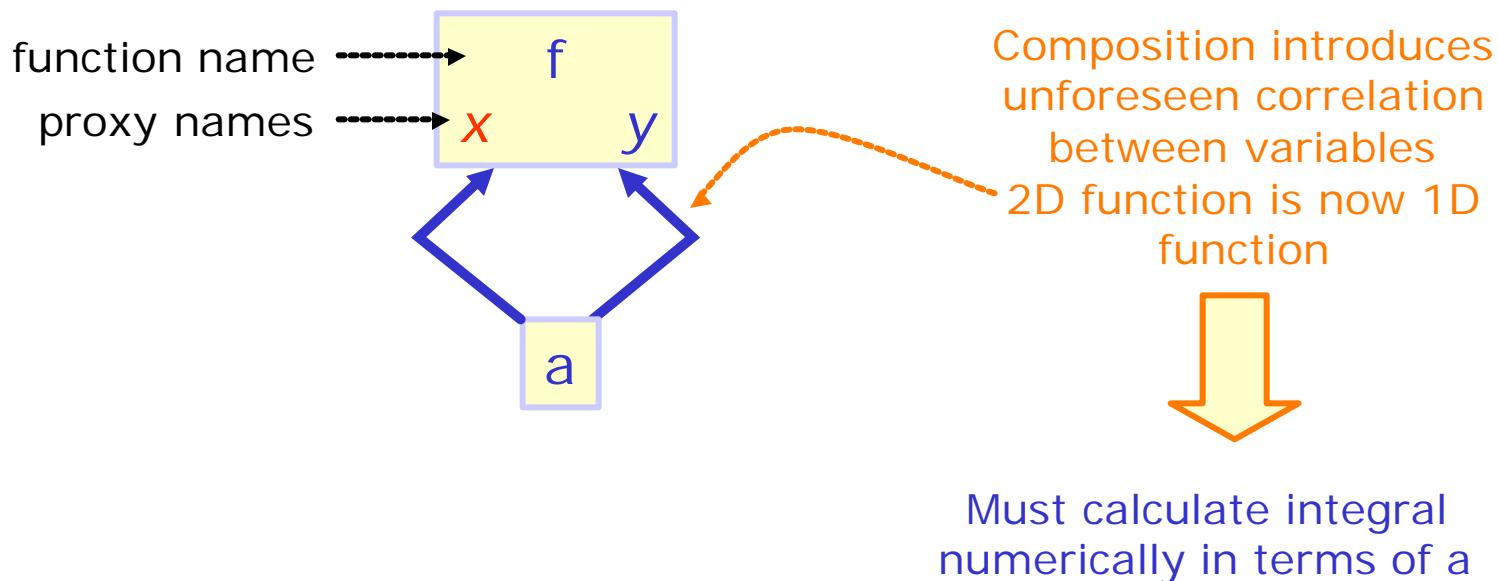


(Exception:  $g(x,y)$  is an invertable function  
(`RooAbsRealLValue`) with a constant Jacobian term)

## Why advertised analytical integrals are sometimes not used

- Function depends more than once on integration variable
  - Suppose  $f(x,y)$  advertises analytical integration over  $x$

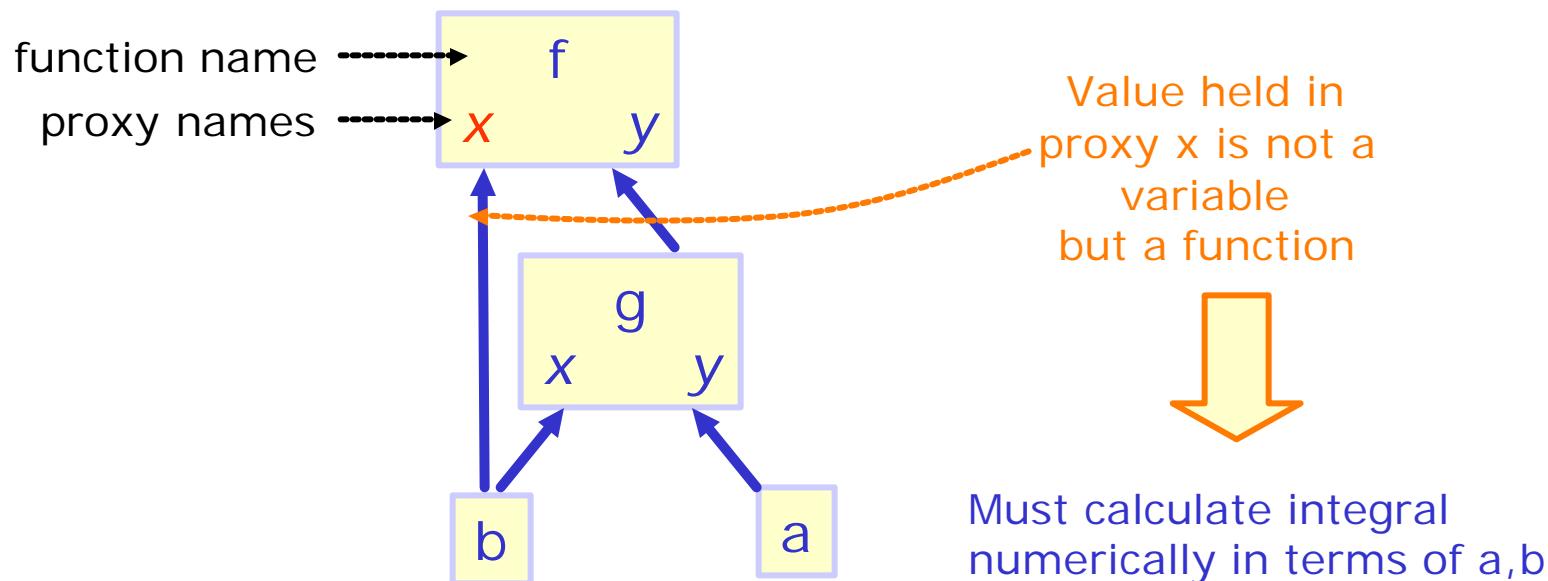
$$f(x, y) \rightarrow f(a, a)$$



## Why advertised analytical integrals are sometimes not used

- Function depends more on integration variable via more than one route
  - Suppose  $f(x,y)$  advertises analytical integration over  $x$

$$f(x,y), g(a,x) \rightarrow f(x, g(a,x))$$



## Class documentation

---

- General description of the class functionality should be provided at the beginning of your .cc file

```
// -- CLASS DESCRIPTION [PDF] --
// Your description goes here
```

Magic line for **THtml**

PDF Keyword causes class to be classified as PDF class

- First comment block in each function will be picked up by **THtml** as the description of that member function
  - Put some general, sensible description here

# Writing a PDF – class **RooAbsPdf**

- Class declaration

```
class RooUserPdf : public RooAbsPdf {  
public:  
    RooUserFunc(const char *
```

PDFs inherit from **RooAbsPdf**

This is the *only* difference with a **RooAbsReal**

**RooAbsPdf::getVal()** will automatically normalize  
your return value by dividing it by the integral of the  
PDF. No further action is needed!

RooRealProxy mean ;

RooRealP

**RooRealIntegral** used for integral calculation

Do

privat

Class

};

**RooAbsPdf** owns RRI configured for last  
normalization configuration. If normalization set  
Changes, new RRI as created on the fly..

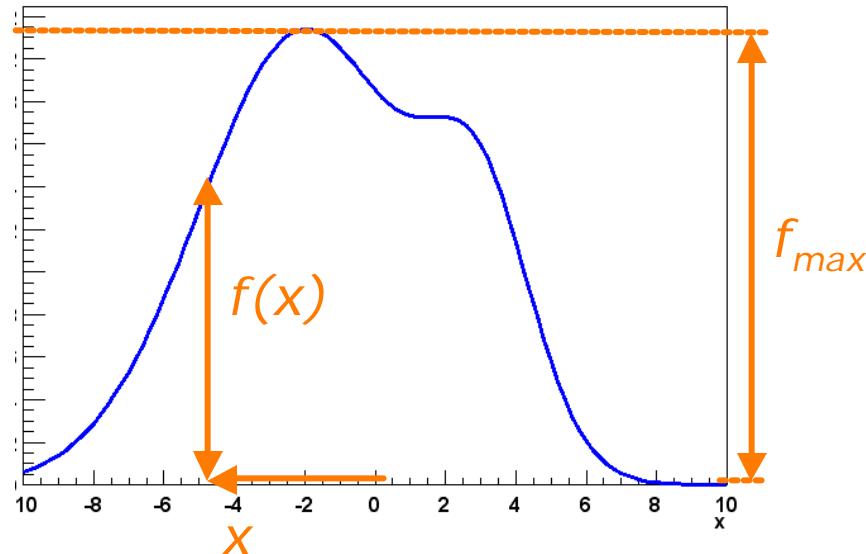
## Writing a PDF – Normalization

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- Do not ***under any circumstances*** attempt to ***normalize*** your PDF in `evaluate()` via ***explicit*** or ***implicit integration***
- You do not know over what variables to normalize
  - In RooFit, parameter/observable distinction is dynamic, a PDF does not have a unique normalization/return value
- You don't even now know how to integrate yourself!
  - Your PDF may be part of a larger composite structure. Variables may be functions, your internal representation may have a difference number of dimensions than the actual composite object.
  - `RooRealIntegral` takes proper care of all this
- But you can help!
  - Advertise all partial integrals that you can calculate
  - They will be used in the normalization when appropriate
    - Function calling overhead is minimal

## PDF Event generation – Accept/reject method

- By default, toy MC generation from a PDF is performed with accept/reject sampling
  - Determine maximum PDF value by repeated random sample
  - Throw a uniform random value ( $x$ ) for the observable to be generated
  - Throw another uniform random number between 0 and  $f_{max}$   
If  $\text{ran} * f_{max} < f(x)$  accept  $x$  as generated event



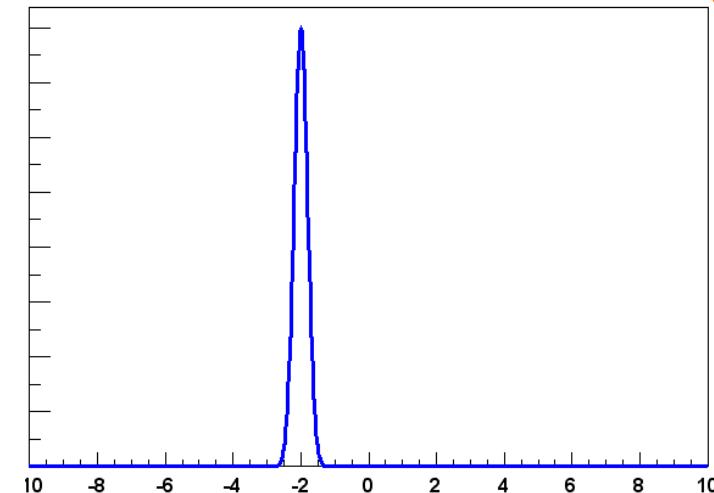
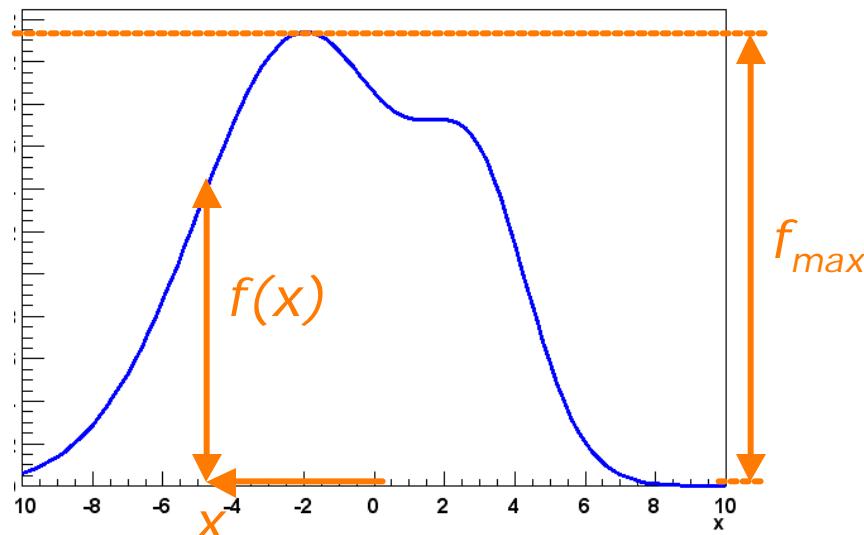
## PDF Event generation – Accept/reject method

- Accept/reject method can be very inefficient

- Generating efficiency is

$$\frac{\int_{x_{\min}}^{x_{\max}} f(x) dx}{(x_{\max} - x_{\min}) \cdot f_{\max}}$$

- Efficiency is very low for narrowly peaked functions
  - Initial sampling for  $f_{\max}$  requires very large trials sets in multiple dimension (~10000000 in 3D)



# PDF Event generation – Optimizations

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- **RooFit 'operator' PDFs provide various optimizations**
- **RooProdPdf** – Components PDFs generated separately
  - Breaks down N dimensional problem to n m-dimensional problems
  - Large initial  $f_{\max}$  sampling penalty not incurred
- **RooAddPdf** – Only one component generated at a time
  - RooAddPdf randomly picks a component PDF to generate for each event. Component probabilities weighted according to fractions
  - Helps to avoid accept/reject sampling on narrowly peaked distributions, if narrow and wide component are separately generated
- **RooSimultaneous** - Only one component generated at a time
  - Technique similar to **RooAddPdf**

## PDF Event generation – Internal generators

---

- For certain PDFs alternate event generation techniques exist that are **more efficient than accept/reject sampling**
  - Example: Gaussian, exponential,...
- If your PDF has such a technique, you can advertise it
  - Interface similar to analytical integral methods  
`RooAbsPdf::getGenerator()`  
`RooAbsPdf::initGenerator()`  
`RooAbsPdf::generateEvent()`
- You **don't** have to be able to generate *all* observables
  - Generator context can combine accept/reject and internal methods within a single PDF
- This is an **optional** optimization
  - PDF can always generate events via accept/reject method

# Writing a PDF – advertising an internal generator

Task of `getGenerator()`:

- 1) find the *largest subset* of observables PDF can generate internally
- 2) Copy largest subset into `dirVars`
- 3) Return unique identification code for this integral

```
Int_t RooUserFunc::getGenerator(  
    RooArgSet& allVars, RooArgSet& dirVars, Bool_t staticOK) const  
{  
    if (matchArgs(allVars,dirVars,x)) return 1 ;  
    return 0 ;  
}
```

Utility method `matchArgs()` does all the work for you:

If `allVars` contains the variable held in proxy `x`  
variable is copied to `dirVars` and `matchArgs()` returns `kTRUE`  
If not, it returns `kFALSE`

# Writing a PDF – advertising an internal generator

- For certain internal generator implementations it can be efficient to do a one-time initialization for each set of generated events
  - Example: precalculate fractions for discrete variables
- **Caveat:** one-time initialization **only safe** if no observables are generated from a **prototype dataset**
  - Only advertise such techniques if staticOK flag is true

```
Int_t RooBMixDecay::getGenerator(const RooArgSet& directVars,
                                  RooArgSet &generateVars, Bool_t staticInitOK) const
{
    if (staticInitOK) {
        if (matchArgs(directVars,generateVars,t,mix,tag)) return 4 ;
        if (matchArgs(directVars,generateVars,t,mix)) return 3 ;
        if (matchArgs(directVars,generateVars,t,tag)) return 2 ;
    }

    if (matchArgs(directVars,generateVars,_t)) return 1 ;
    return 0 ;
}
```

If you advertise multiple configurations, try the most extensive one first

## Writing a PDF – implementing an internal generator

- Implementing a generator: **generateEvent()**
  - One entry point for *all* advertised event generators

```
void RooGaussian::generateEvent(Int_t code)
{
    Double_t xgen ;
    while(1) {
        xgen = RooRandom::randomGenerator()->Gaus(mean,sigma);
        if (xgen<x.max() && xgen>x.min()) {
            x = xgen;
            break;
        }
    }
    return;
}
```

Generator identification code  
assigned by **getGenerator()**

Return generated value  
by assigning it to the proxy

# Writing a PDF – implementing an internal generator

- Static generator initialization: **initGenerator()**
  - This function is guaranteed to be call once before each series of **generateEvent()** calls with the same configuration

```
void RooBMixDecay::initGenerator(Int_t code)
{
    switch (code) {
    case 2:
        {
            // Calculate the fraction of B0bar events to generate
            Double_t sumInt = RooRealIntegral(...).getVal() ;
            _tagFlav = 1 ; // B0
            Double_t flavInt = RooRealIntegral(...).getVal() ;
            _genFlavFrac = flavInt/sumInt ;
            break ;
        }
    }
}
```

Generator identification code assigned by **getGenerator()**

Store your precalculated values in data members

## Writing a convoluted PDF – physics/resolution factorization

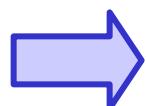
- Physics model and resolution model are implemented separately in RooFit
  - Factorization achieved via a common set 'basis functions'  $f_k$

Implements  $f_i(dt, \dots) \otimes R(dt, \dots)$   
Also a PDF by itself

**RooResolutionModel**

$$P(dt, \dots) = \sum_k c_k(\dots) \underbrace{(f_k(dt, \dots) \otimes R(dt, \dots))}_{\text{RooConvolutedPdf (physics model)}}$$

- Implements  $c_k$   
- Declares list of  $f_k$  needed



**No magic:** You must still calculate the convolution integral yourself, but factorization enhances modularity & flexibility for end user

## Writing a convoluted PDF – class `RooConvolutedPdf`

- Class declaration

```
class RooBMixDecay : public RooConvolutedPdf {  
public:
```

Convolutable PDF classes inherit from  
`RooConvolutedPdf` instead of `RooAbsPdf`

```
RooBMixDecay(const RooBMixDecay& other, const char* name=0);  
virtual TObject* clone(const char* newname) const ;  
virtual ~RooBMixDecay();
```

```
virtual Double_t coefficient(Int_t basisIndex) const ;
```

```
protected:
```

Implement `coefficient()` instead of `evaluate()`

```
}
```

## Class `RooConvolutedPdf` – Constructor implementation

- Constructor must declare all **basis functions** used

```
RooBMixDecay::RooBMixDecay(const char *name, const char *title,...) :  
    RooConvolutedPdf(name,title,model,t), ...  
{  
    // Constructor  
    _basisExp = declareBasis("exp(-abs(@0)/@1)",  
                             RooArgList(tau)) ;  
    _basisCos = declareBasis("exp(-abs(@0)/@1)*cos(@0*@2)",  
                            RooArgList(tau,dm)) ;  
}
```

Call `declareBasis()` for each basis functions used in this PDF

Supply basis function parameters here

Return code assign unique integer code to each declared basis

Name of basis function is `RooFormulaVar` expression  
@0 is convolution variable  
@1..@n are basis function parameters

## Class `RooConvolutedPdf` – Coefficient implementation

- Method `coefficient()` implements all coefficient values

Requested index is one of the basis function codes returned by `declareBasis()`

```
Double_t RooBMixDecay::coefficient(Int_t basisIndex) const
{
    if (basisIndex==_basisExp) {
        return (1 - _tagFlav*_delMistag) ;
    }

    if (basisIndex==_basisCos) {
        return _mixState*(1-2*_mistag) ;
    }
    return 0 ;
}
```

- At this point class is complete and functional

## Class `RooConvolvedPdf` – Analytical integrals

---

- You can **optionally** advertise and implement **analytical integrals** for your **coefficient functions**
  - Interface similar to analytical integrals in `RooAbsReal`
- Advertising coefficient integrals
  - Method identical to `RooAbsReal::getAnalyticalIntegral()`, just the name is different

```
Int_t getCoefAnalyticalIntegral(RooArgSet& allVars,  
                                RooArgSet& analVars) const ;
```

- Implementing coefficient integrals
  - Method similar to `RooAbsReal::analyticalIntegral()`
  - One extra argument to identify the coefficient in question

```
Double_t coefAnalyticalIntegral(Int_t coef,  
                               Int_t code) const ;
```

## Class `RooConvolutedPdf` – Internal generator implementation

---

- You can **optionally** advertise and implement an **internal generator** for the *unconvoluted* PDF function
  - Methods identical to regular PDF generator implementation
- An internal generator will **greatly accelerate** toyMC generation from a convoluted PDF
  - If both physics PDF and **resolution model** provide **internal generators**, then events can be generated as

$$x_{P \otimes R} = x_P + x_R$$

- i.e. **no convolutions integrals** need to be **evaluated**
- Only works with internal generator implementations because both  $x_P$  and  $x_R$  must be generated on an unbound domain for this technique to work
    - Accept reject sample doesn't work on unbound domains

## Writing a resolution model – physics/resolution factorization

---

- Physics model and resolution model are implemented separately in RooFit
  - Factorization achieved via a common set 'basis functions'  $f_k$

Implements  $f_i(dt, \dots) \otimes R(dt, \dots)$   
Also a PDF by itself

**RooResolutionModel**

$$P(dt, \dots) = \sum_k c_k(\dots) \underbrace{\left( f_k(dt, \dots) \otimes R(dt, \dots) \right)}_{\text{RooConvoltedPdf (physics model)}}$$

- Implements  $c_k$   
- Declares list of  $f_k$  needed

## Writing a resolution model PDF – class `RooResolutionModel`

- Class declaration

```
class RooGaussModel : public RooResolutionModel {  
public:
```

Resolution model classes inherit from  
`RooResolutionModel` instead of `RooAbsPdf`

```
    RooGaussModel(const RooBMixDecay& other, const char* name=0);  
    virtual TObject* clone(const char* newname) const ;  
    virtual ~RooGaussModel();
```

Method `basisCode()` advertises supported basis functions

```
    virtual Int_t basisCode(const char* name) const = 0 ;  
    virtual Double_t evaluate() const ;
```

```
protected:
```

```
    ...  
    ClassDef(RooGaussModel, 1)  
};
```

`evaluate()` returns *regular or convoluted PDF*  
depending on internal state

## Class `RooResolutionModel` – Advertising basis functions

- Function `basisCode()` assigns unique integer code to each supported basis function

```
Int_t RooGaussModel::basisCode(const char* name) const
{
    if (!TString("exp(-@0/@1)").CompareTo(name)) return 1 ;
    if (!TString("exp(@0/@1)").CompareTo(name)) return 2 ;
    if (!TString("exp(-abs(@0)/@1)").CompareTo(name)) return 3 ;
    if (!TString("exp(-@0/@1)*sin(@0*@2)").CompareTo(name)) return 4 ;
    if (!TString("exp(@0/@1)*sin(@0*@2)").CompareTo(name)) return 5 ;
    if (!TString("exp(-abs(@0)/@1)*sin(@0*@2)").CompareTo(name)) return 6;
    if (!TString("exp(-@0/@1)*cos(@0*@2)").CompareTo(name)) return 7 ;
    if (!TString("exp(@0/@1)*cos(@0*@2)").CompareTo(name)) return 8 ;
    if (!TString("exp(-abs(@0)/@1)*cos(@0*@2)").CompareTo(name)) return 9;
    return 0 ;
}
```

Return 0 if basis  
function is not supported

## Class RooResolutionModel – Implementing `evaluate()`

- `evaluate()` returns both convoluted and unconvoluted PDF value

`currentBasisCode()` returns the ID of the basis function we're convoluted with. If zero, not convoluted is requested

```
Double_t RooGaussModel::evaluate() const {
    Int_t code = currentBasisCode();

    if (code==0) {
        // return unconvoluted PDF value ;
    }

    if (code==1) {
        // Return PDF convoluted with basis function #1

        // Retrieve basis function parameter value
        Double_t tau = basis().getParameter(1)->getVal();
    }
}
```

## Class RooResolutionModel – Implementing `evaluate()`

- `evaluate()` returns both convoluted and unconvoluted PDF value

```
Double_t RooGaussModel::evaluate() const
{
    Int_t code = currentBasisCode();
    basis() returns a reference
    to the RooFormulaVar
    representing the current basis function
    if (code==1,
        // Return PDF convoluted with ...
        // Retrieve basis function parameter value
        Double_t tau = basis().getParameter(1)->getVal();
    }
}
```

`basis()` returns a reference to the **RooFormulaVar** representing the current basis function

convoluted PDF value

`getParameter(n)` returns a **RooAbsReal** reference to the  $n^{\text{th}}$  parameter of the **RooFormulaVar**

## Class RooResolutionModel – Analytical integrals

- Advertising and implementing analytical integrals works the same way as in RooAbsPdf

Advertisement and implementation should reflect the 'current' convolution indicated by `currentBasisCode()`

```
Int_t RooGaussModel::  
    getAnalyticalIntegral(RooArgSet& allVars,  
                          RooArgSet& analVars) const  
{  
    switch(currentBasisCode()) {  
        // Analytical integration capability of raw PDF  
        case 0:  
            if (matchArgs(allVars,analVars,convVar())) return 1 ;  
            break ;  
  
        // Analytical integration capability of convoluted PDF  
        case 1:  
            if (matchArgs(allVars,analVars,convVar())) return 1 ;  
            break ;  
    }  
}
```

## Class `RooResolutionModel` – Internal generator implementation

---

- You can **optionally** advertise and implement an **internal generator** for the *unconvoluted* resolution model
  - Methods identical to regular PDF generator implementation

## Class **RooAbsGoodnessOfFit** – Goodness of fit

---

- No time left to write this section... (sorry!)

## Debugging

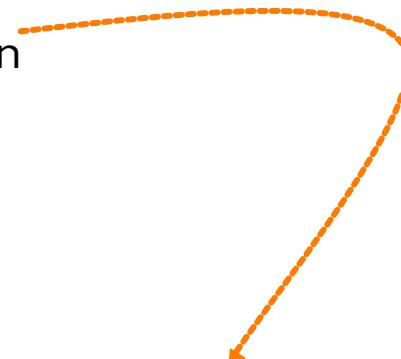


- ROOT and gdb/dbx
- Finding memory leaks
- Tracing function evaluation
- Checking integrals & generators
- Profiling

# Using the system debugger

---

- Compiled applications linked with RooFit
  - Just use '`gdb/dbx <executable>`'
- Interactive ROOT
  - You can use `gdb/dbx` to debug your compiled RooFit class
  - Trick: attach debugger to already running ROOT process
    1. Start interactive ROOT the usual way
    2. In a separate shell on the same host  
attach `gdb/dbx` to the running ROOT session
    3. Resume running of ROOT  
`gdb> continue`
    4. Execute the code you want to test



```
#!/bin/sh
line=`ps -wwfu $USER | grep root.exe | grep -v grep | tail -1`
if [ "$line" = "" ] ; then
  echo "No ROOT session running"
  exit 1
fi
set $line
exec gdb $8 $2
```

# Finding memory leaks

- **RooTrace** utility keeps track of RooFit object allocation

```
RooTrace::active(kTRUE)

RooRealVar x("x","x",-10,10) ;
RooGaussian g("g","g",x,RooConst(0),RooConst(1)) ;

RooTrace::dump(cout);
List of RooFit objects allocated while trace active:
00086b7118 :           RooRealVar - x
00086aa178 :           RooArgList - RooRealVar Constants Database
00086b7658 :           RooConstVar - 0.000000
00086b7b08 :           RooConstVar - 1.000000
00086bc3e8 :           RooGaussian - g
```

# Finding memory leaks

---

- You can do incremental leak searches

```
RooTrace::active(kTRUE)

RooRealVar x("x","x",-10,10) ;
RooGaussian g("g","g",x,RooConst(0),RooConst(1)) ;

RooTrace::mark() ; // mark all objects created sofar

RooGaussian g2("g2","g2",x,RooConst(2),RooConst(1)) ;

// Dump only objects created since last mark
RooTrace::dump(cout,kTRUE);
List of RooFit objects allocated while trace active:
00086c8f50 :           RooConstVar - 2.000000
00086c9400 :           RooGaussian - g2
5 marked objects suppressed
```

## Tracing function evaluation

---

- When you have many instances of a single class it can be more useful to trace function evaluation with printed messages than via debugger
  - Debugger breakpoint will stop in every instance of your class even if you only want to examine a single instance
- RooFit provides system-wide tracing techniques
  - `RooAbsArg::setVerboseDirty(kTRUE)`
    - Track lazy evaluation logic of RooAbsArg classes
    - May help to understand why your evaluate() doesn't get called
  - `RooAbsArg::setVerboseEval(Int_t level)`
    - Level 0 – No messages
    - Level 1 – Print one-line message each time a normalization integral is recalculated
    - Level 2 – Print one-line message each time a PDF is recalculated
    - Level 3 – Provide details of convolution integral recalculations

## Tracing function evaluation

---

- And object-specific tracing techniques
  - `pdf->setTraceCounter(Int_t n, Bool_t recursive)`
  - Prints one-lines messages for the next `n` times `pdf` is evaluated
  - If recursive option is set, trace counter is also set for all component PDFs of `pdf`
  - Useful in fitting/likelihood calculations where a single likelihood evaluation can trigger thousands of PDF evaluations

## Checking analytical integrals and internal generators

---

- Function integrals and PDF event generators both have a numerical backup solution
  - You can use those as a cross check to validate your function/PDF-specific implementation
- Integrals
  - `RooAbsReal::forceNumInt(kTRUE)` will disable the use of any advertised analytical integrals
- Generators
  - `RooAbsPdf::forceNumGen(kTRUE)` will disable the use of any advertised internal PDF generator methods

# Profiling

---

- To run the profiler you must build your test application as a standalone executable
  - compile & link with `-pg` flag

```
#include "TROOT.h"
#include "TApplication.h"

// Instantiate ROOT system
TROOT root("root", "root");
int main(int argc, char **argv)
{
    // Instantiate graphics event handler
    TApplication app("TAppTest",&argc,argv) ;

    // User code goes here
}
```

- *You cannot have any RooFit classes as global variables*
  - Prior instantiation of TROOT needed, but cannot be guaranteed
- Place your driver executable in the **RooFitModels** directory and list it as a binary target in the **GNUMakefile**

## Outlook

---

- New goodness-of-fit calculation classes will be introduced soon (~1 week)
  - Likelihood and ChiSquare as examples.
  - Complete function optimization support for likelihood fitting now generically available for all goodness of fits
  - Built-in support for handling RooSimultaneous PDFs
  - Support for parallel execution on multi-CPU hosts
    - No support from user code needed except prescription to merge partial results  
(Default implementation adds partial results)